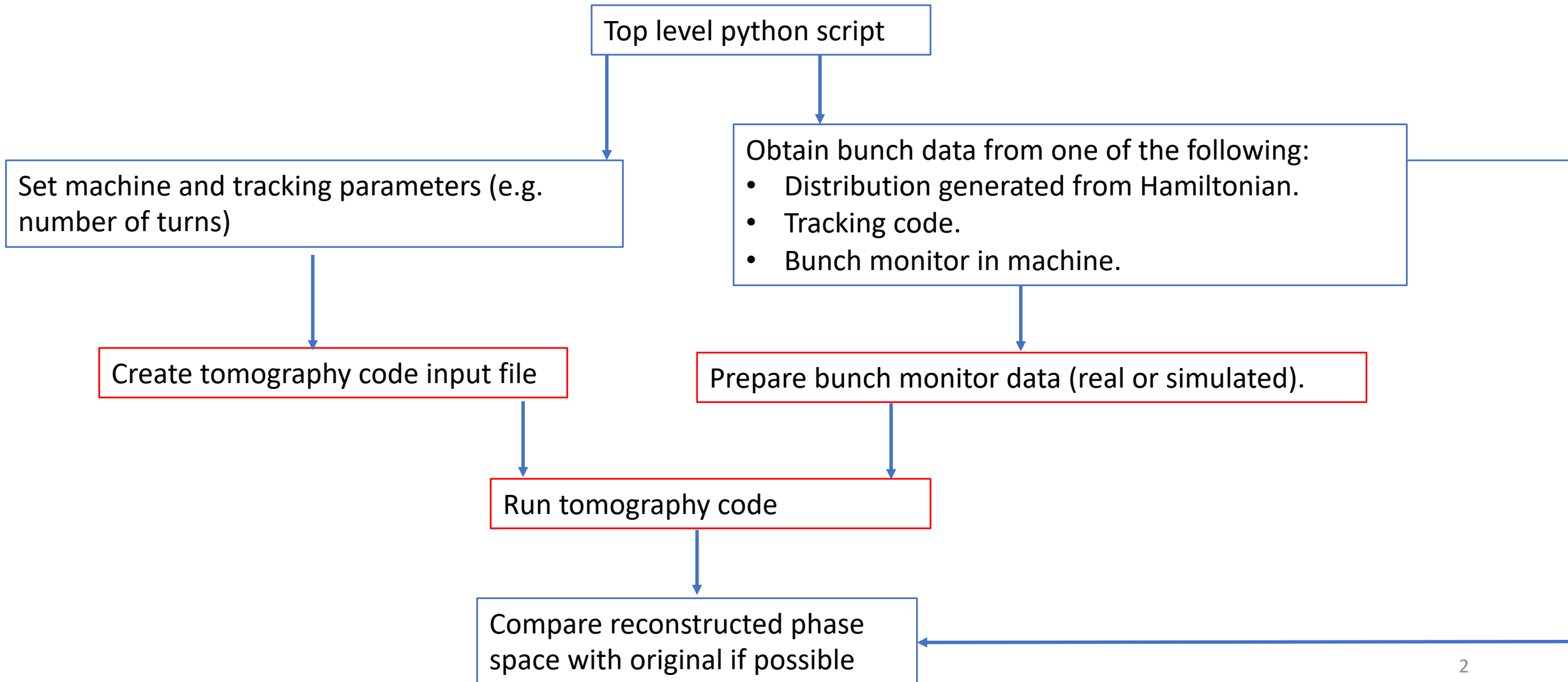


Longitudinal tomography

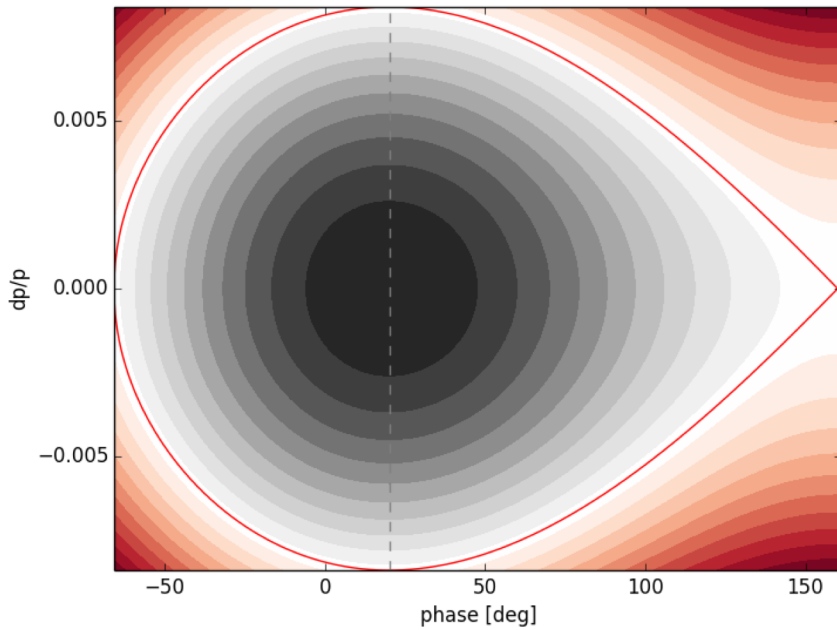
David Kelliher, 24/8/18

Tomography analysis flowchart

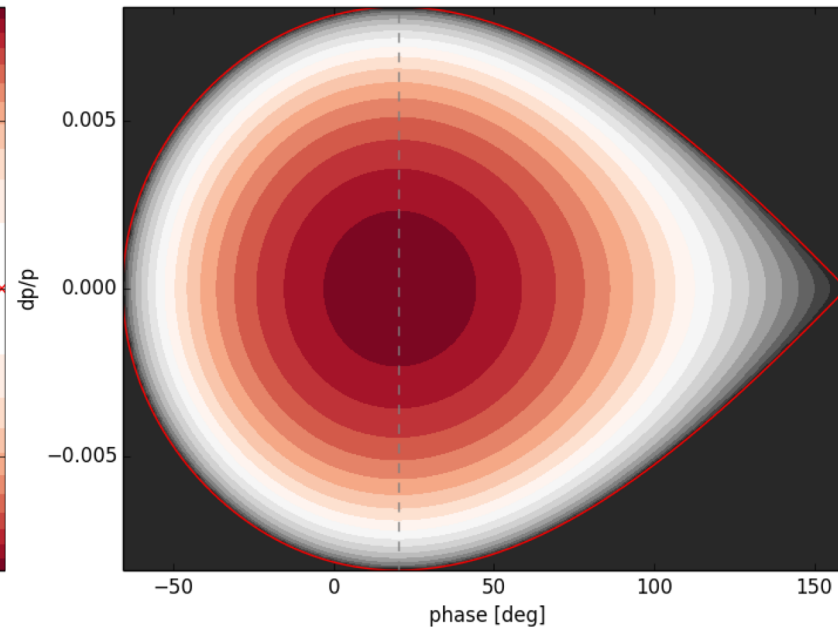


Generating a stationary distribution

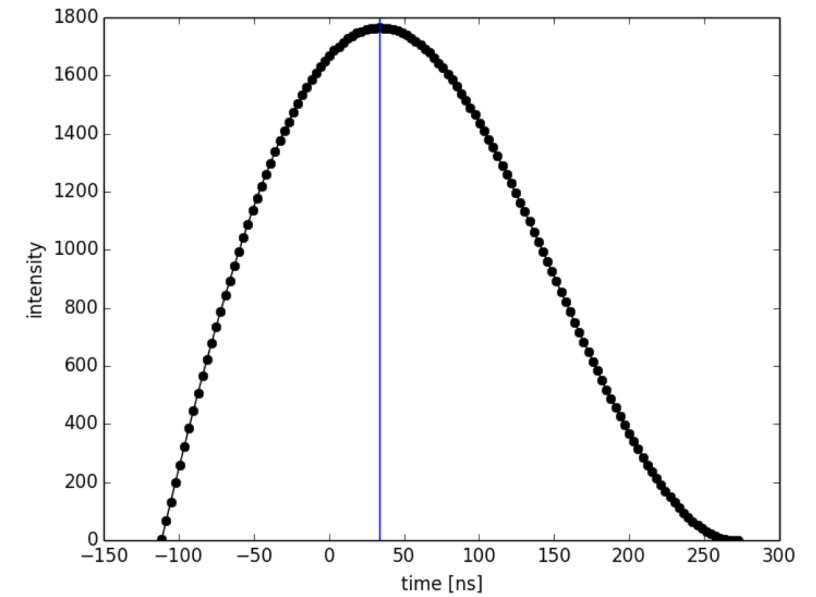
- Evaluate the longitudinal Hamiltonian on a grid producing $H(\delta, \Phi)$.
- Generate distribution as a function of H (excluding $H > H_{\text{sep}}$).
- Time projection used as input in tomography code.



