

# Measurement of Longitudinal Motion at 150MeV FFAG

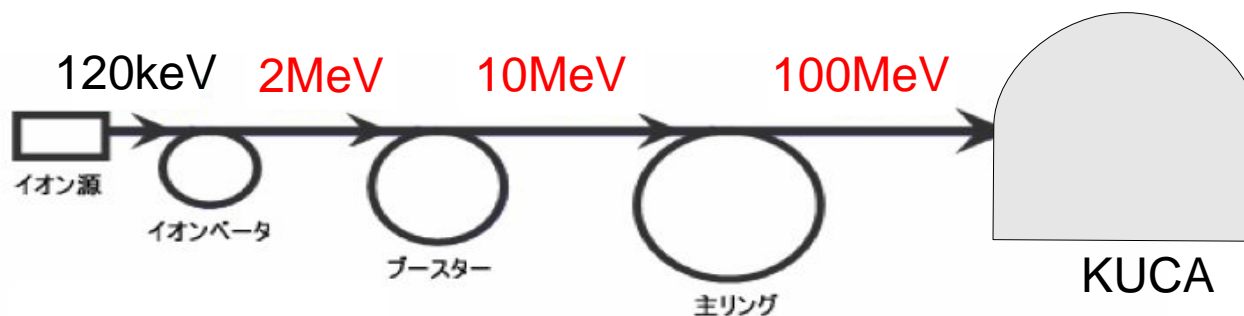
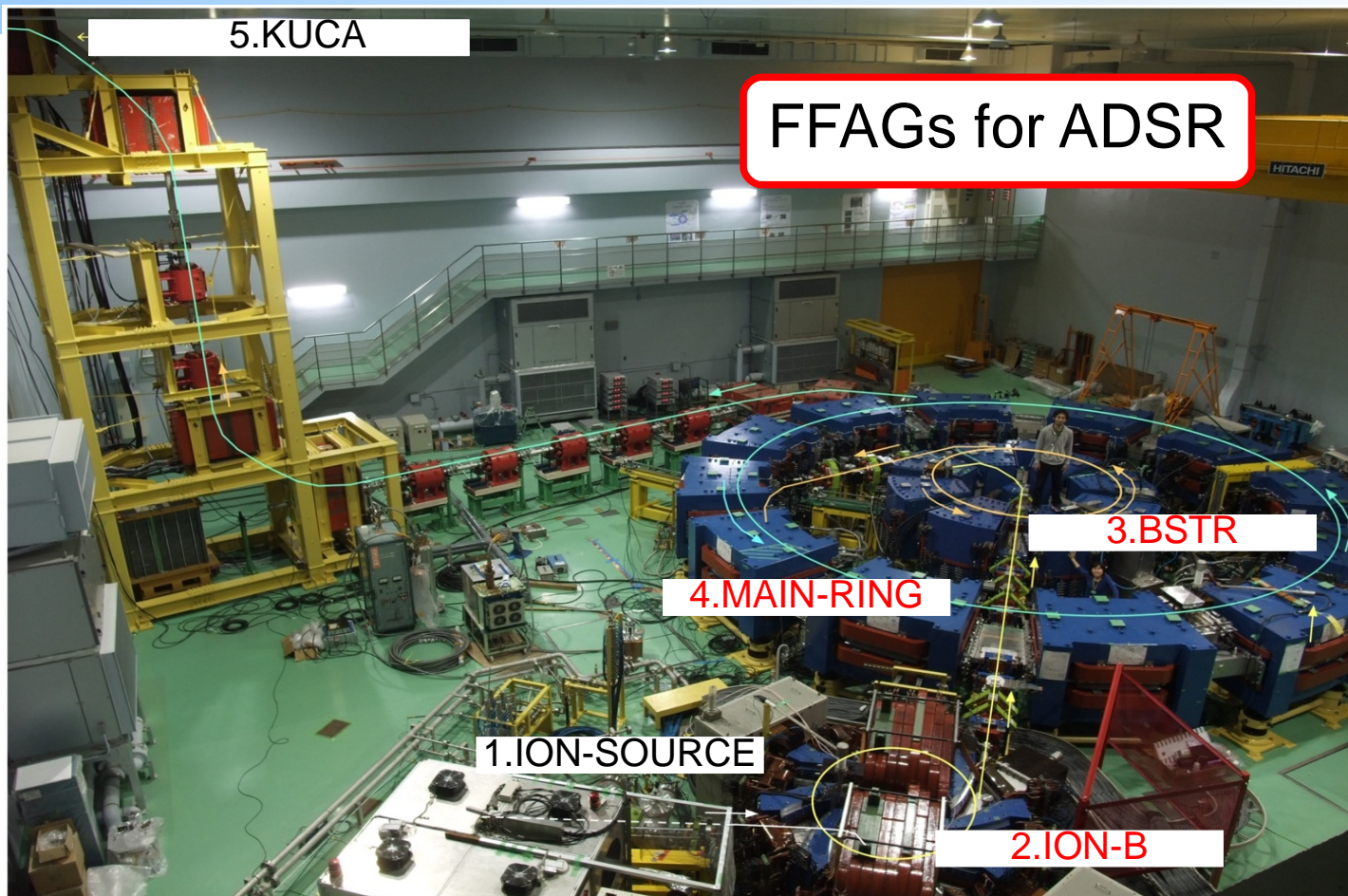
Fukui University  
Hideki Imazu

