



Science & Technology
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Space charge study and modelling ERIT (version 0.41)

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Goals (1)

- Is bunch charge limit the same as one in a synchrotron?

Is transverse tune spread of 0.25 (for example) achievable?

Resonance lines are denser with stronger nonlinearity.

Can be suffered more from image charge and current.

Problem is the same in scaling and “tune stabilized” non-scaling FFAG.



Goals (2)

- Does transverse painting work?
 - Does it create desirable distribution and reduce peak density?
 - (Nonlinear) **coupling in two transverse planes is stronger.**
- Does large aperture in horizontal help?
 - Can we keep anisotropic emittance?

See whether emittance is under control.



Steps

- Back of the envelope calculation
- Modelling with codes
- Beam experiments
- Hardware developments



Back of the envelope calculation (0)

- Basic beam parameters

$$T = 11 \text{ MeV (E = 949.272 MeV)}$$

$$P = 144.094 \text{ MeV/c}$$

$$\gamma = 1.011724$$

$$\beta = 0.151794$$

$$\varepsilon_{\text{rms}} = 8 \pi \text{ mm mrad (unnormalized, rms)}$$

$$\varepsilon_{95\%} = 48 (=6 \times 8) \pi \text{ mm mrad (unnormalized, 95\%)}$$

$$dT/T = 0.1\% \text{ (rms)}$$

$$(dp/p = 0.05\% \text{ (rms)})$$



Back of the envelope calculation (1)

- Tune shift (for uniform beam)
$$\Delta Q = -\frac{r_p n_t}{2\pi\epsilon\beta^2\gamma^3} \frac{1}{B_f}$$

$\epsilon_{100\%} = 100 \pi \text{ mm mrad}$ (unnormalized, 100%)

$B_f = 0.25$

$n_t = 6 \times 10^{11}$

gives $\Delta Q = -0.25$

- Number of particles
$$n_t = 2\pi R \cdot TN \cdot \frac{I}{e\beta c}$$

$n_t = 6 \times 10^{11}$

$R = 2.35 \text{ m}$

$I = 5 \text{ mA}$

gives $TN = 59$ (or 19 micro s)



Back of the envelope calculation (2)

- Bucket height

$$B_h = 2 \sqrt{\frac{eV}{2\pi\beta^2 E h |\eta|}}$$

$$V = 0.225 \text{ MV}$$

$$E = 11 + 938 \text{ MeV}$$

$$h = 6$$

$$\eta = \alpha_t - 1/\gamma^2 = -0.633$$

$$\text{gives } B_h (=dp/p) = 4.15 \times 10^{-2}$$

- Synchrotron tune

$$Q_s = \sqrt{\frac{h e V |\eta|}{2\pi\beta^2 E}}$$

$$\text{gives } Q_s = 7.88 \times 10^{-2} \text{ (or 13 turns)}$$



Back of the envelope calculation (3)

- Longitudinal space charge $F_{sc} / e = -\frac{eg_0}{4\pi\epsilon_0\gamma^2} \frac{\partial\lambda}{\partial s}$
 $k_0 = 7.317 \times 10^{11}$
 $k_2 = 1.935 \times 10^{12}$
 $\text{Sqrt}[k_0/k_2] = \lambda_{rf}/4$ and $n_t = 6 \times 10^{11}$
 $g_0 = 2$
gives $(F_{sc}/e)/s = 1.1 \times 10^4$
- rf voltage $F_{rf} / e = V \sin(2\pi s / \lambda_{rf}) = \frac{2\pi Vs}{\lambda_{rf}}$
 $V = 0.225 \text{ MV}$
 $\lambda_{rf} = 2\pi R/h = 2.461 \text{ m}$
gives $(F_{rf}/e)/s = 5.7 \times 10^5 (>> 1.1 \times 10^4)$



Back of the envelope calculation (4)

- Energy loss by foil scattering

$dE = 0.760$ kV per turn (Okabe at FFAG10)

$\phi_s = \arcsin(0.760/225) = 0.19$ degree (negligible)

However, with coasting beam operation

$DE = dE \times TN = 0.760$ kV \times 1000 turns (for example) = 0.76 MeV

gives $DE/T = 6.9 \times 10^{-2}$

- Overlapping of linac micro structure

$$dt = \eta \frac{dp}{p} t_{rev}$$

$f_{Linac, rf} = 425$ MHz (Okabe at FFAG10)