Hamiltonian

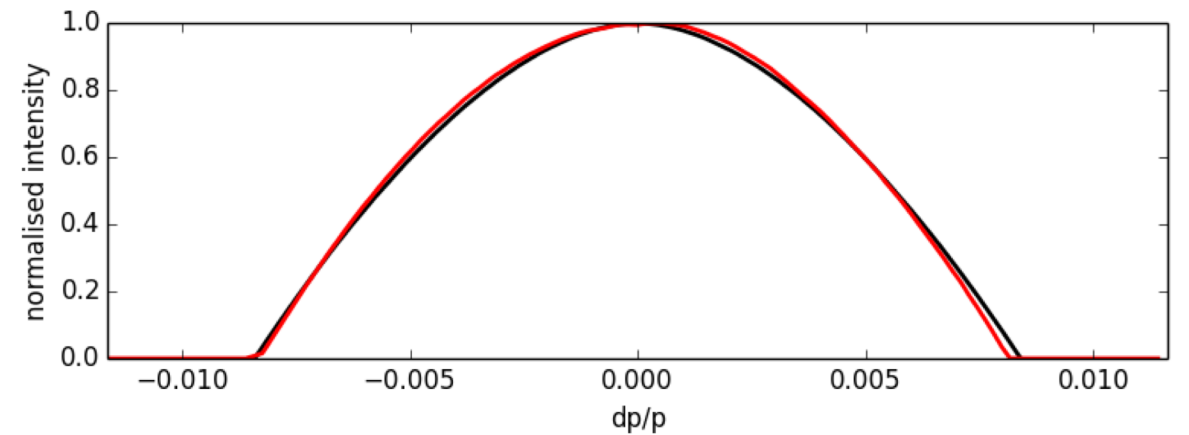
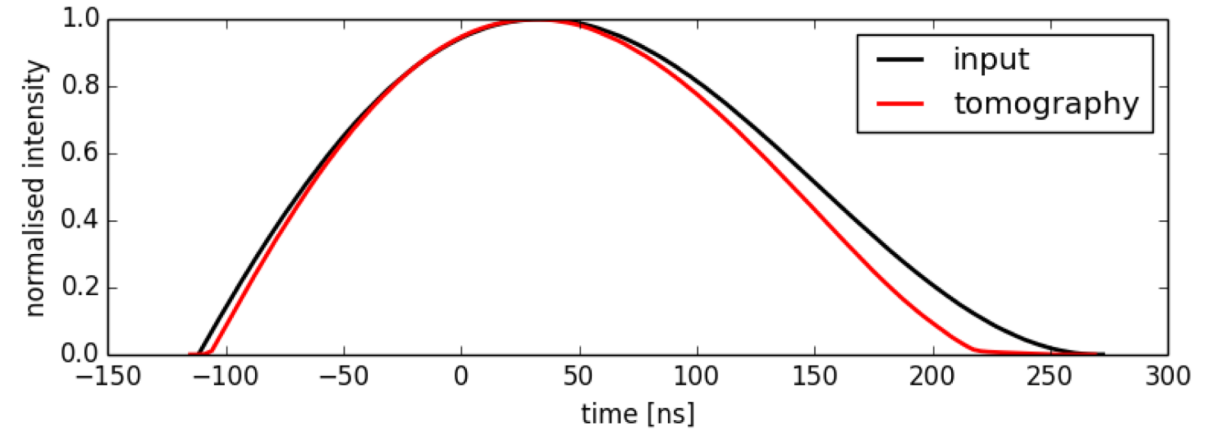
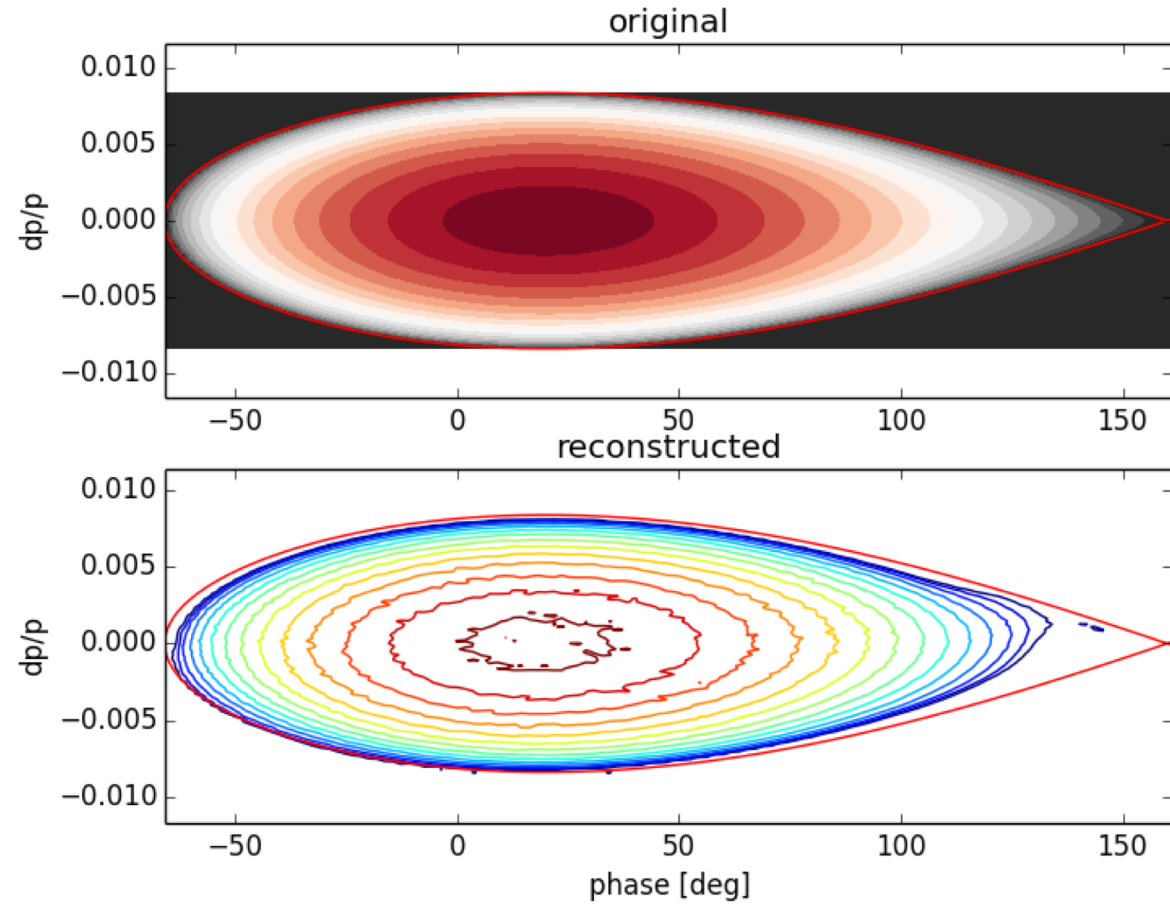


