



# Tune measurement with NAFF, ver.2

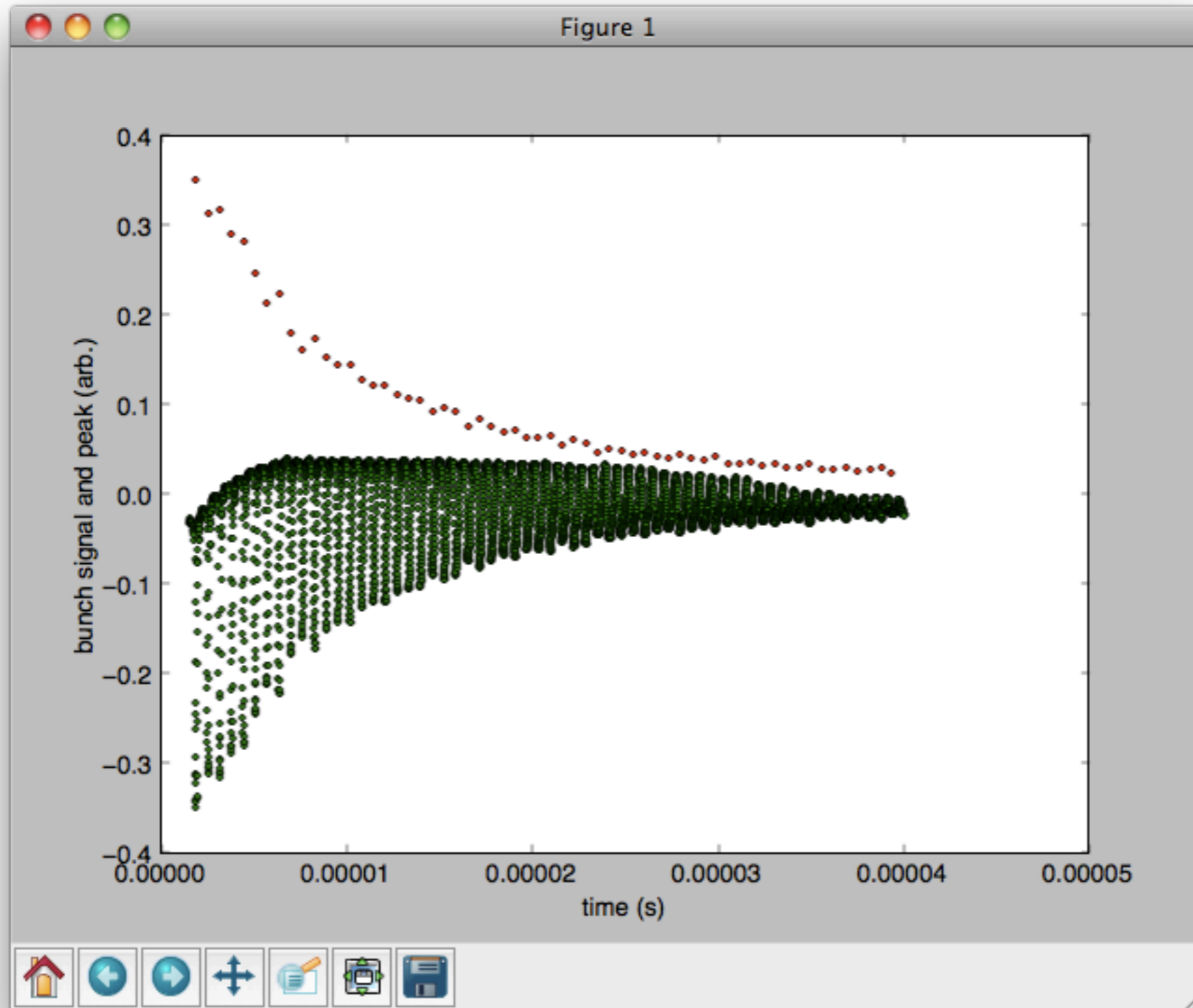
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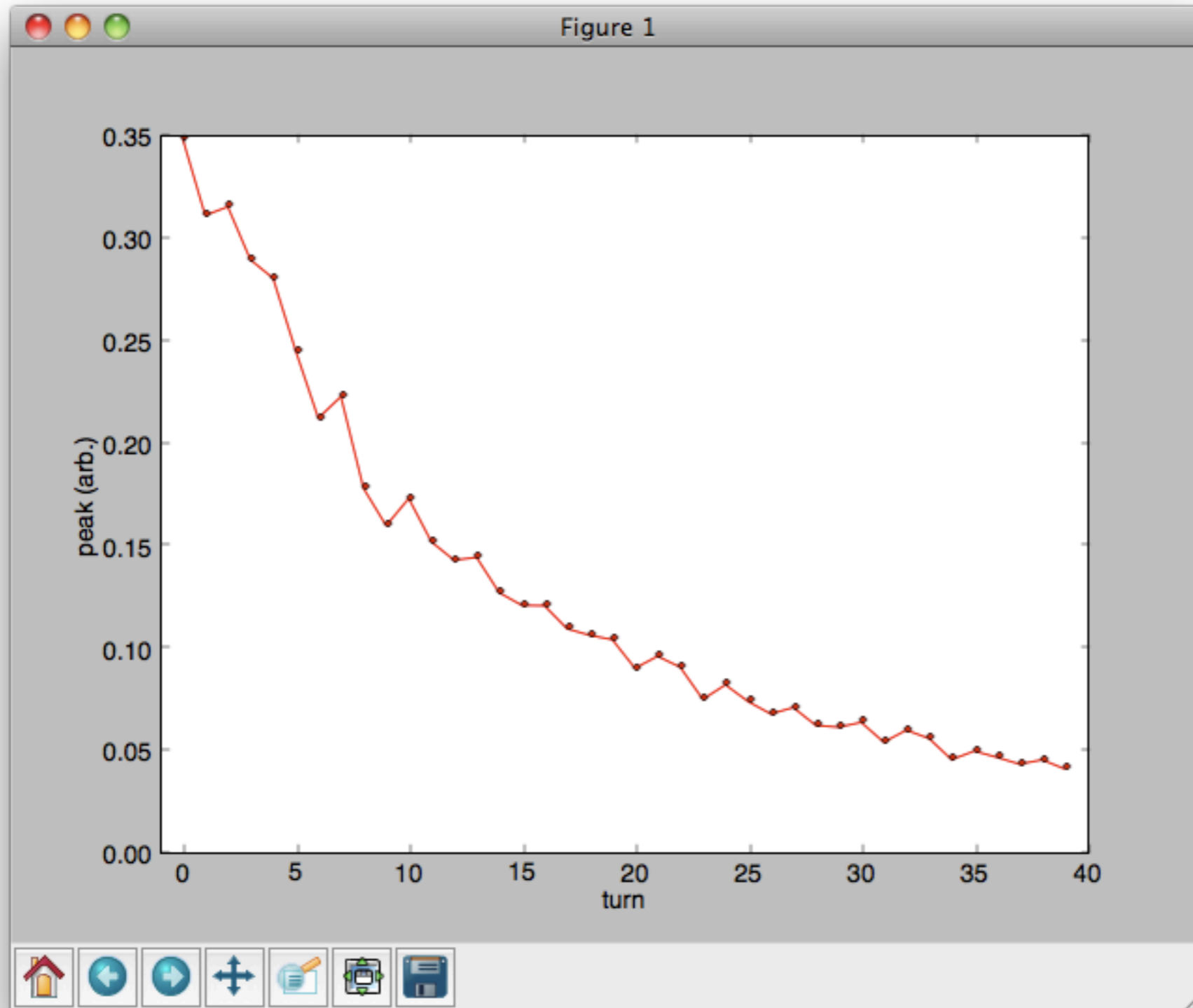
19 November 2013

- HPF did not improve the tune measurement.
- Beam does not last for many turns, at most ~60 turns. A simple FFT gives the tune resolution of  $1/60=0.017$ .