# Outline

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- FFAG accelerators for ADSR
- Transparency of 150MeV FFAG Ring at KURRI
- Measurement of Longitudinal Motion
- Analysis of Synchrotron oscillation
- Summary & Next step

# FFAGs for ADSR



## FFAG for ADSR

Three step acceleration

1.ION-SOURCE

2.ION-B

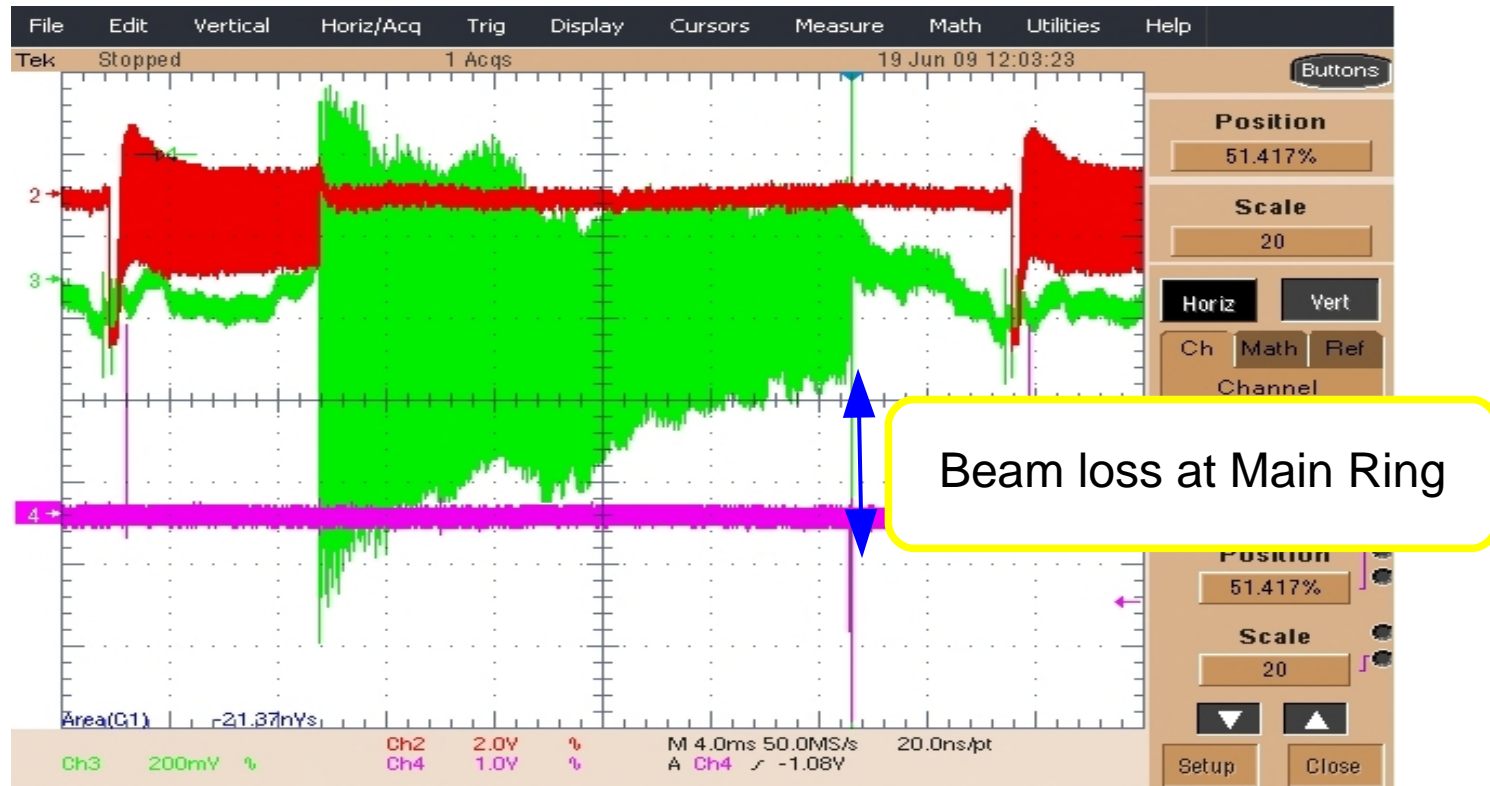
3.BSTR

4.MAIN-RING

Producing neutron  
by irradiating  
proton beam to target

5.Neutron is supplied  
for KUCA

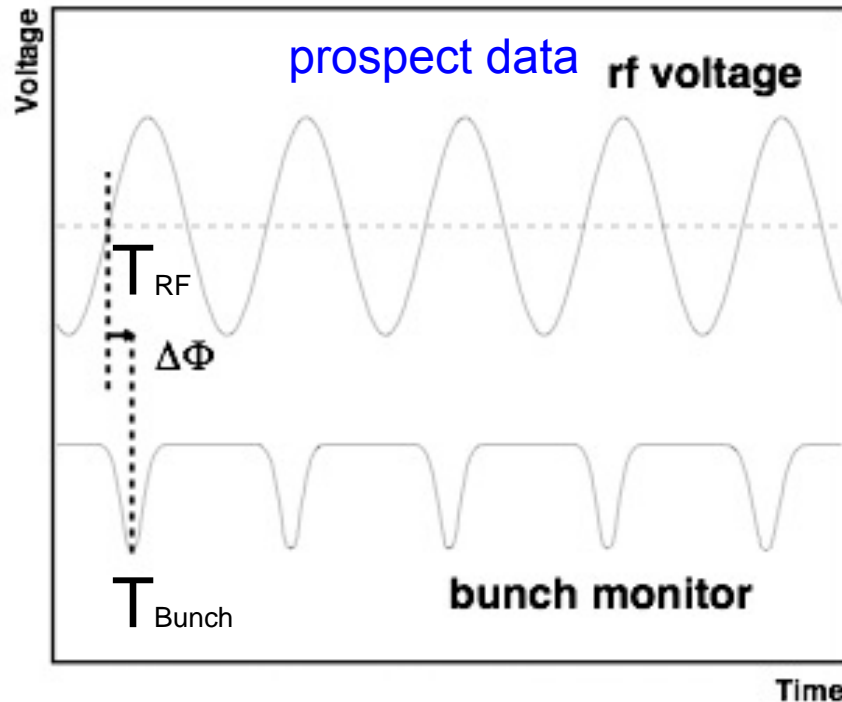
# Transparency of 150MeV FFAG at KURRI



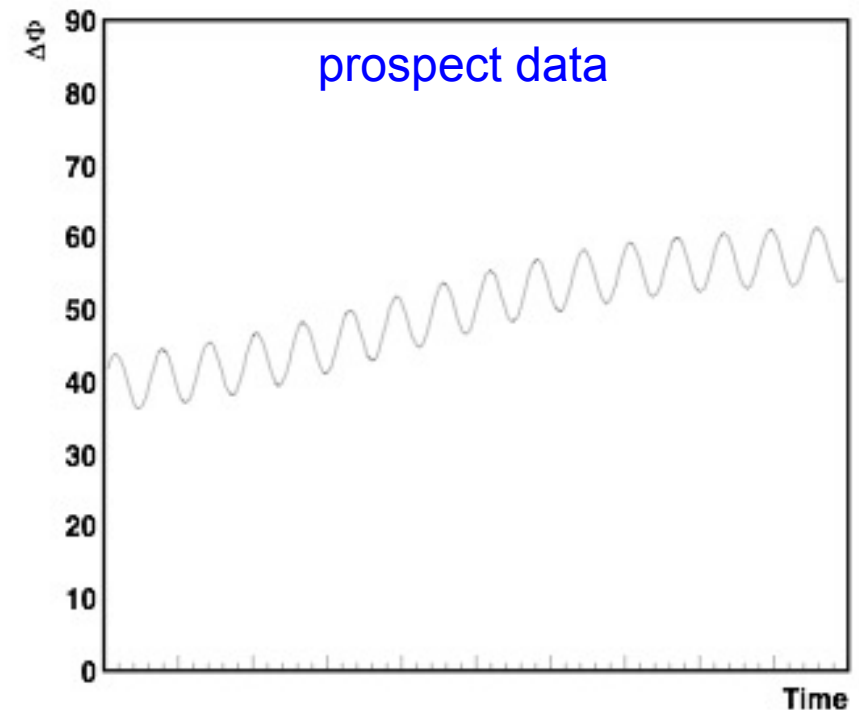
Longitudinal instability ?

