

# Measurement of betatron tunes in KURRI FFAG Main ring



Y.Takahoko (FUKUI university)  
M.Takashima (KYOTO university)  
Y.Kuriyama (KYOTO university)

Purpose

Introduction of FFAG at KURRI

Experiment

Result

Summary

Future

# Purpose

Beam loss exists at main ring

Beam loss at main ring

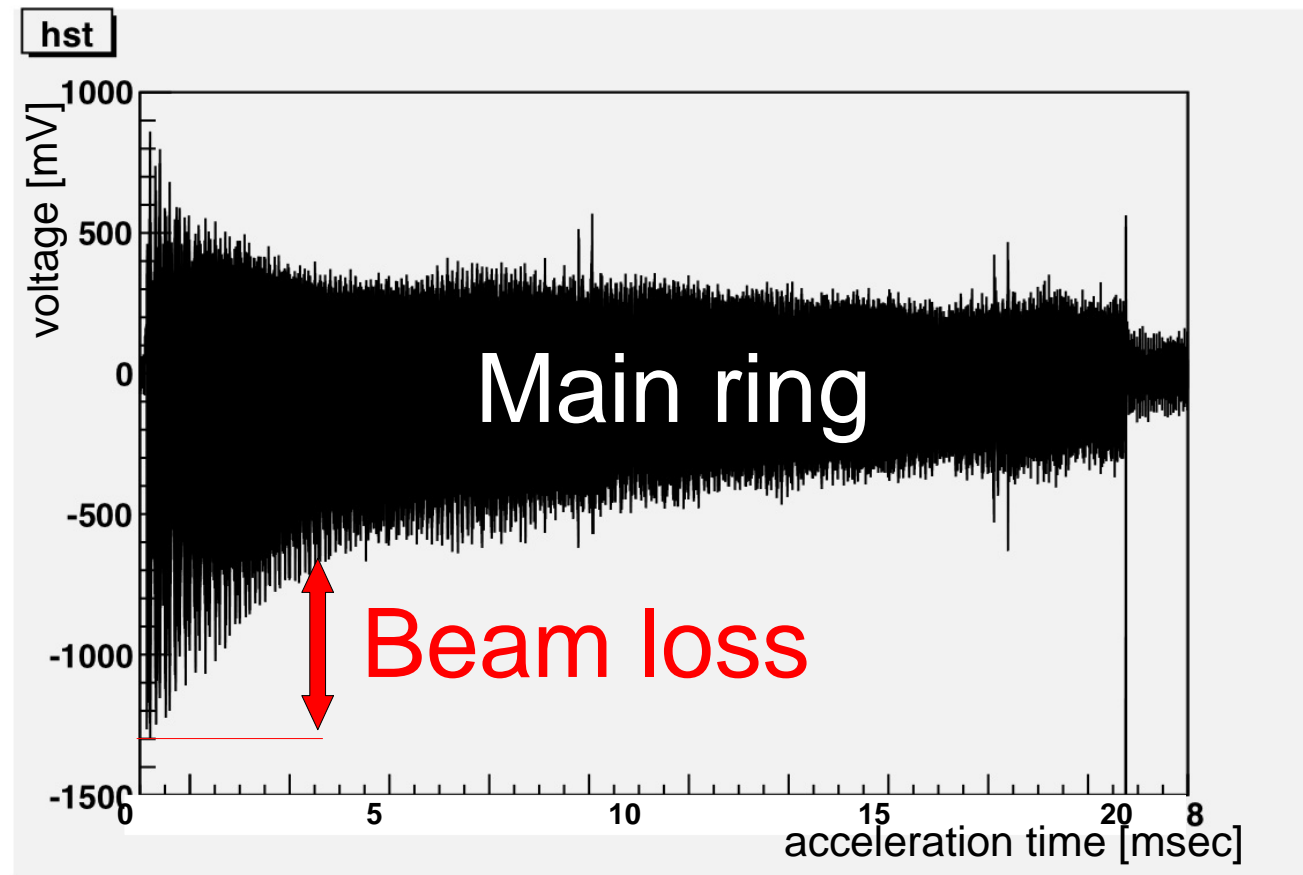
➡ Longitudinal instability ?



Transverse instability ?