Distribution



Projection

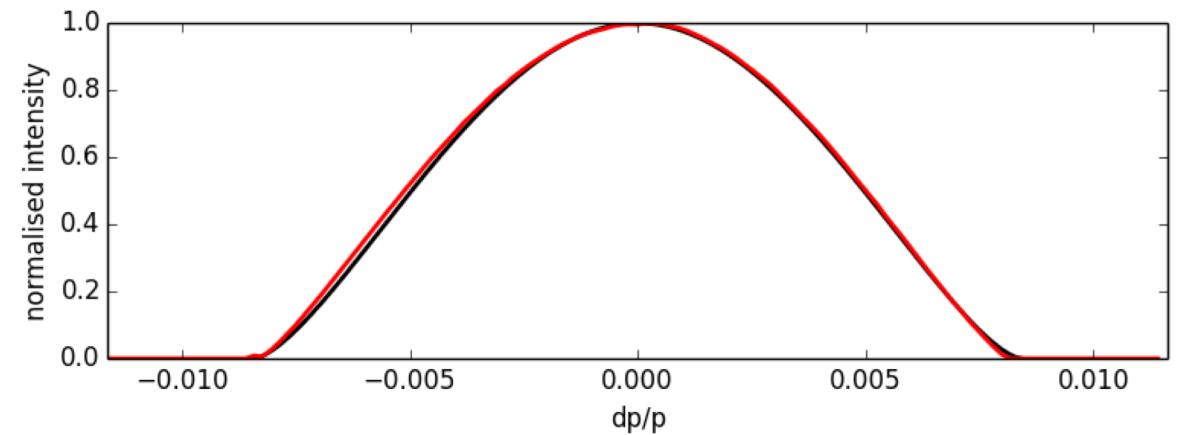
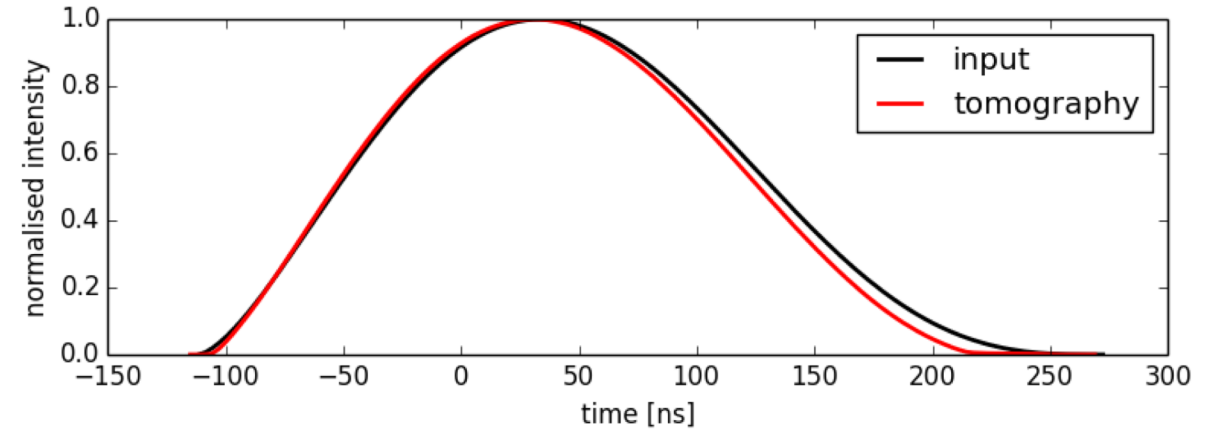
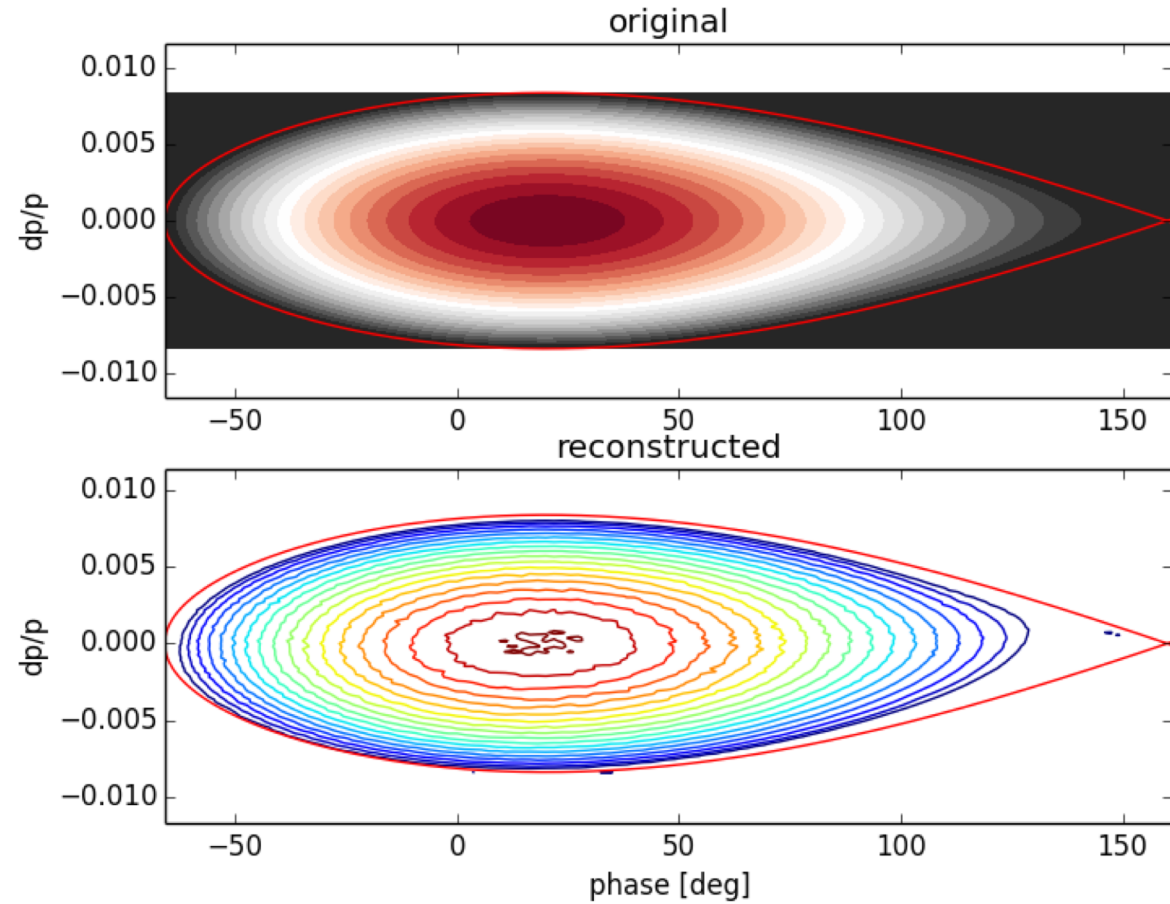
Stationary distribution (1)



Qs: 0.005 ($T_s=200$), ϕ_s : 20 deg.
Number of bins in projection: 128
Number of "turns": 100 ($=0.5 \cdot T_s$)