Experimentally, obtain real  $\phi$ s

# Measurement Scheme of Longitudinal Motion



$$\Delta\Phi \longleftrightarrow 2 \times (T_{Bunch} - T_{RF})/T_{rev}$$

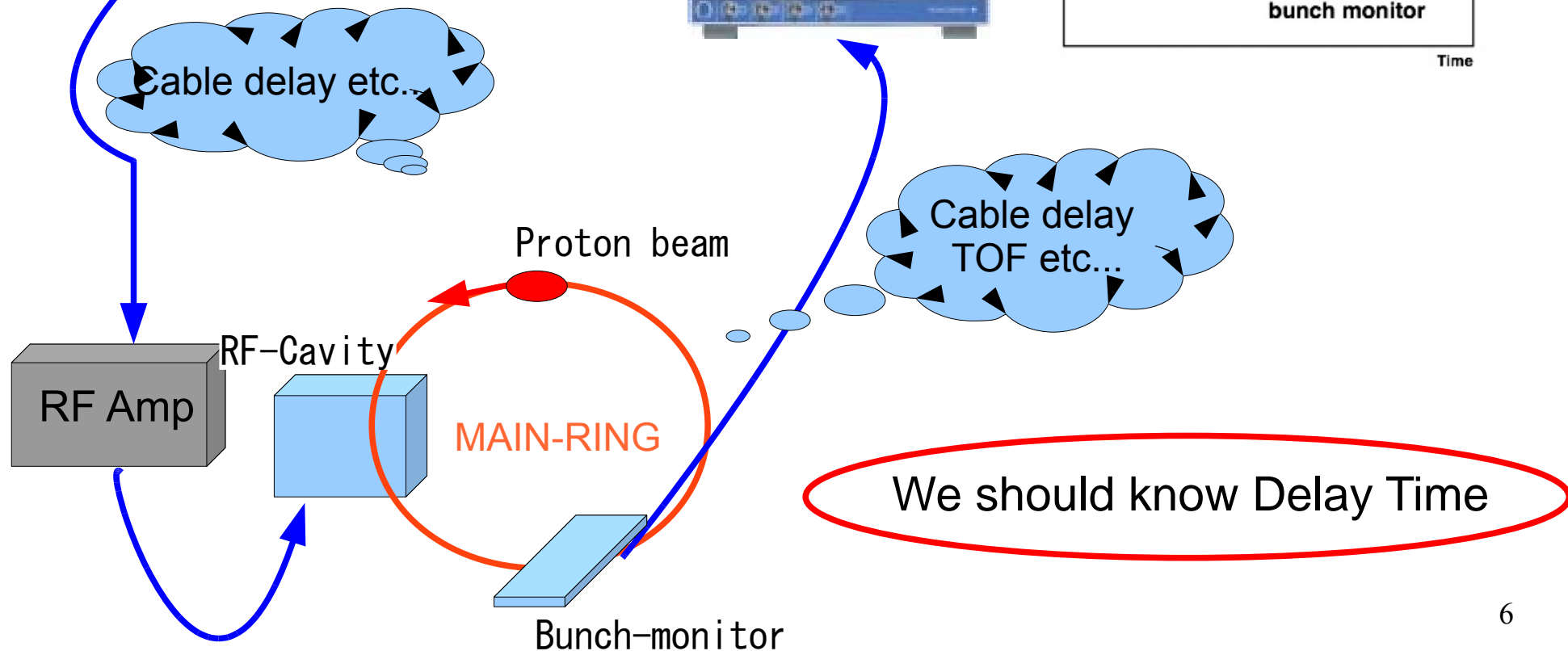
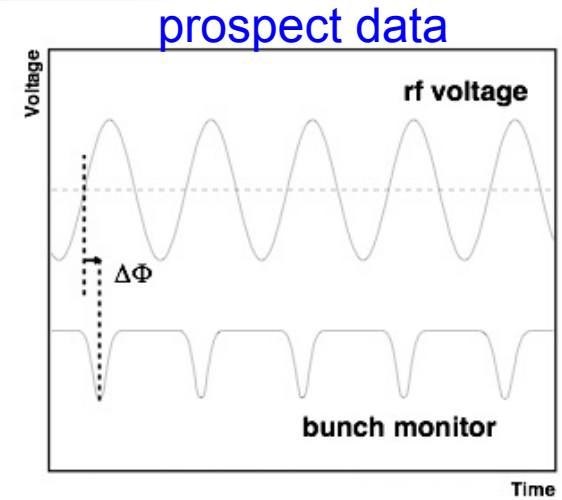


# Experimental setup

Waveform generator (AWG)