$f_{rev} = 3.02$ MHz ($f_{ERIT, rf} = 18.1$ MHz)

gives $f_{Linac, rf}/f_{ref} = 141$

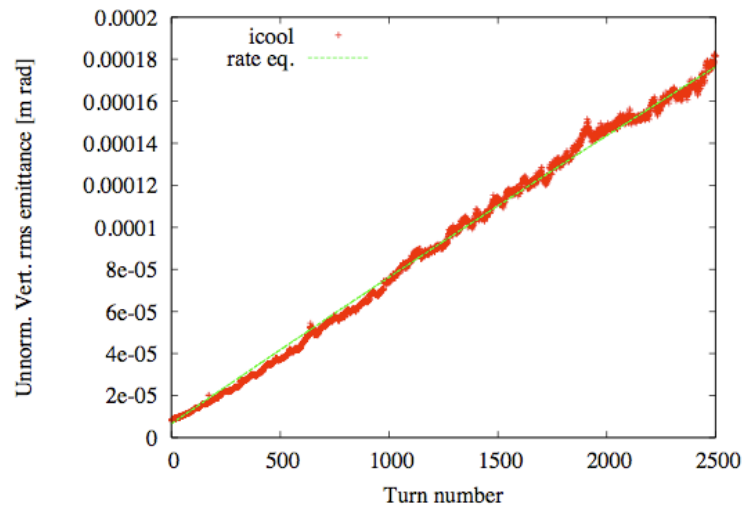
$n_{debunch} = (t_{rf}/t_{rev})/(\eta \times dp/p) = 1/(141 \times 0.633 \times 0.0005) = 22$ turns



Modelling with codes (1.0)

- Main purpose is to see whether emittance growth due to space charge can be identified and, if so, how large.

Another factor of emittance growth; foil scattering at injection.



Vertical emittance

by Okabe and Mori



Modelling with codes (1.1)

- Simulation of emittance evolution with space charge
 - **Without foil scattering effects**, estimate emittance evolution by space charge only.
 - Combine S-Code (FFAG) and Simpsons (space charge).
- Scan 2D tune space.
- Introduce fringe field and/or measured COD.



Modelling with codes (1.2)

- First, check dynamics without space charge.

Bucket height

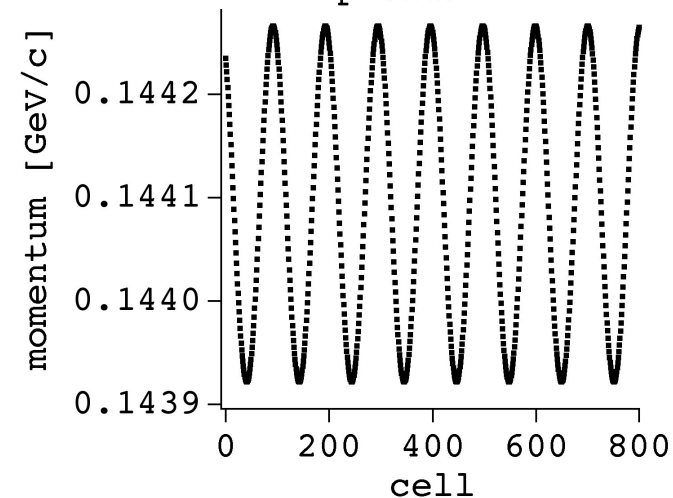
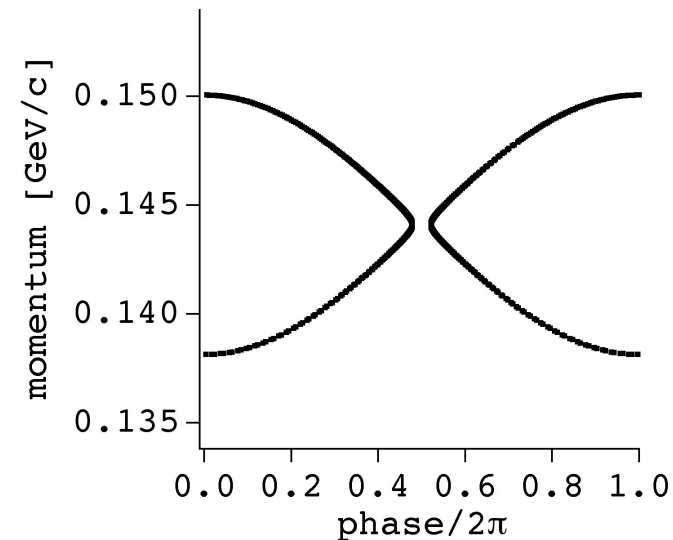
$$\begin{aligned} dp/p &= (0.150-0.144)/0.144 \\ &= 4.2 \times 10^{-2} \end{aligned}$$

$$\text{c.f. } B_h (=dp/p) = 4.15 \times 10^{-2}$$

Synchrotron tune

$$8 \text{ oscs}/100 \text{ turns} = 8 \times 10^{-2}$$

$$\text{c.f. } Q_s = 7.88 \times 10^{-2} \text{ (or 13 turns)}$$





Modelling with codes (1.3)

- Orbit and optics

Orbit

$$T_{\text{rev}} = 357.385 \text{ ns or}$$
$$f_{\text{rf}} = 16.789 \text{ MHz (h = 6)}$$