$$f(\phi, \delta) = \sqrt{H_{sep} - H(\delta, \phi)}$$

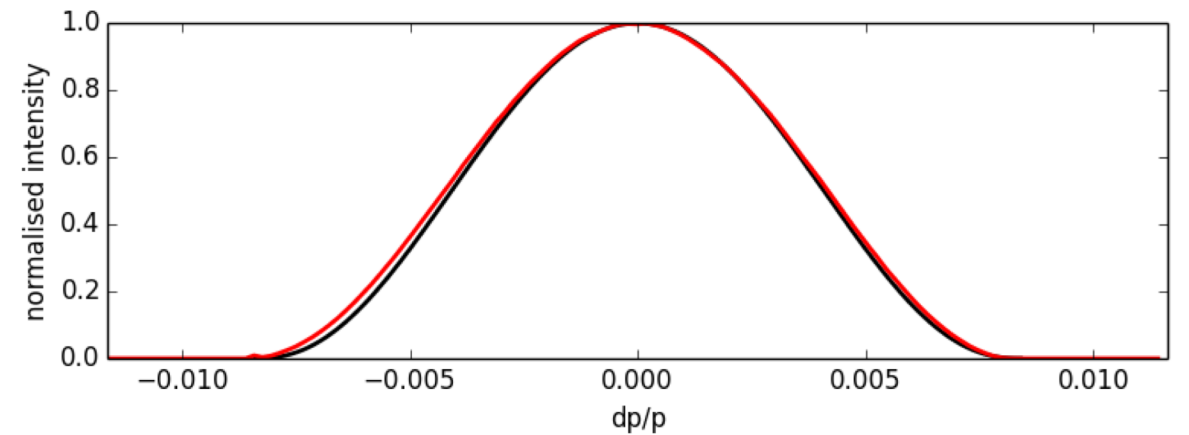
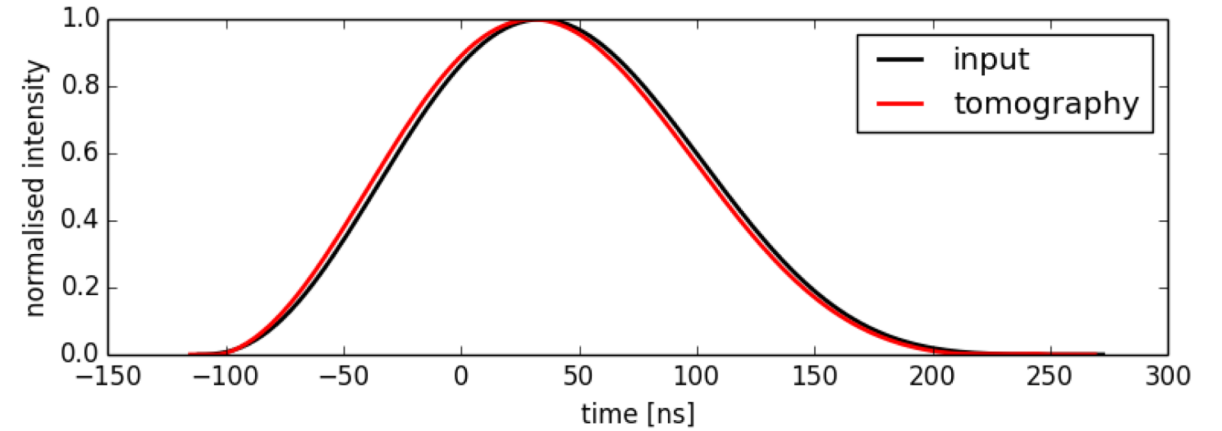
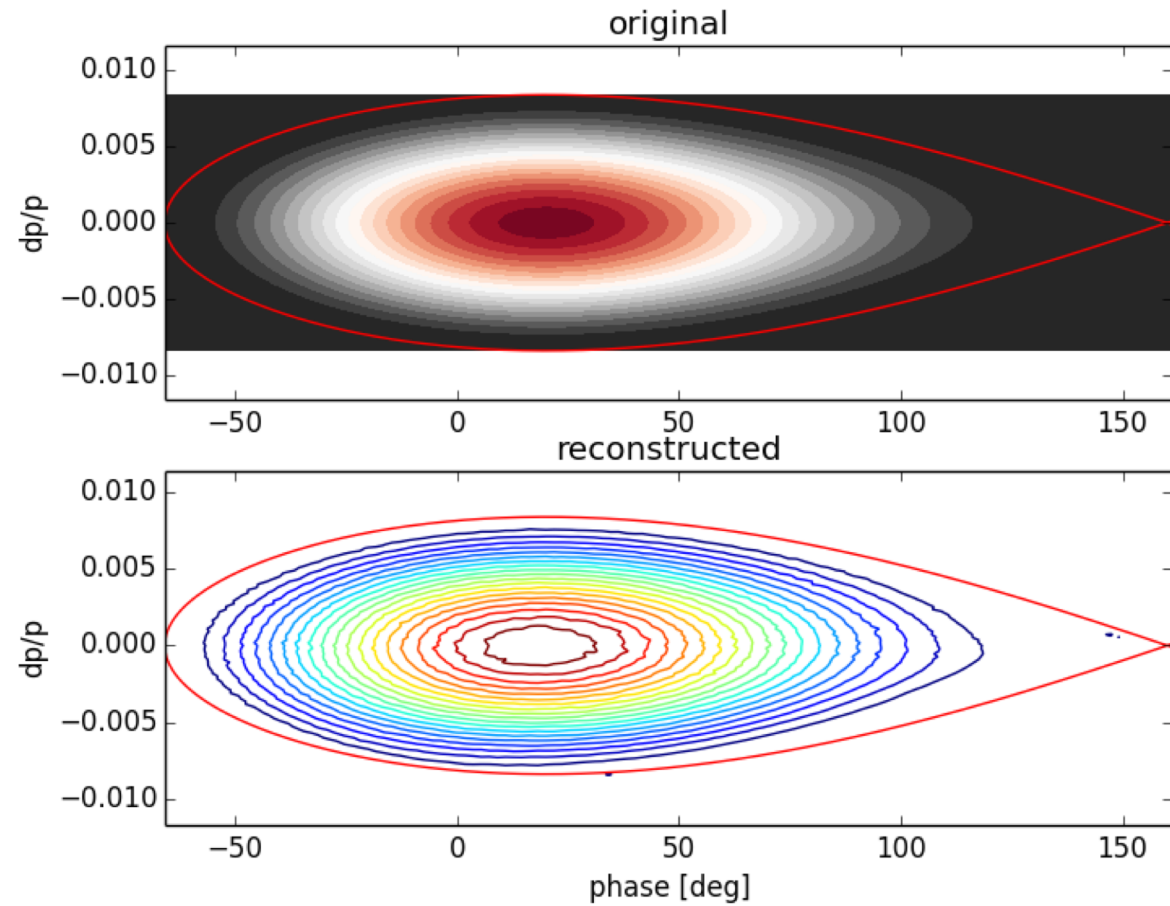
Stationary distribution (2)



Qs: 0.005 ($T_s=200$), ϕ_s : 20 deg.
Number of bins in projection: 128
Number of "turns": 100 ($=0.5 \cdot T_s$)