Measurement of  
betatron tunes  
at Main ring



5.KUCA

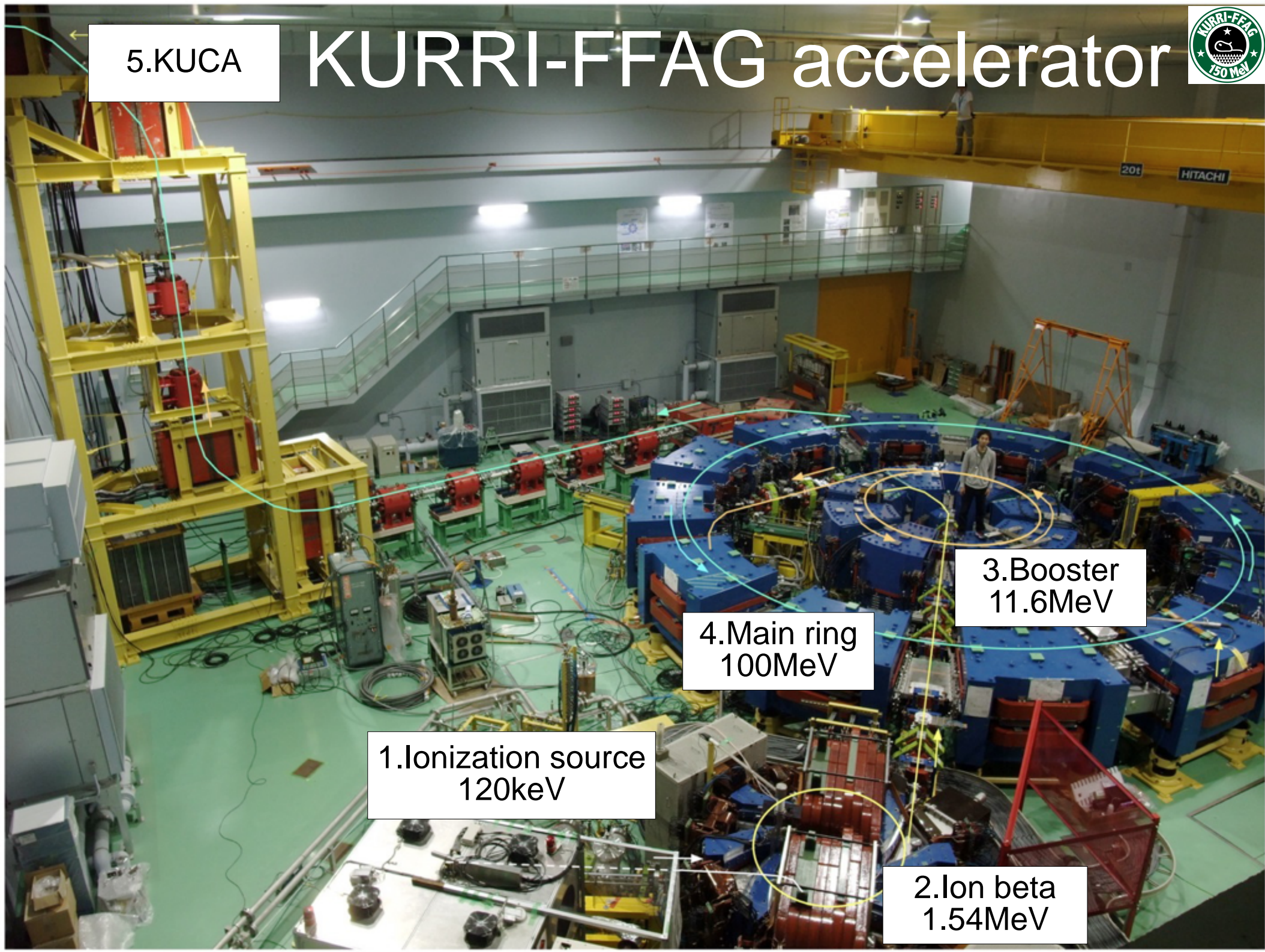
# KURRI-FFAG accelerator

1. Ionization source  
120keV

4. Main ring  
100MeV

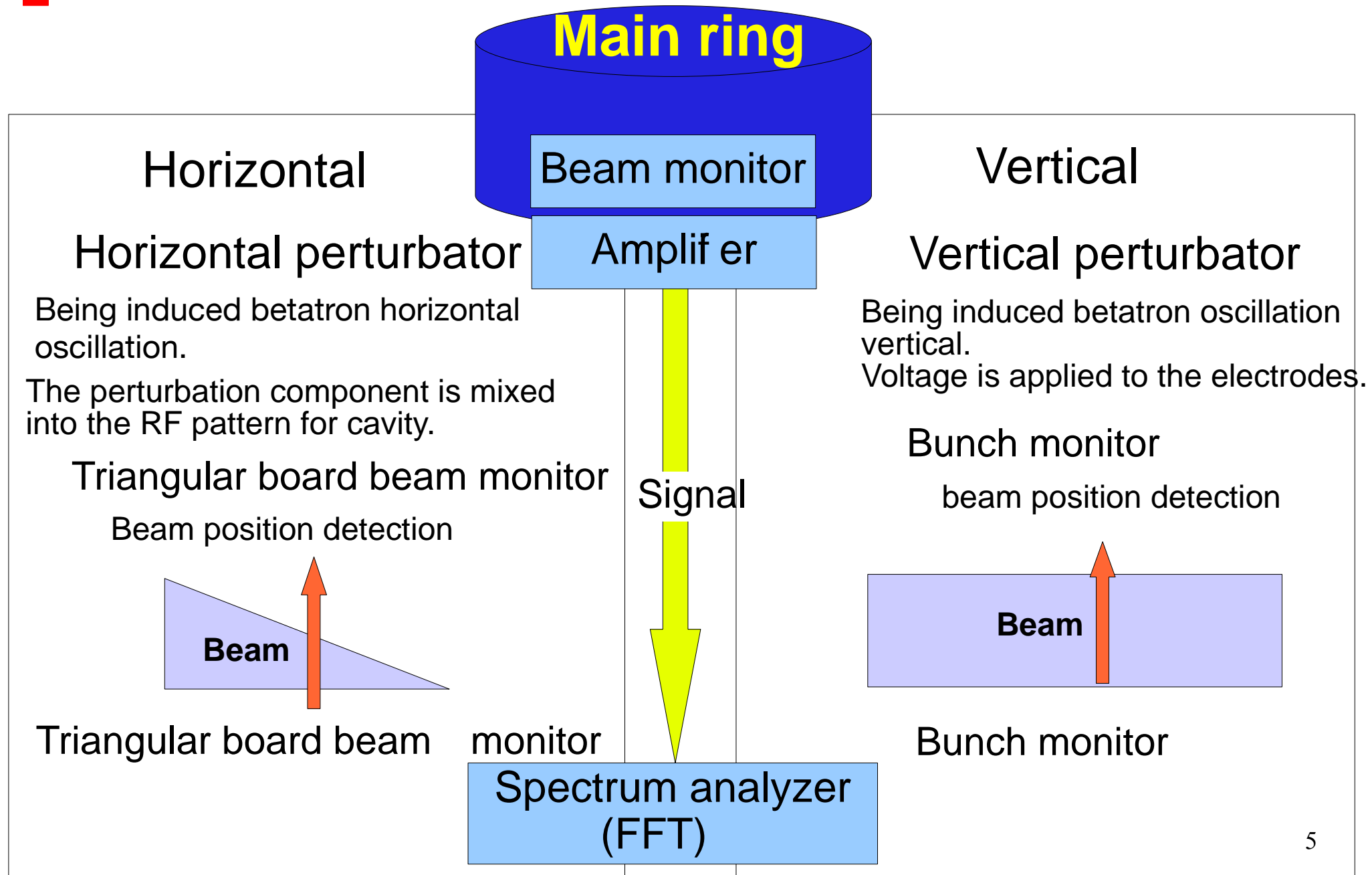
3. Booster  
11.6MeV

2. Ion beta  
1.54MeV





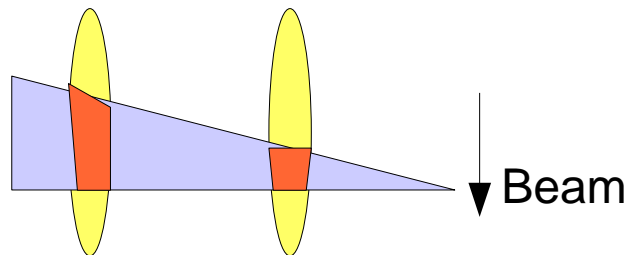
# Experimental set up



# Structure of the beam position monitor

The **electrostatic picking up** monitors are set up in the vacuum chamber.

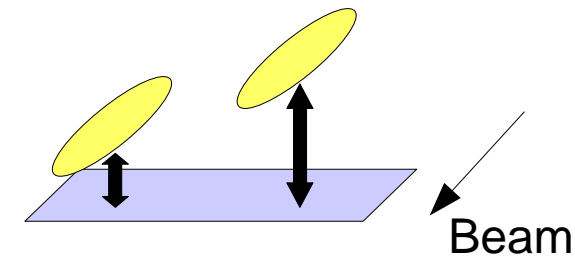
## Triangular board beam monitor



Induced voltage

Deviation of **horizontal beam position**  
= Difference of induced voltage

## Bunch monitor



Induced voltage

Deviation of **vertical beam position**  
= Difference of induced voltage