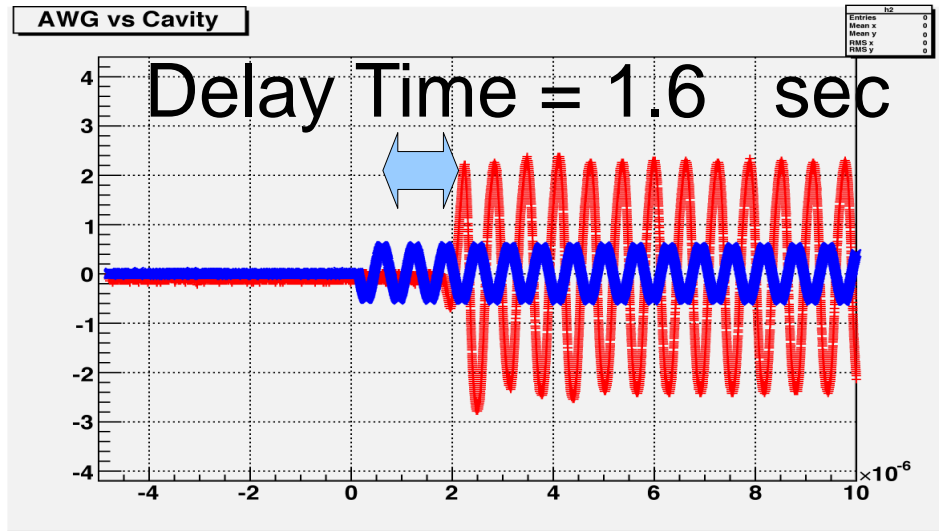


Oscilloscope



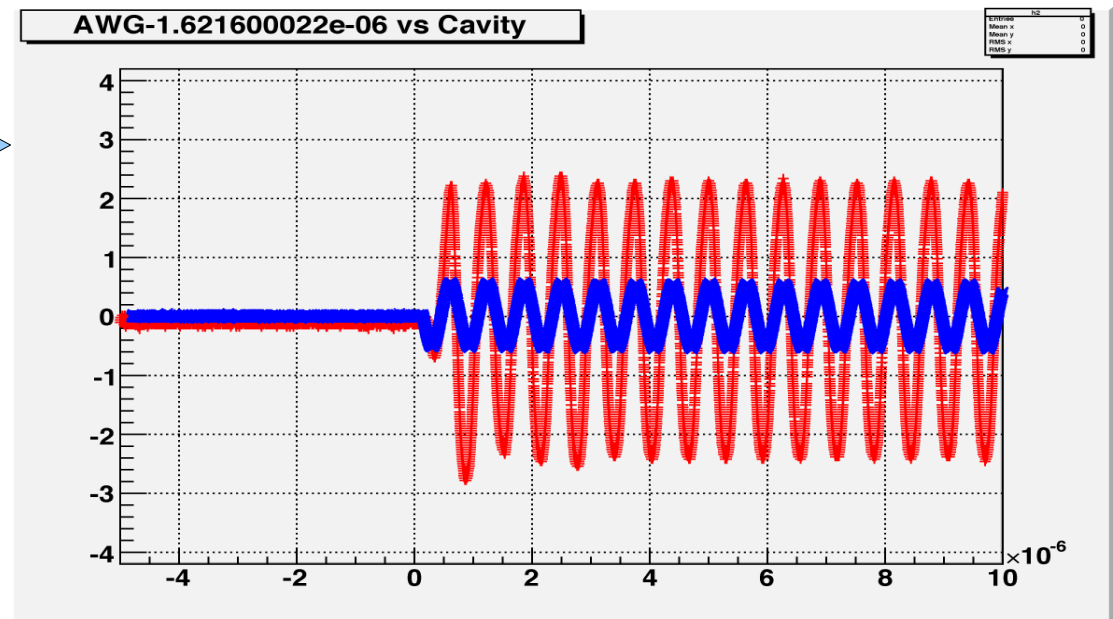


# Measurement of Delay Time

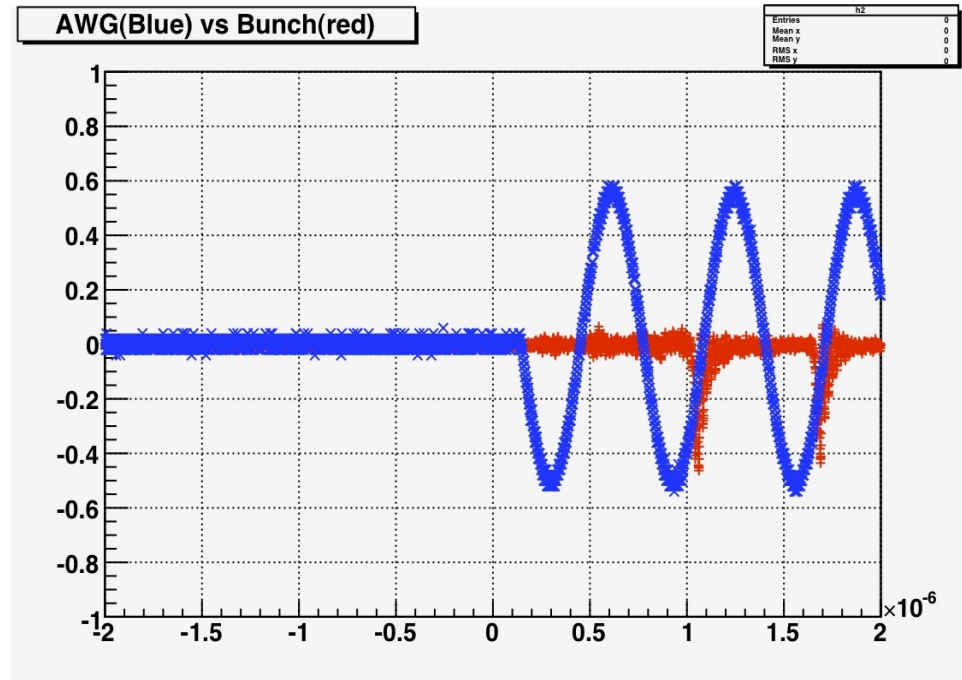


Red -> Cavity-RF  
Blue -> Wave form generator(AWG)