$$f(\phi, \delta) = H_{sep} - H(\delta, \phi)$$

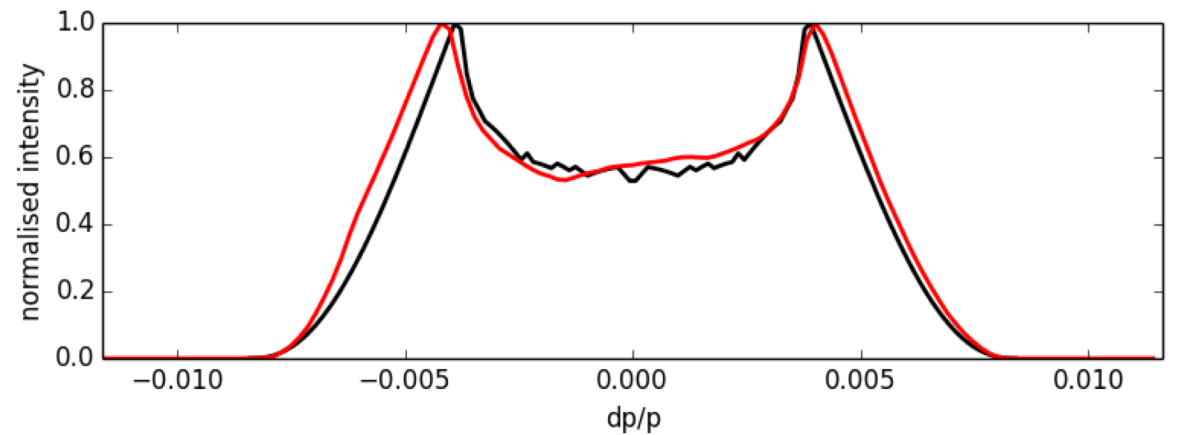
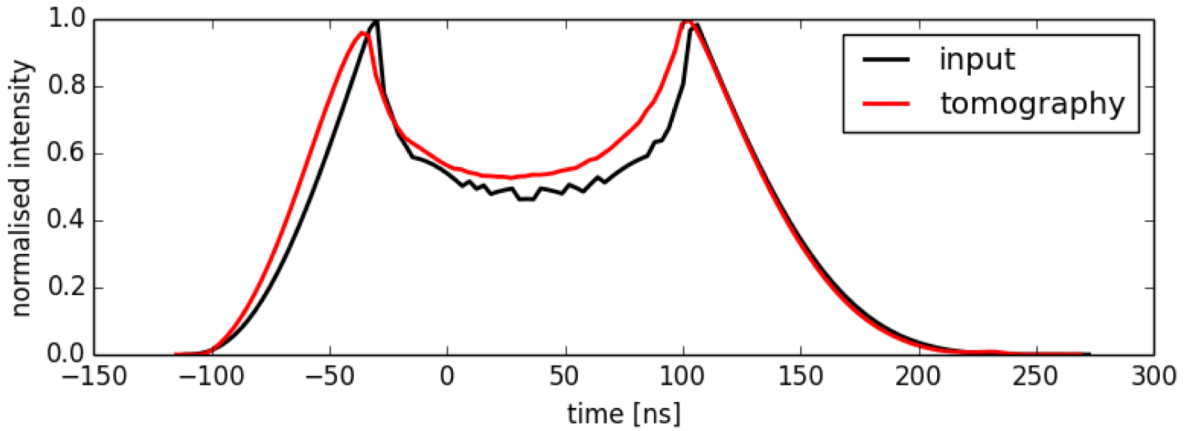
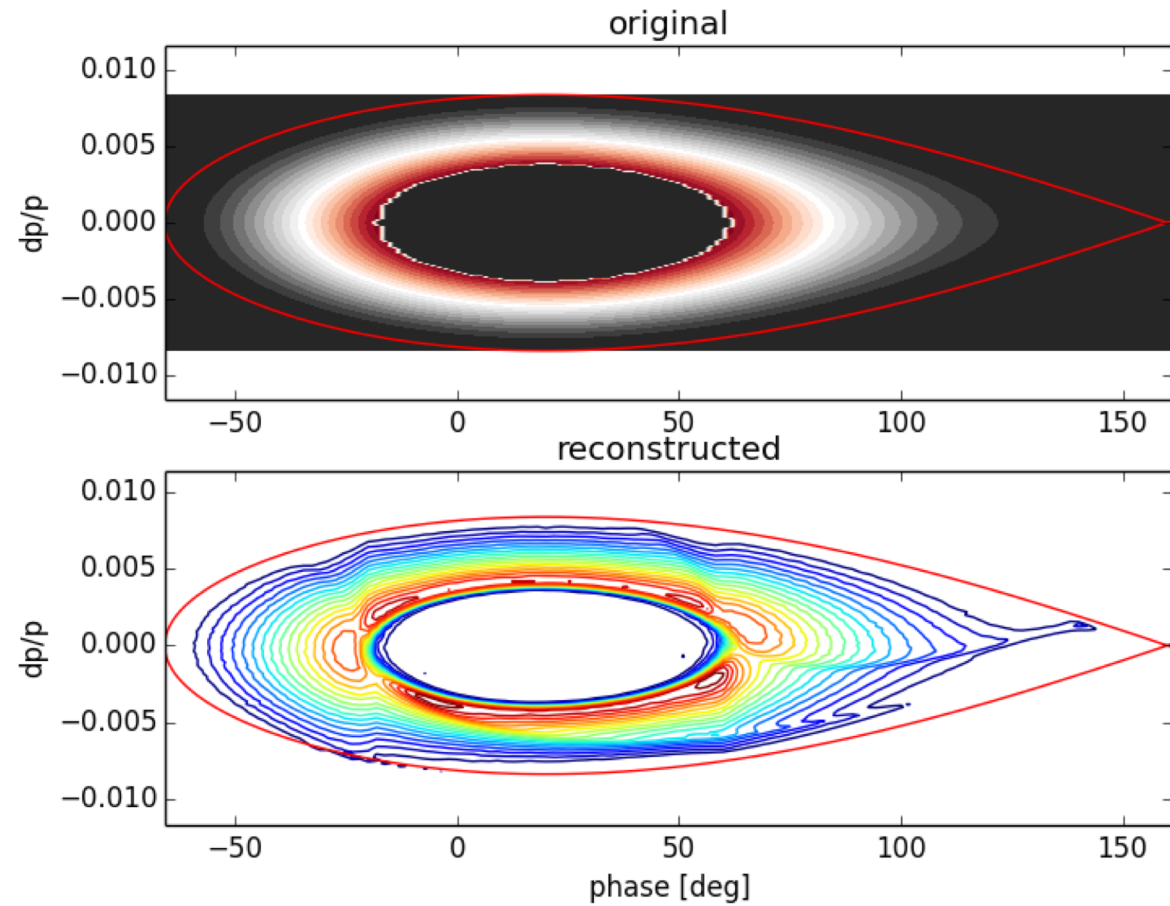
Stationary distribution (3)



Qs: 0.005 ($T_s=200$), ϕ_s : 20 deg.
Number of bins in projection: 128
Number of "turns": 100 ($=0.5 \cdot T_s$)