We can know the beam position according to the induced voltage

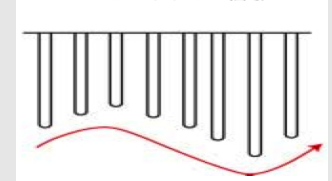
# Measurement of betatron oscillation

The betatron oscillation around the close orbit is observed as an **amplitude modulation** of the output signals.

$$V = A(1 + \Delta A) \cos(2\pi f_{rev} t)$$

$$\Delta A = A_{side} \cos(2\pi f_{side} t + \theta)$$

$$V = A \cos(2\pi f_{rev} t) + \frac{A_{side}}{2} \cos\{(2\pi f_{rev} + 2\pi f_{side})t + \theta\} + \frac{A_{side}}{2} \cos\{(2\pi f_{rev} - 2\pi f_{side})t - \theta\}$$

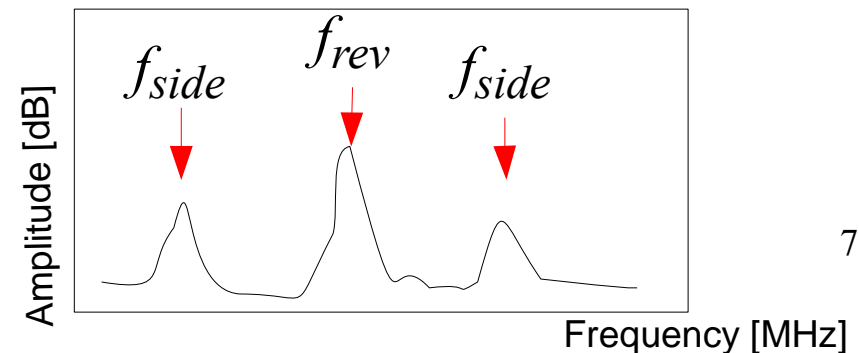


Fourier transform

Revolution frequency ( $f_{rev}$ ) and sideband ( $f_{side}$ ) is observed.

Fraction **C** of betatron tune is obtained from two peaks .