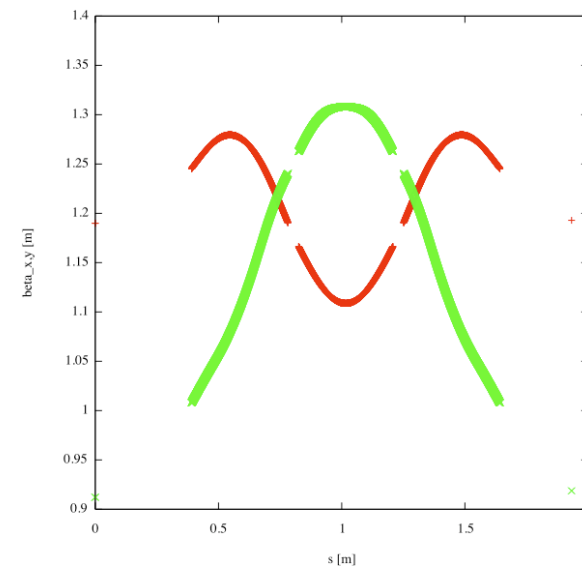
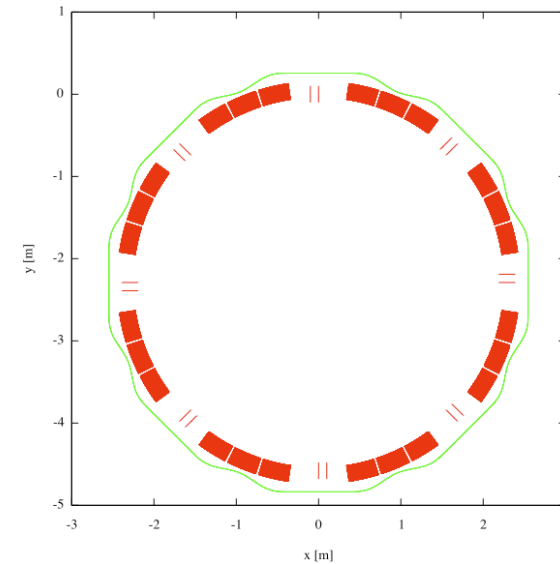
c.f. 18.1 MHz

Optics

$$(Q_x, Q_y) = (1.816, 2.292)$$

with Enge fringe ($g=30 \text{ mm}$)

c.f. (1.73, 2.22)



Red: beta_x
Green: beta_y



Modelling with codes (1.4)

- Test run with space charge.



Modelling with codes (2)

- Simulation of capture process (1D only)
 - Assuming no chopper, estimate the number of particles captured in a rf bucket.
 - Estimate bunching factor.
 - With foil scattering, estimate longitudinal emittance.



Modelling with codes (3)

- Simulation of foil scattering
 - **Without space charge effects**, estimate emittance evolution by foil scattering.
(I assume that the previous simulation by Okabe does not have multi-turn injection process.)
 - Simulate (or superimpose) multi-turn injection process.
 - Simulate off-axis injection process.



Beam experiment (0.1)

beam emittance (size) measurement vs. turn number

- Fix collimator aperture slightly larger than the linac beam.
- Identify time (turn) when beam loss starts appearing.
- Enlarge collimator aperture a little larger and identify time (turn) when beam loss starts appearing.
- Repeat the above process and plot collimator aperture (on y-axis) vs. time (turn) when beam loss starts (on x-axis).



Beam experiment (0.2)

orbit matching

- Repeat the beam emittance (size) measurement with slightly different initial injection orbit.
- When a beam is injection on axis, measured growth should be minimum without space charge effects.



Beam experiment (0.3)

foil position

- Repeat the beam emittance (size) measurement with different foil position.
- Can we reduce the hitting probability?
- Can we optimize the foil position such that large amplitude particle will escape from foil scattering but still in the aperture?



Beam experiment (1.1)

foil scattering only

- Without rf
- Beam emittance (size) increase by foil scattering.
 - Inject small number of particles on axis (less than ~ 100 turns, but enough to do emittance measurement on the previous).
 - Measure beam emittance (size) vs. time (turn).
 - This process should be independent of beam intensity so that we can use the result to estimate emittance growth purely from scattering when more number of particles are injected.



Beam experiment (1.2)

foil scattering and space charge

- Without rf
- Beam emittance (size) increase by foil scattering and space charge.
 - Inject large number of particles on axis (~ 240 turns or more, which should make tune shift of ~ -0.25).
 - Measure beam emittance (size) vs. time (turn).
 - Can we identify emittance growth on top of foil scattering?



Beam experiment (1.3)

with larger initial emittance

- Without rf
- Same as (1.1) to (1.2), but inject off axis.
 - Growth rate $d\varepsilon/\varepsilon$ by scattering becomes relatively smaller.
 - However, need more number of particles to make the same space charge tune shift.
 - Is this easier to separate emittance growth by foil scattering and space charge?



Beam experiment (2)

bunched beam

- With rf
- Basically the same procedure of (1.1) to (1.3)
 - However, physics is different. Not quantitative difference due to bunching factor, but qualitative difference due to synchrotron oscillations, resonance crossing, etc.
 - Monitor bunch profile.



Beam experiment (3)

other parameter space

- After establish the way to observe space charge effects, explore parameter space.
 - rf voltage
 - rf gymnastics around injection
 - 2D scan in tune space.
 - With and without COD correction.
 - Start from anisotropic emittance.
- etc.



Hardware developments

- Bump magnets
 - Single or pi-bump?
- Beam position
 - BPM
- Beam profile
 - Scraper
 - Flying wire
 - Ionization profile monitor