$$f(\phi, \delta) = (H_{sep} - H(\delta, \phi))^2$$

Stationary distribution with hole

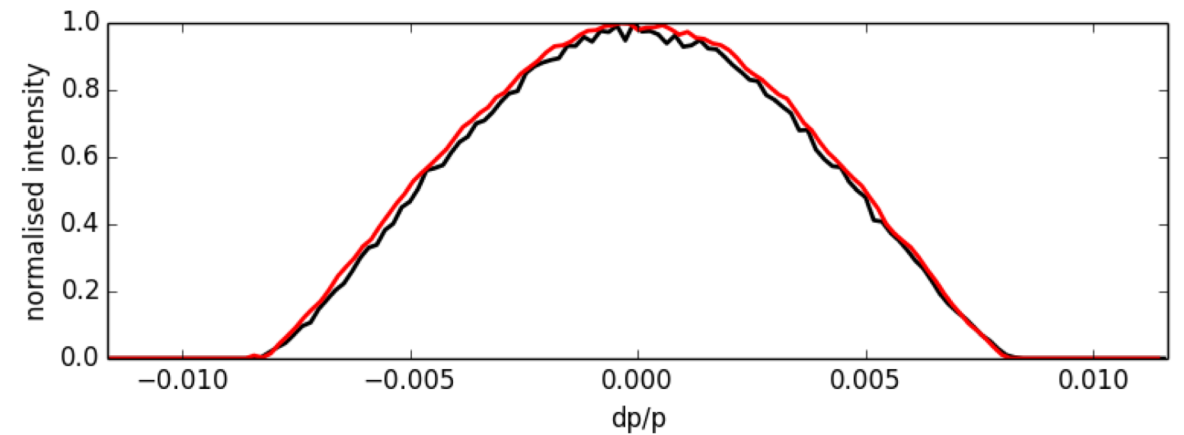
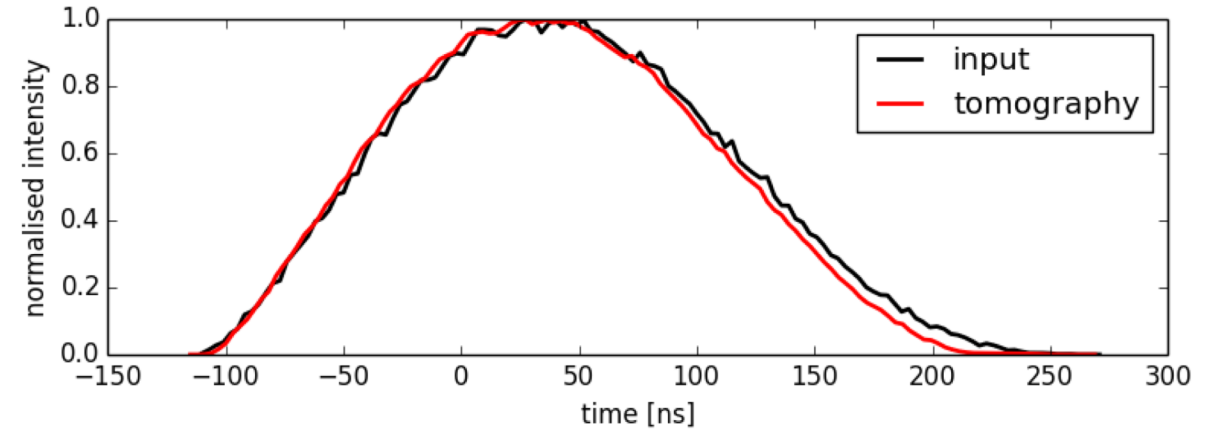
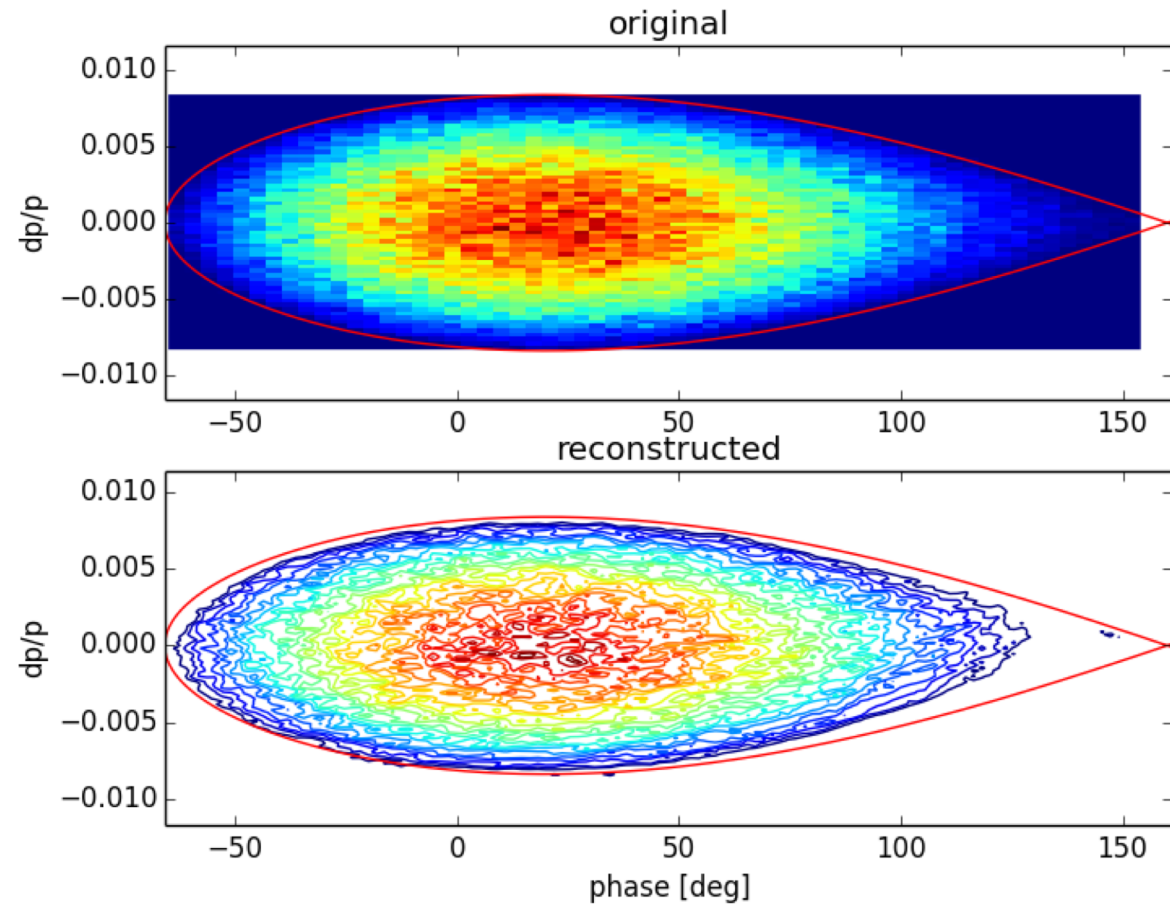


Qs: 0.005 ($T_s=200$), ϕ_s : 20 deg.
 Number of bins in projection: 128
 Number of "turns": 100 ($=0.5 \cdot T_s$)

$$f(\phi, \delta) = (H_{sep} - H(\delta, \phi))^2, H > H_{cut}$$

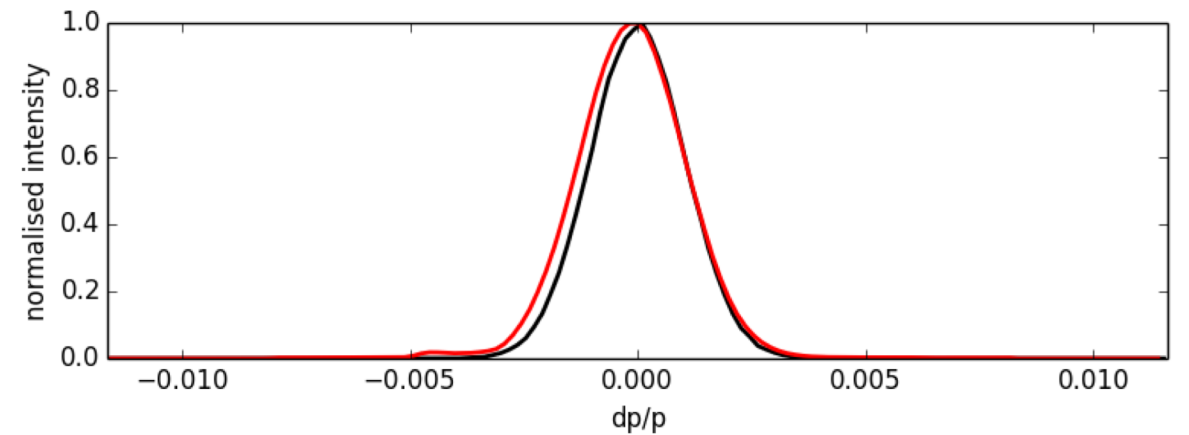
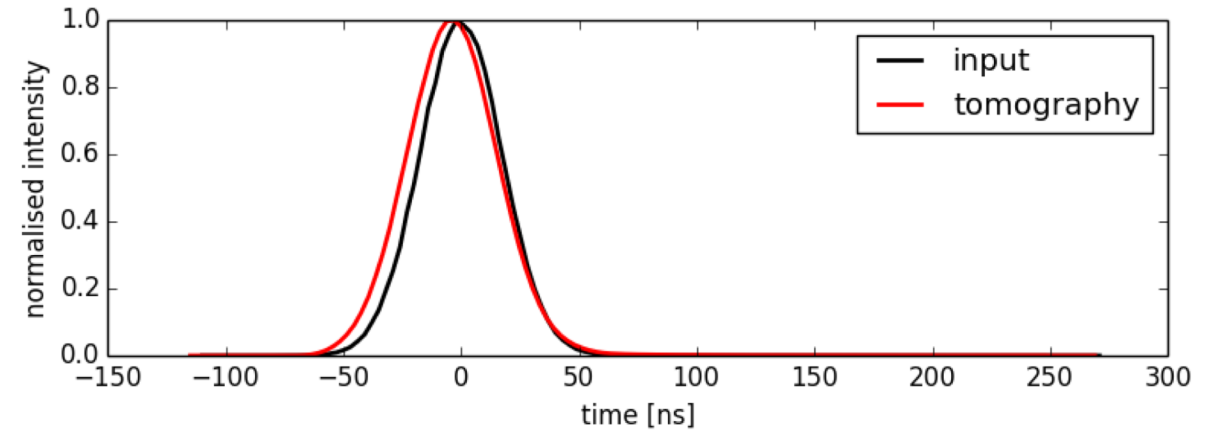
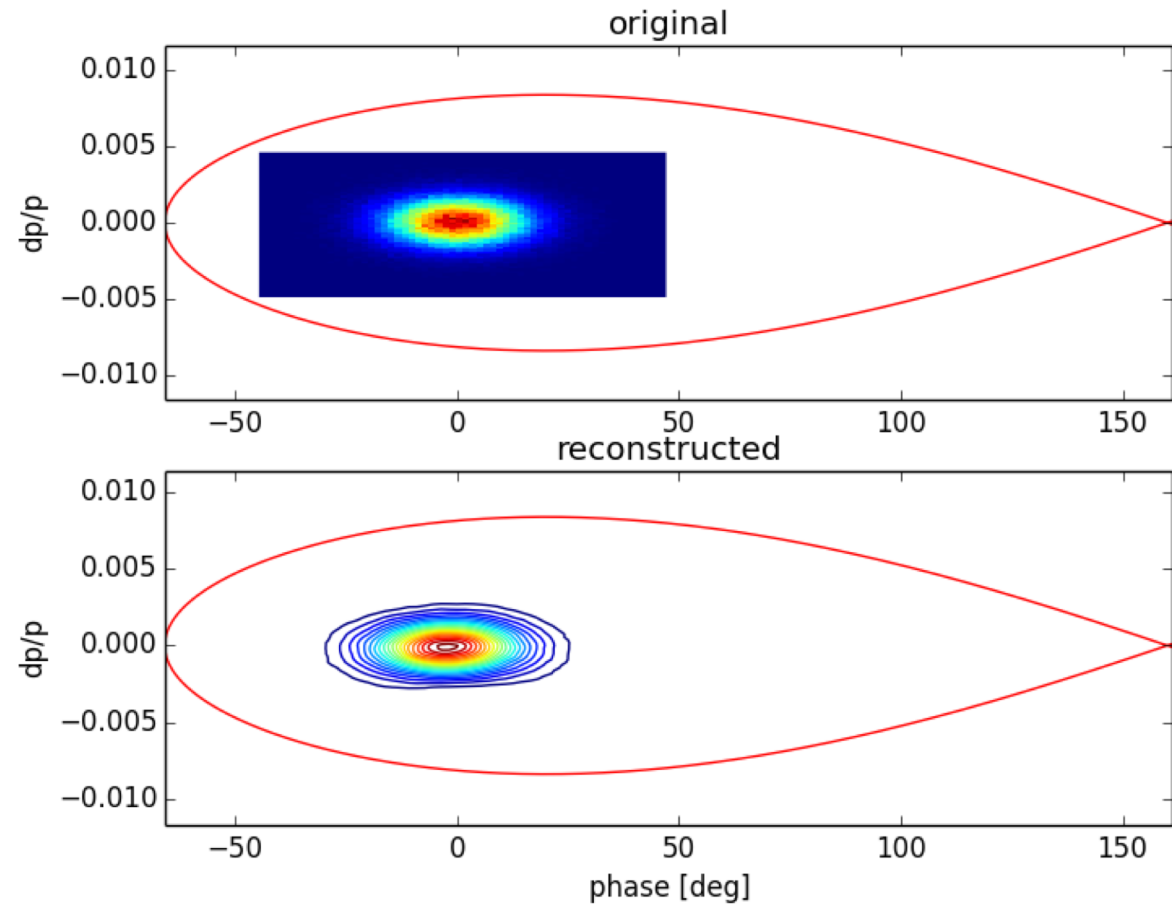
$$f(\phi, \delta) = 0, H < H_{cut}$$