$$C = \frac{|f_{side} - m f_{rev}|}{f_{rev}}$$



# Result of a measurement



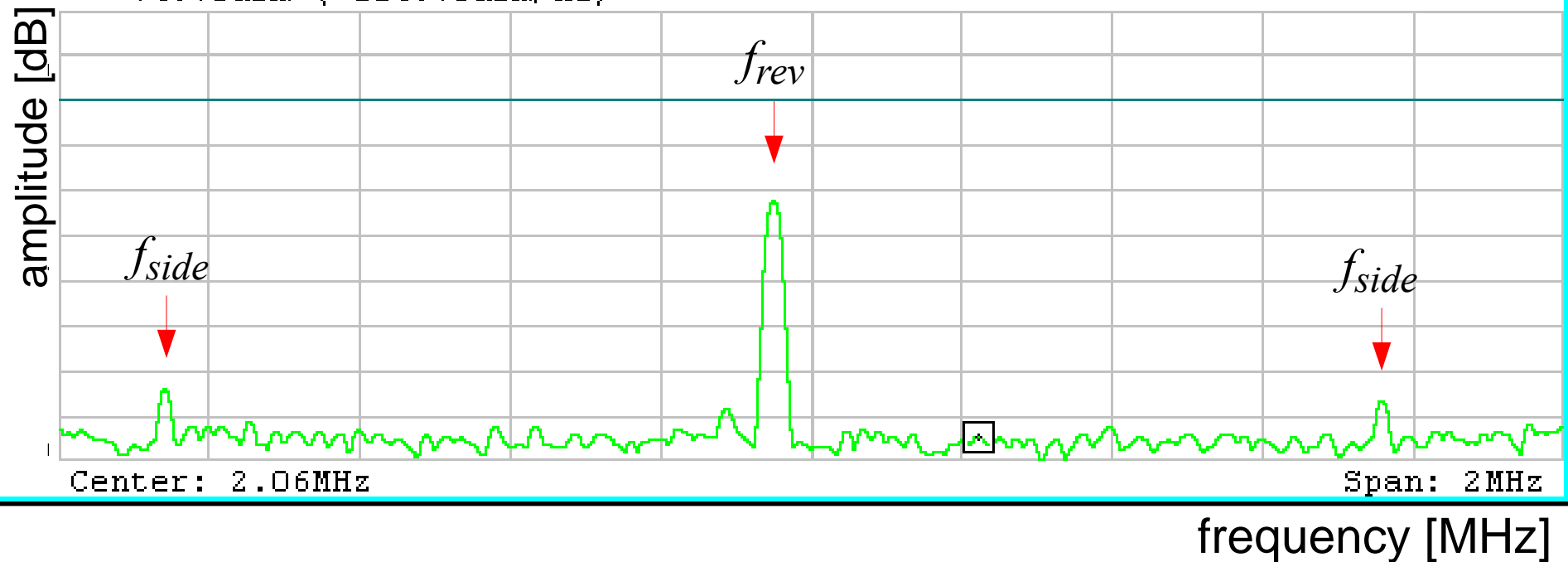
## Output of spectrum analyzer

**Frame Time:** 1.28ms

**RBW:** 10kHz

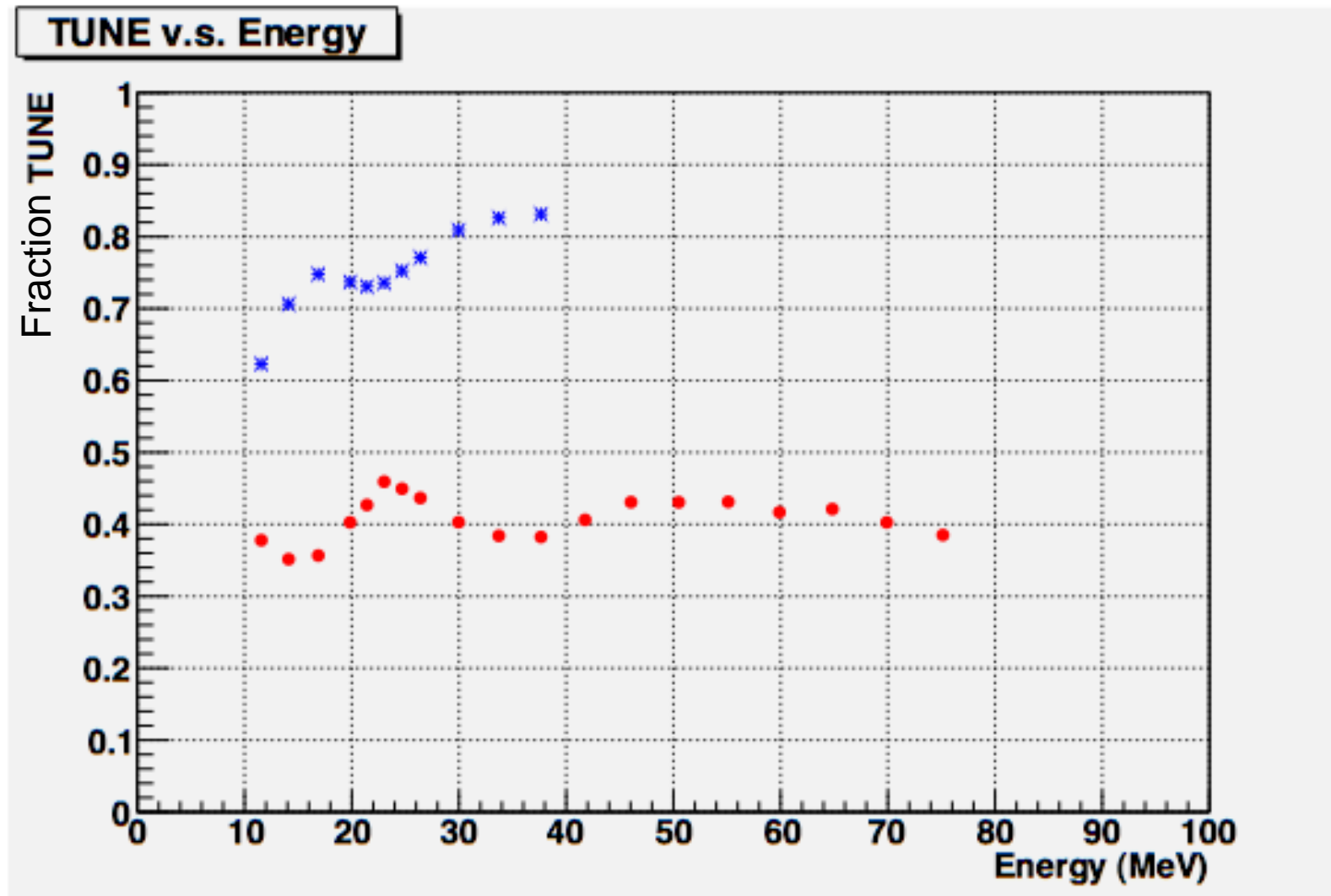
Marker: 2.281 093 75MHz

-74.75dBm (-114.75dBm/Hz)