- NAFF (numerical analysis of fundamental frequency) gives much higher resolution. It was demonstrated in EMMA.

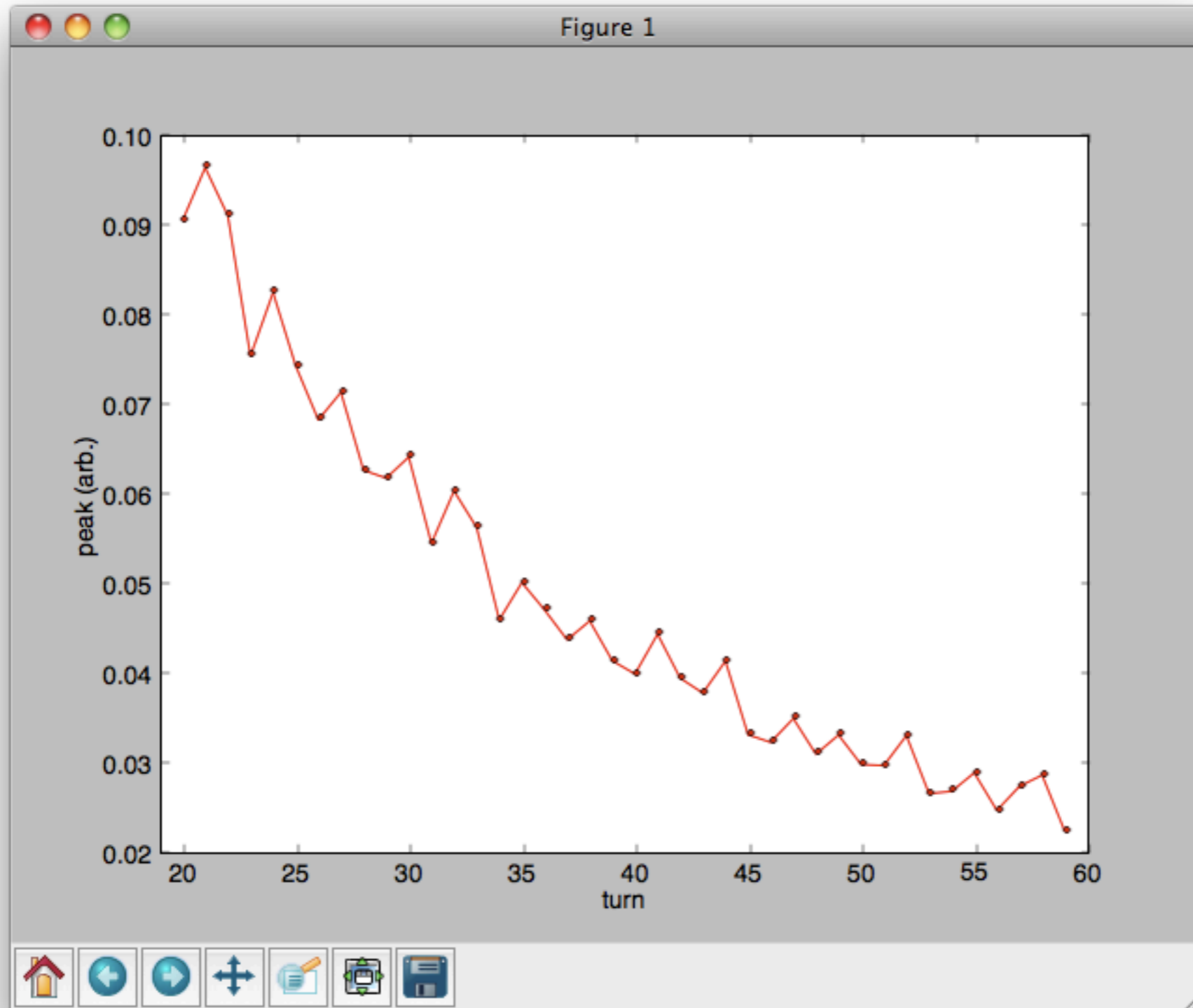