PyHEADTAIL tracking – stationary thermal distribution



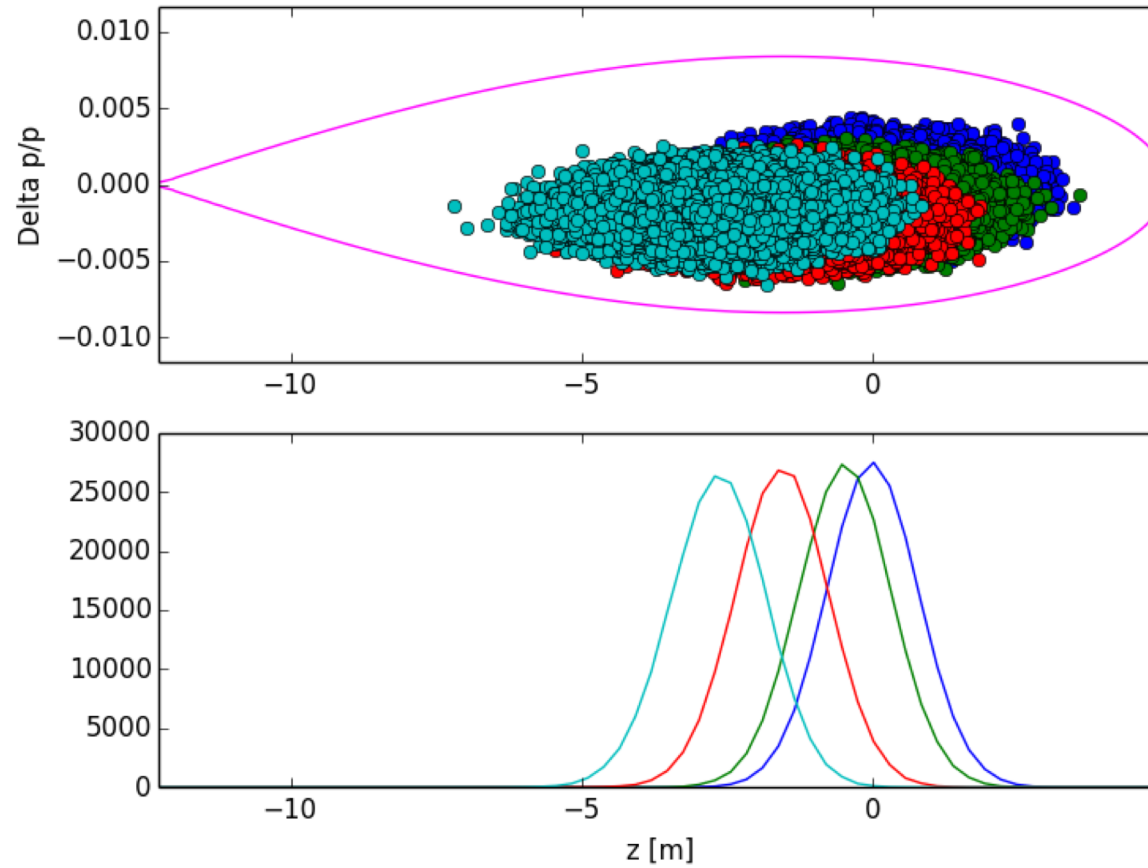
Q_s : 0.005 ($T_s=200$), ϕ_s : 20 deg.
Number of bins in projection: 128
Number of "turns": 100 ($=0.5 \cdot T_s$)

PyHEADTAIL tracking – small Gaussian bunch



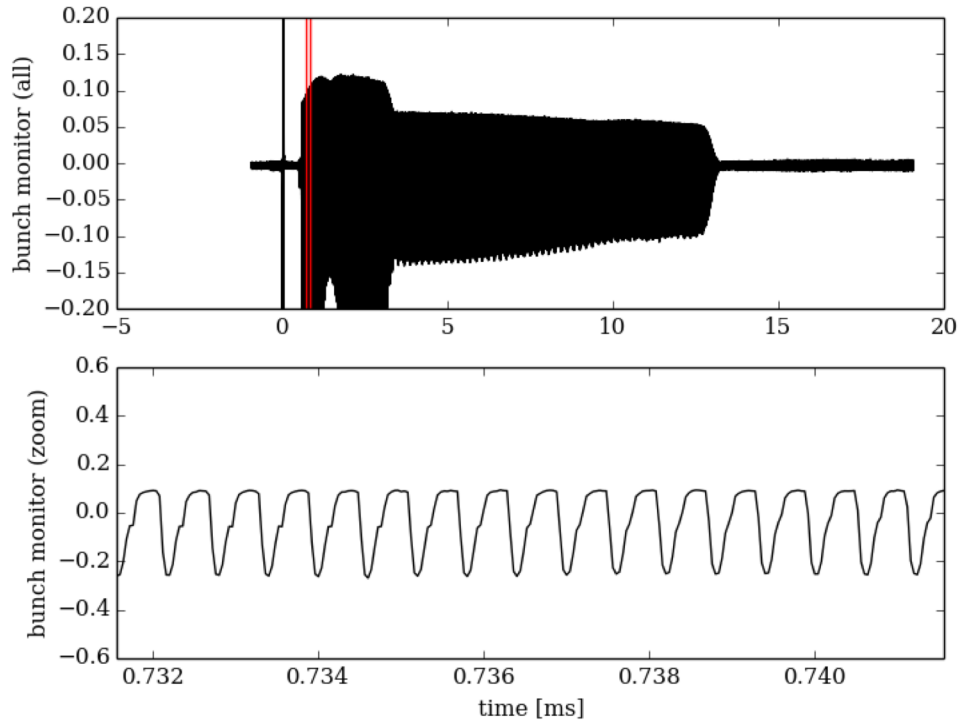
Note: Tomography code expects the bunch profile to span the bucket.