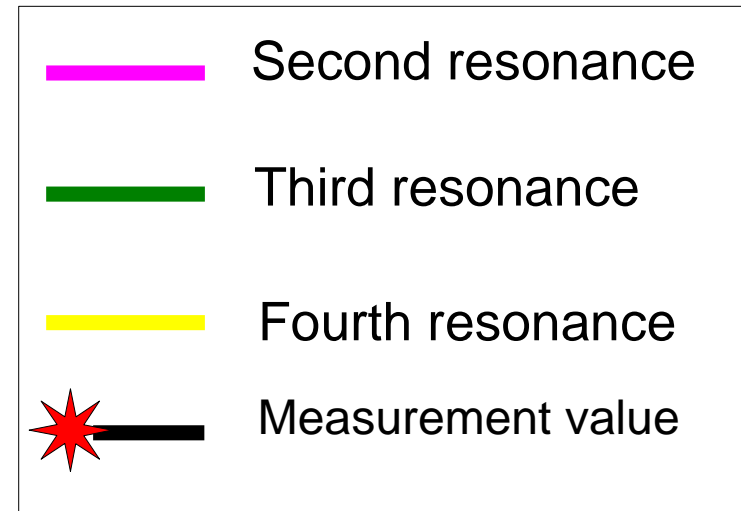
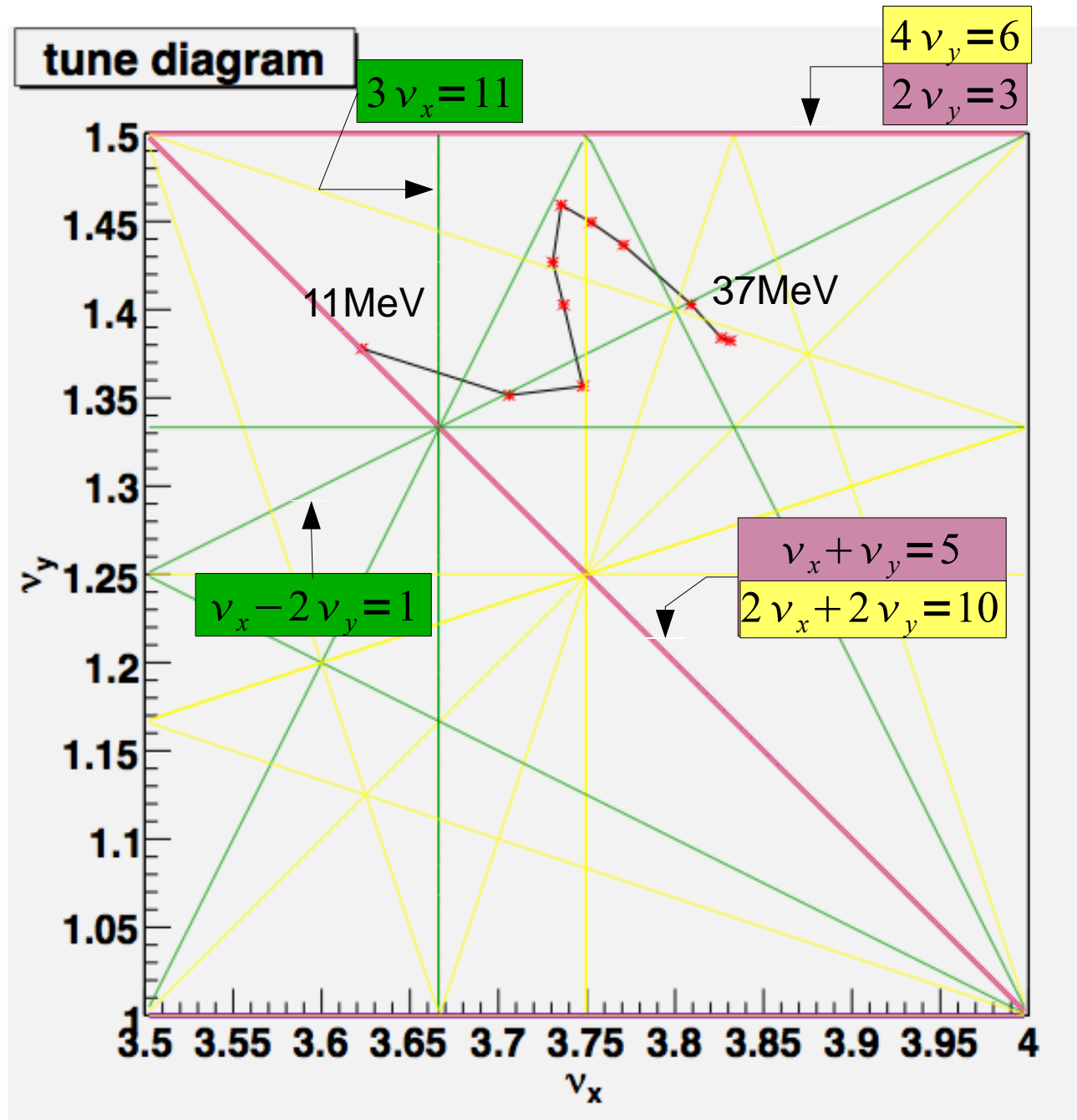