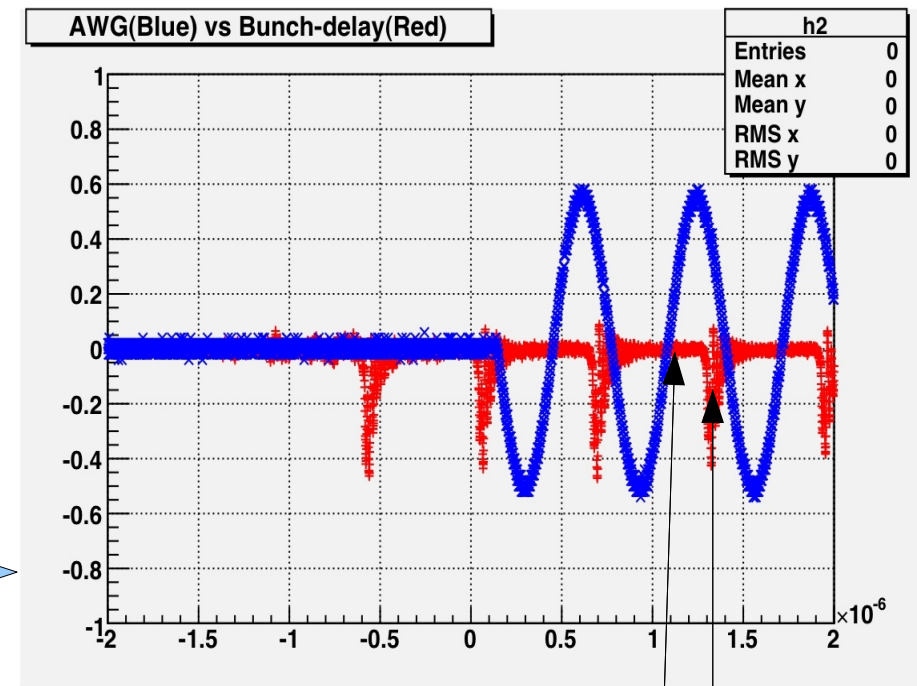
After correction  
of delay time



# Beam Bunch v.s Output of wave form generator (AWG)



Red-> Bunch Beam  
Blue-> AWG-RF



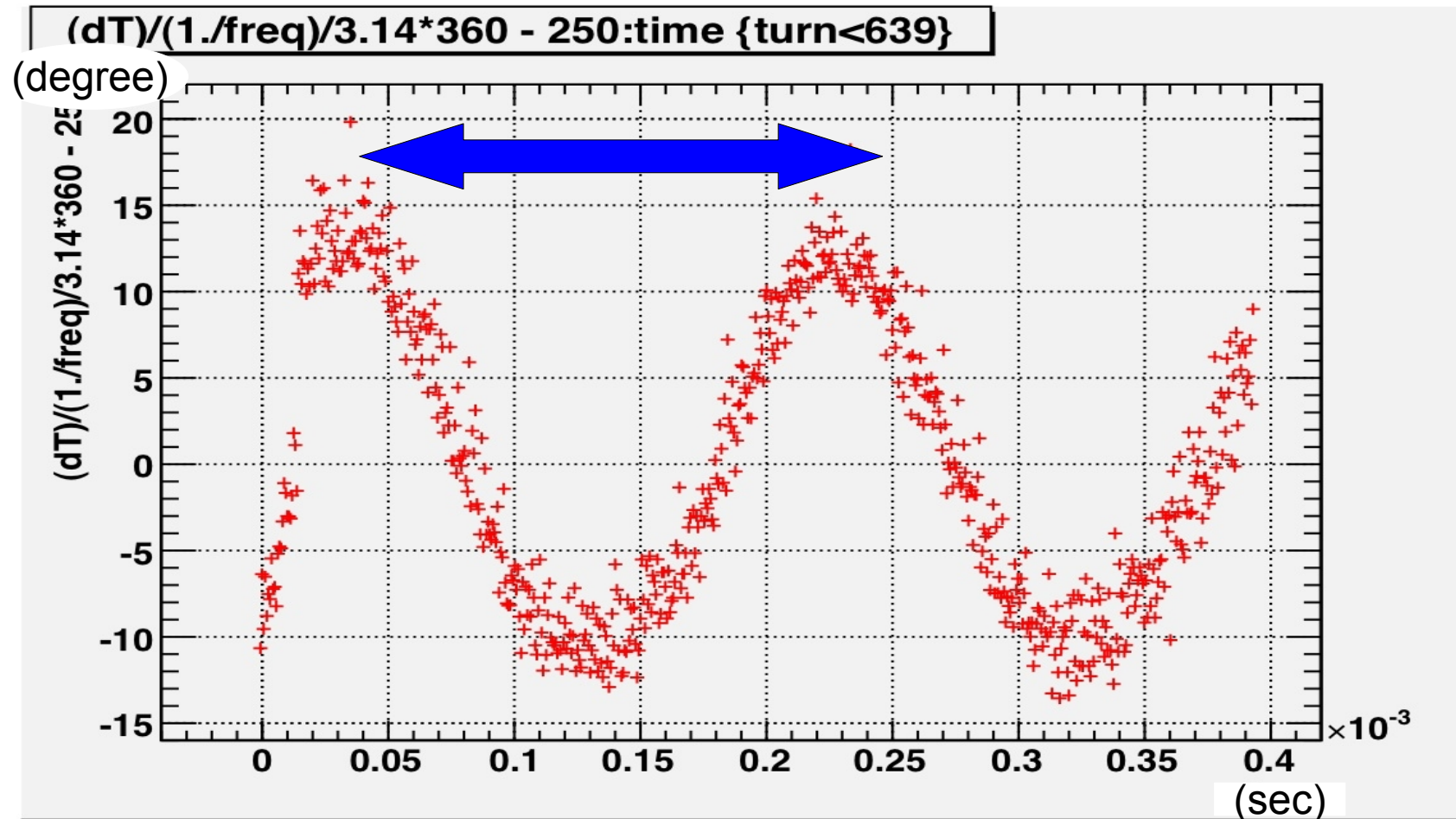
Correction of Delay time ( $1.6\mu\text{sec}$ )

$$\Delta\Phi \longleftrightarrow 2 \times (T_{\text{Bunch}} - T_{\text{RF}})/T_{\text{rev}}$$

$$T_{\text{Bunch}} - T_{\text{RF}} \quad 8$$



# Synchrotron oscillation



synchrotron oscillation frequency  $\rightarrow$  4.3kHz

# Estimation of Synchrotron oscillation frequency

Parameter of Main Ring

$$\frac{\omega_0}{2\pi} = \frac{\omega_s}{2\pi\beta_s} = 10.2 \quad \begin{array}{l} [\text{MHz}] \\ [\text{keV}] \end{array}$$

$$eV = 2$$

$$\eta = -0.709$$

$$\phi_s = 50 \quad [\text{deg}]$$

$$E_s = 938.340 + 11.6 \quad [\text{MeV}]$$

$$\Omega_s = \frac{\omega_0}{2\pi} \sqrt{\frac{-eV \eta \cos \phi_s}{2\pi E_s}}$$

$$\Omega_s = 4.39 \text{ kHz}$$

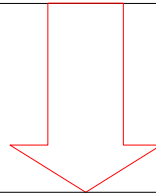
Good Agreement between analysis and calculation

Analysis result 4.3kHz

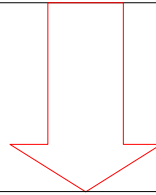
Calculation result 4.39kHz

# Summary

Propose new method to obtain real  $s$



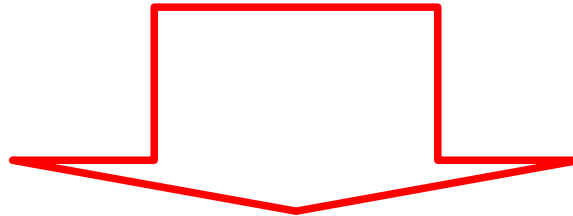
Using obtained  $s$ , Synchrotron oscillation frequency was calculated, experimentally