PyHEADTAIL tracking

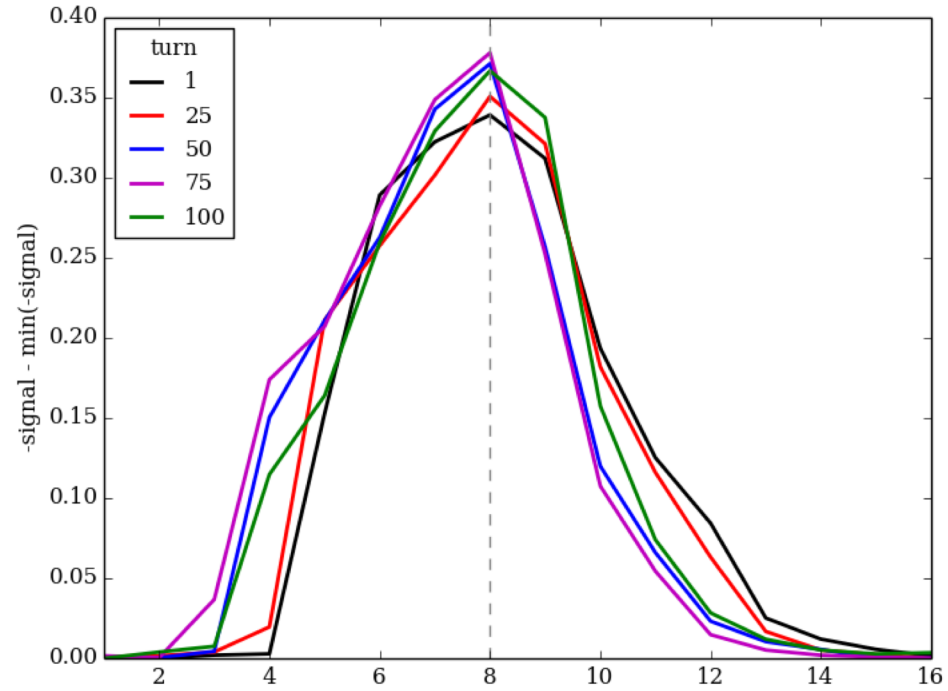


Show tracking result every 25 turns.
To do: compare with tomography results.

Bunch monitor data

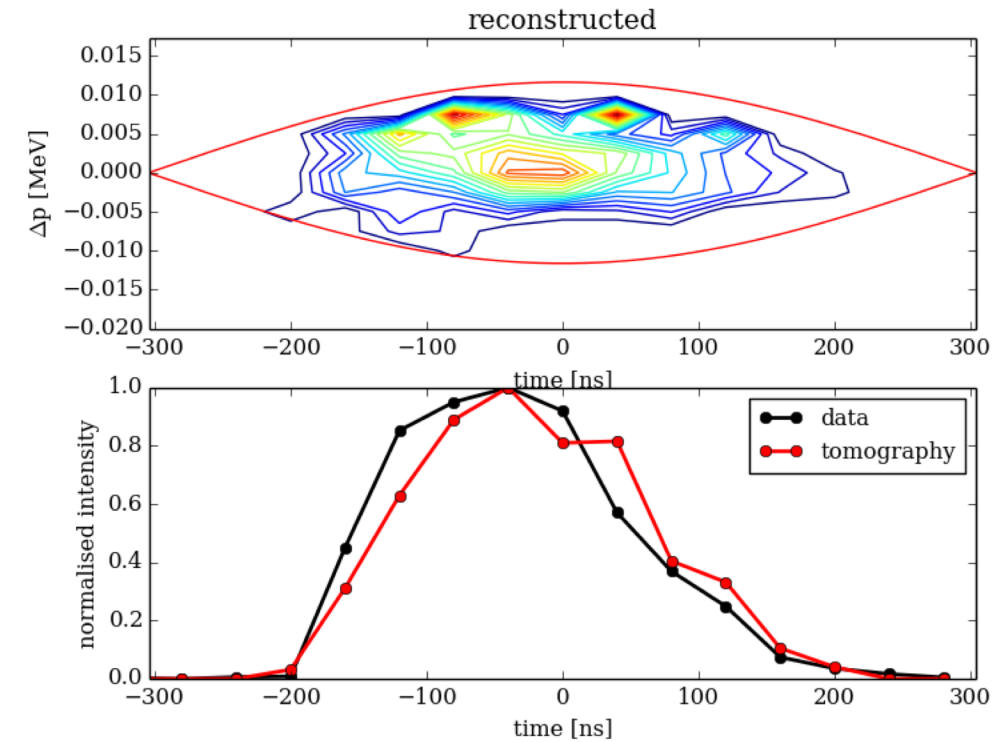


Raw bunch monitor data

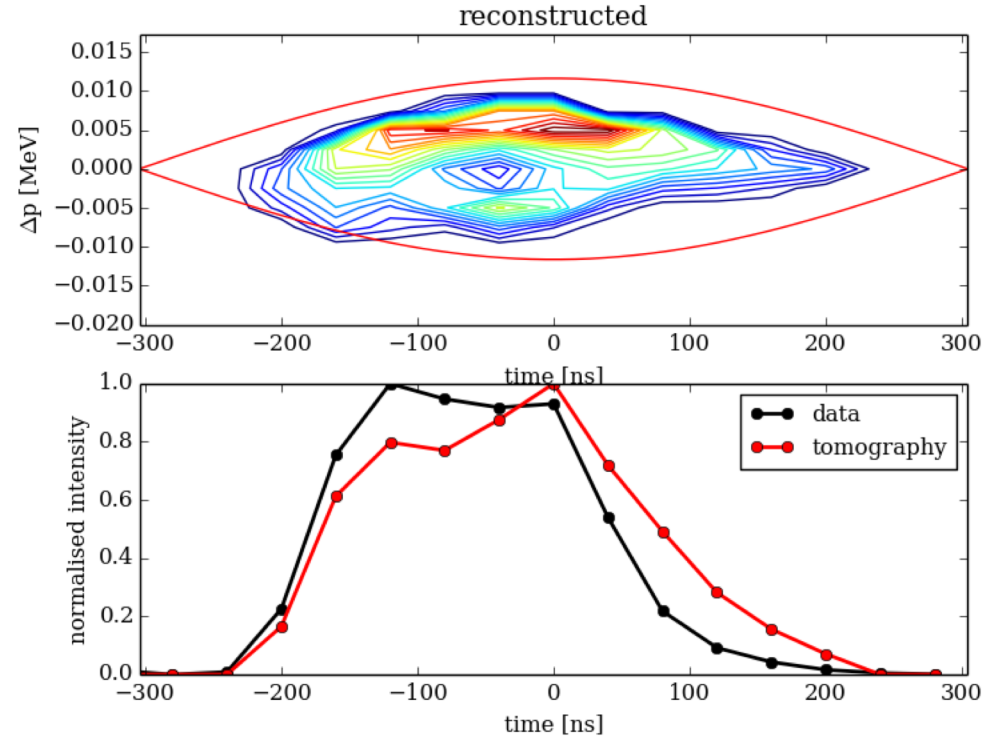


Bunch monitor data as input to tomography code

Reconstructing phase space using experimental data



$t = 0.75\text{ms}$



$t = 1.03\text{ms}$

Assumed ϕ_s : 0 deg.

Number of bins in projection: 16

Number of "turns": 100 (=0.5* T_s)

Tomography code issues/future work

- Resolve remaining discrepancy between input and reconstructed profile widths.
- Show turn-by-turn evolution of reconstructed phase space.
- Deal with variation of TOF with radius (allow number of "bins per frame" to vary in the tomography code).
- Introduce foil crossing in tomography algorithm (fixed energy loss per turn?).
- Tomography in beam stacking case – can we resolve the accelerated and stacked bunches?