# Tune v.s. Energy



# Tune diagram



# Summary



Tune was able to be measured  
at main ring

The measuring method of  
betatron tunes was able to  
be confirmed

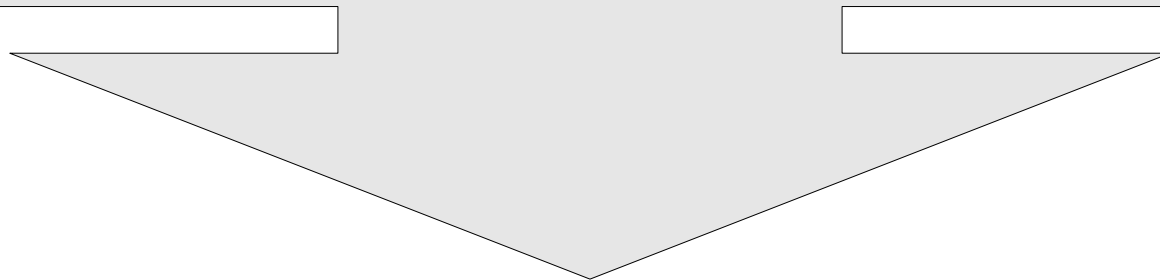
# Future



Further measurement of vertical and horizontal tunes

Optimization of betatron tunes

Modification of magnetic pole tip  
Change the F/D ratio

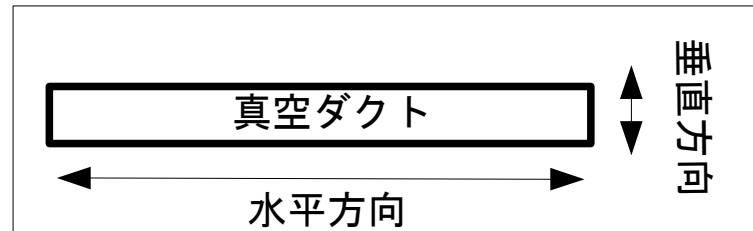


Suppress the beam loss through the accelerating process

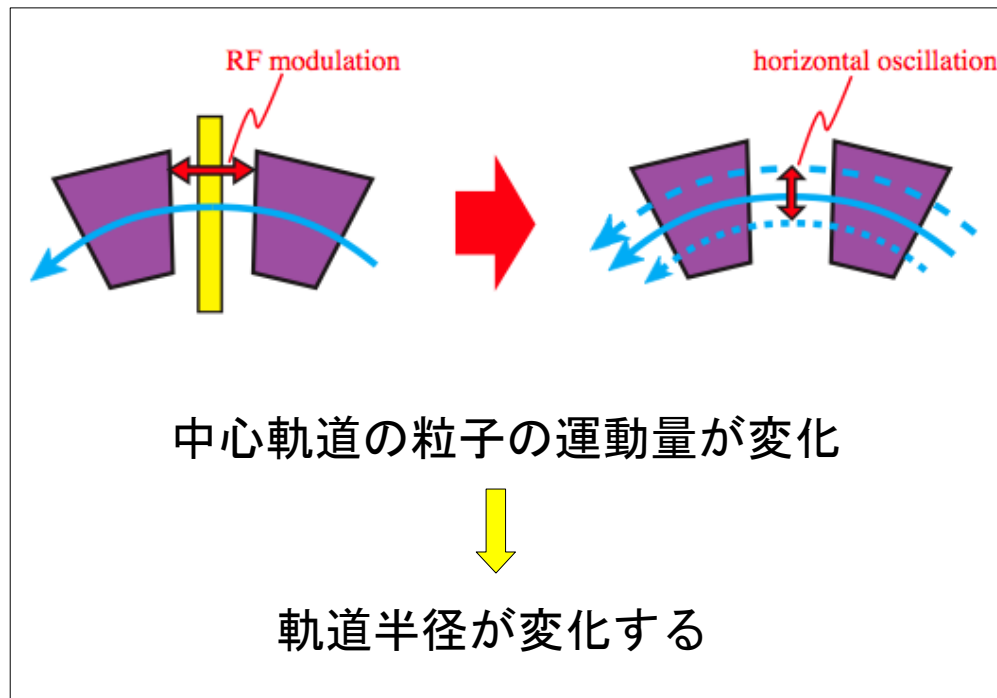
# 付録

# ベータ トロン振動の誘起方法

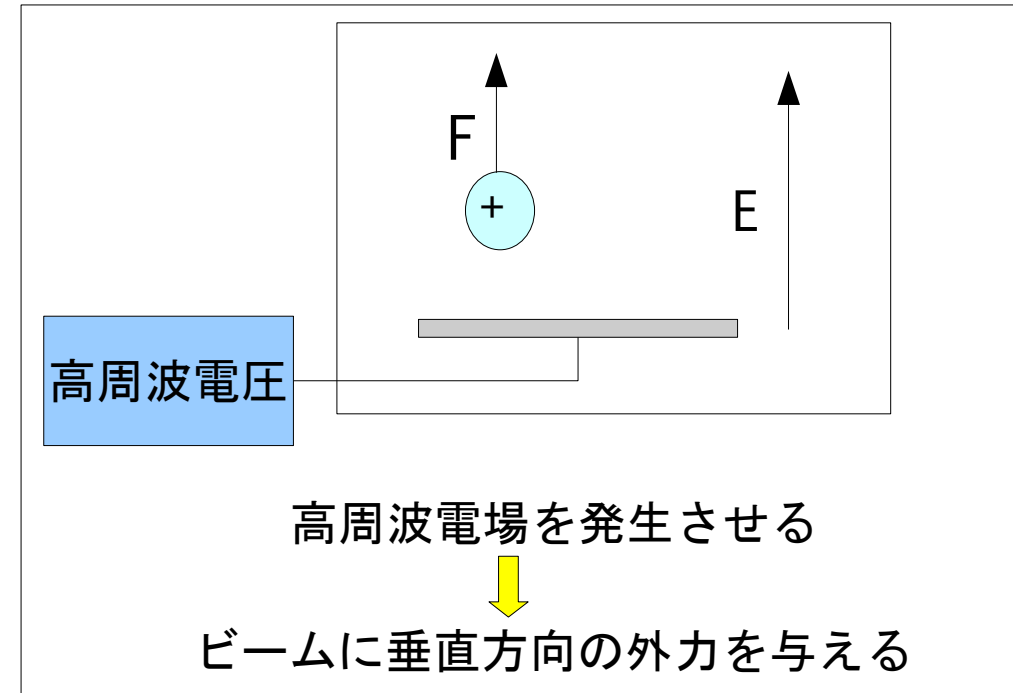