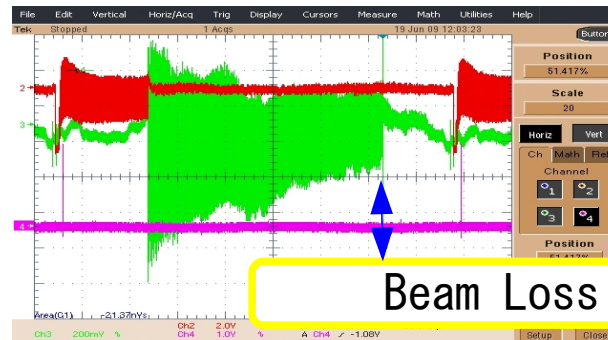
Since good agreement between analytic value and experimental value, new method has been confirmed

# Next Step

Proceed the analysis to obtain real  $\Phi_s$

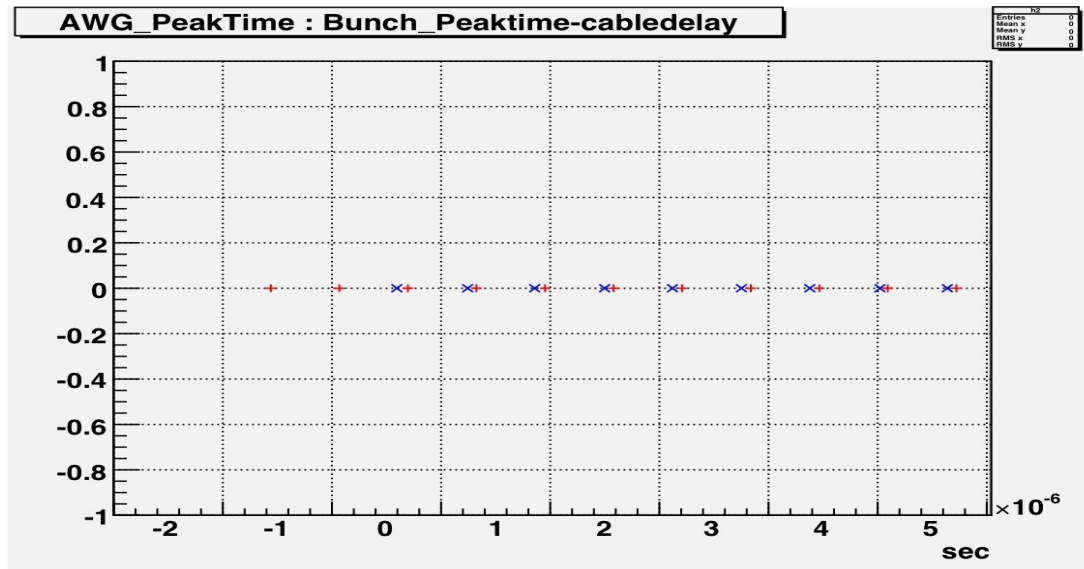


Optimize the RF pattern to avoid beam loss

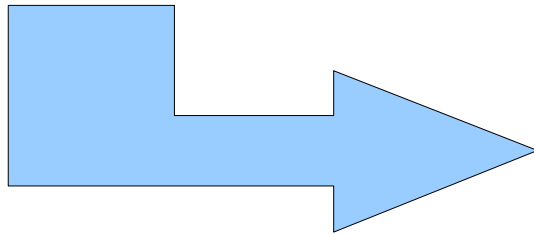


# 付録

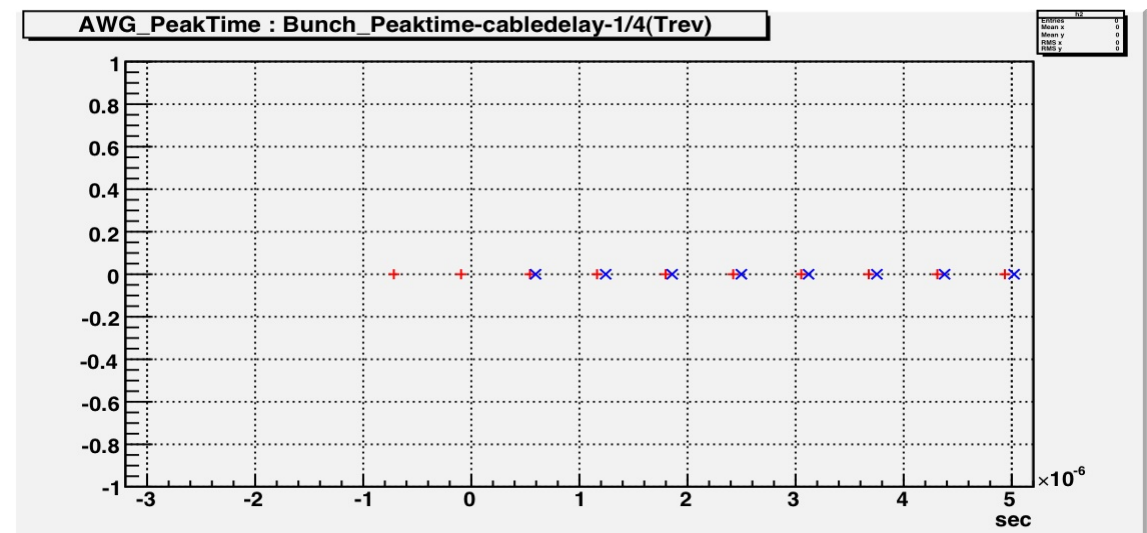
# Peak Bunch timeとPeak RF timeの cable delay T0F 後の関係