真空ダクトの構造上ベータ トロン振動の誘起方法は水平方向と垂直方向で異なる



加速空洞使用（水平方向）



平板電極使用（垂直方向）



結果ベータ トロン振動を誘起できる

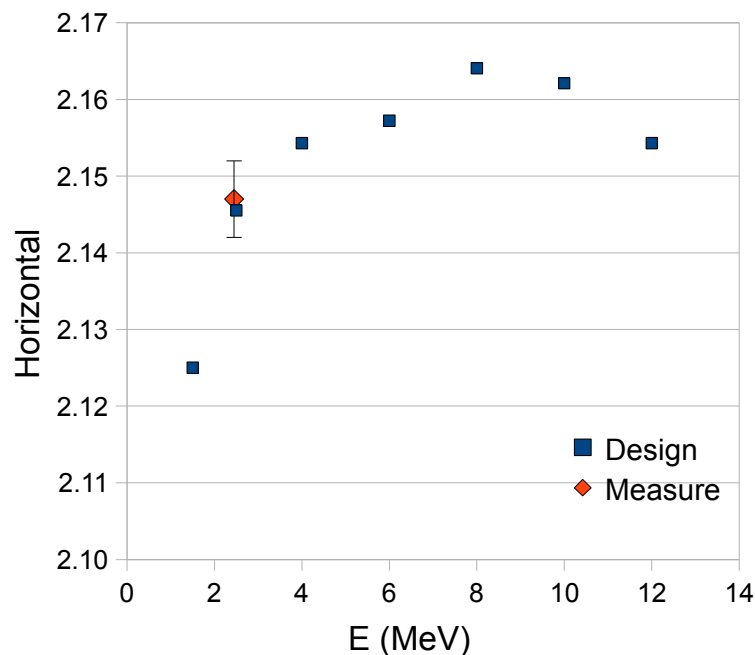


# 設計値との比較

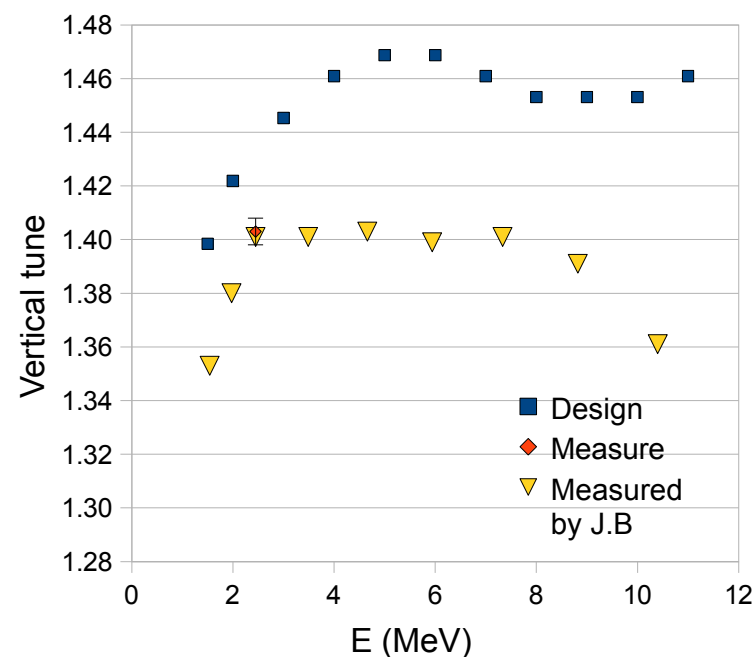
加速時間・エネルギー・周回周波数の表

accelerate time (s)	0	0.5	1	2	3	4	5	6	7	8
E (MeV)	1.5400	1.9740	2.4480	3.4887	4.6581	5.9416	7.3308	8.8200	10.4023	12.0742
F (Hz)	1.9594	2.1438	2.3125	2.6250	2.9063	3.1656				

Energy VS Horizontal



Energy VS Vertical



Design値 :TOSCAでトラッキングシュミレーションしたもの  
Measured by J.B: 過去に測定した結果  
([http://hadron.kek.jp/FFAG/FFAG08J\\_HP/index.htm](http://hadron.kek.jp/FFAG/FFAG08J_HP/index.htm))