Red-> Peak Bunch time  
Blue-> Peak AWG-RF time

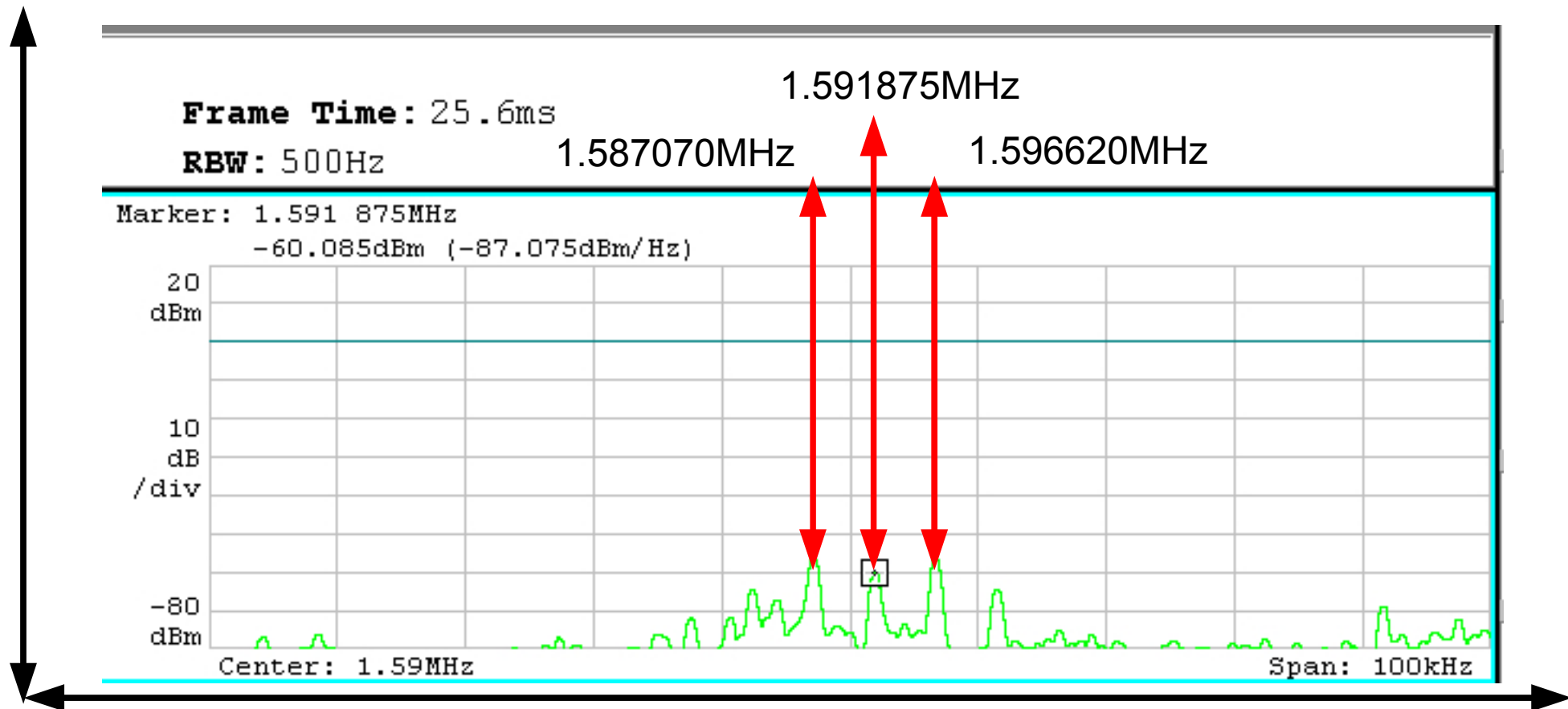


Cable delay  
& TOF  $(1/4)T_{rev}$





# synchrotron oscillation measurement using Realtime spectrum analyzer



synchrotron oscillationL\_side 4.8kHz  
synchrotron oscillationR\_side 4.7kHz

# 位相安定性の原理とは

$$B(r) = B_0 \left( \frac{r}{r_0} \right)^k$$

$$\alpha_p = \frac{dL/L}{dp/p} = \frac{1}{k+1}$$

$\alpha_p$  : モーメントムコンパクション  
 $L$  : 平衡軌道  
 $p$  : 運動量  
 $\eta$  : スリップファクター

$$T = \frac{L}{v} \quad \frac{dT}{T} = \frac{dL}{L} - \frac{dv}{v}$$

$$\frac{dv}{v} = \frac{1}{\gamma^2} \frac{dp}{p} \quad \frac{dT}{T} = \left( \frac{1}{\gamma^2} - \alpha_p \right) \frac{dp}{p} = \eta \frac{dp}{p}$$

$$\eta = \frac{1}{\gamma^2} - \frac{1}{k+1}$$

式中のk値による、モーメントムコンパクション及びスリップファクターの値がシンクロトロン振動の挙動を決定する。