# 加速器駆動型未臨界原子炉 (ADSR)

## KUCA-FFAG結合実験のイメージ図



2009年3月4日  
**世界初の**  
加速器駆動型未臨界原子炉実験開始

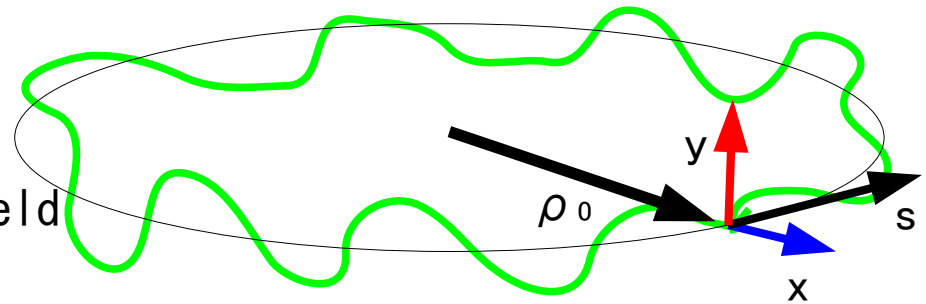


# Behavior of electron in accelerator

## ◆ Motion equation in focusing magnetic field

$$\left\{ \begin{array}{l} \frac{d^2 x}{ds^2} + \frac{(1-k(s))}{\rho^2} \cdot x = 0 \\ \frac{d^2 y}{ds^2} + \frac{k(s)}{\rho^2} \cdot y = 0 \end{array} \right. \quad \begin{array}{l} \text{Horizontal} \\ \text{Vertical} \end{array}$$

$\rho_0$  : Curvature radius  
 $k$  : Inclination of magnetic field  
 $k(s) \equiv -\frac{\rho(s)}{B_0} \frac{\partial B_y}{\partial \rho_0}$



## Betatron vibration

$$x(s) = \sqrt{\varepsilon \beta(s)} \cos(\psi(s) + \delta)$$

The vibration frequency of the small oscillation near a round is called

$$2\pi\nu = \psi(c) = \oint \frac{ds}{\beta}$$

$c$  : Ring surroundings length

$\nu$  : Betatron tune

$\nu$  : An odd value is taken usually

# Resonance and tune diagram

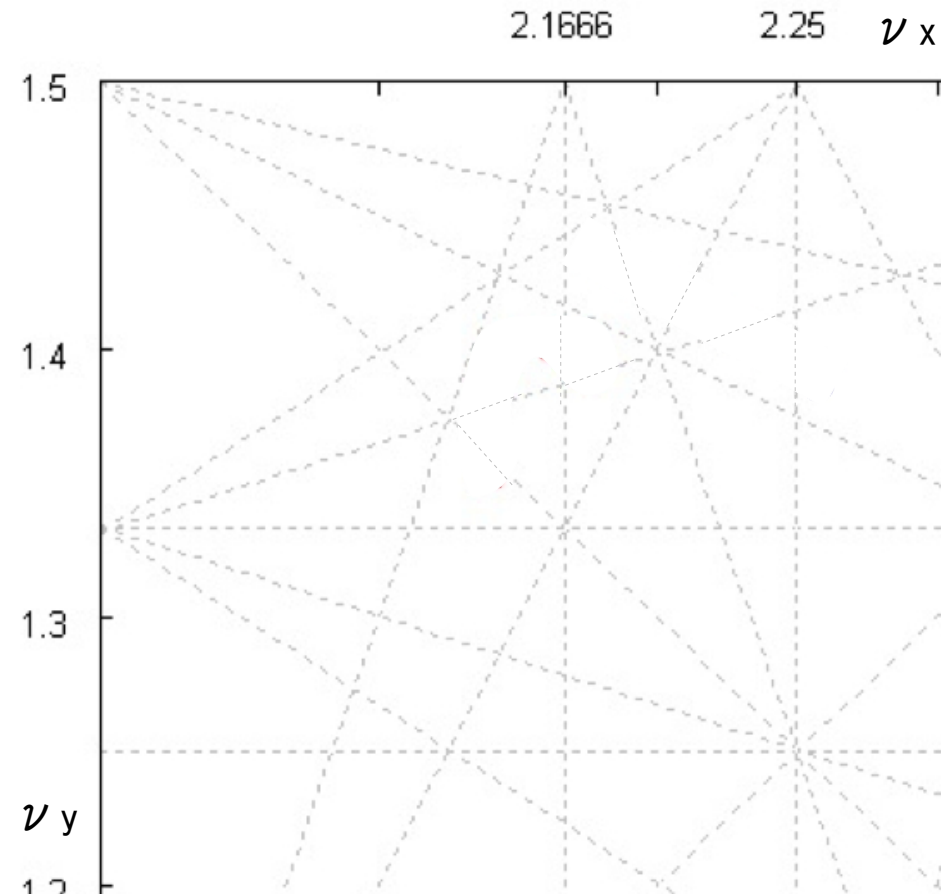
- Periodic power is received by the magnetic field error etc
- It is impossible to adjust the magnetic field error to zero

Resonance condition  $m \nu_x + n \nu_y \simeq l$   $m, n, l$  : Integer that is positive or negative

## ◆Tune diagram

$\nu_x$ と $\nu_y$ を座標軸とする図の上に  
共鳴の線 (resonance line) を書いたもの

共鳴の線を避ける  
運転上好ましいチューンを選ぶ



# Integration time

Span [MHz]	Integration time [ s]
10	80
5	160
2	320
1	640