# Raw data (black) and peak sampled (red)



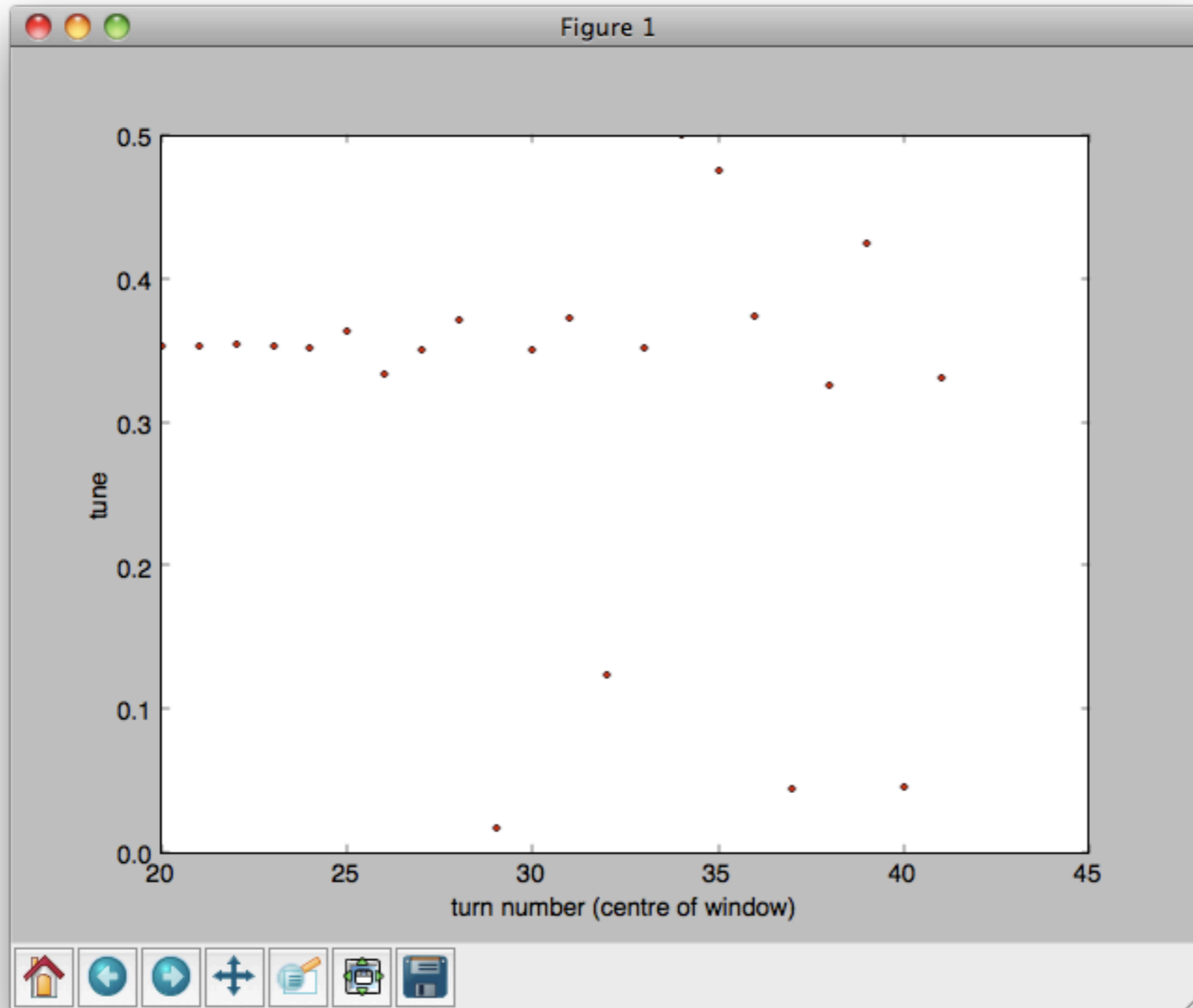
# 40 peak data from turn 0 to 39



# 40 peak data from turn 20 to 59

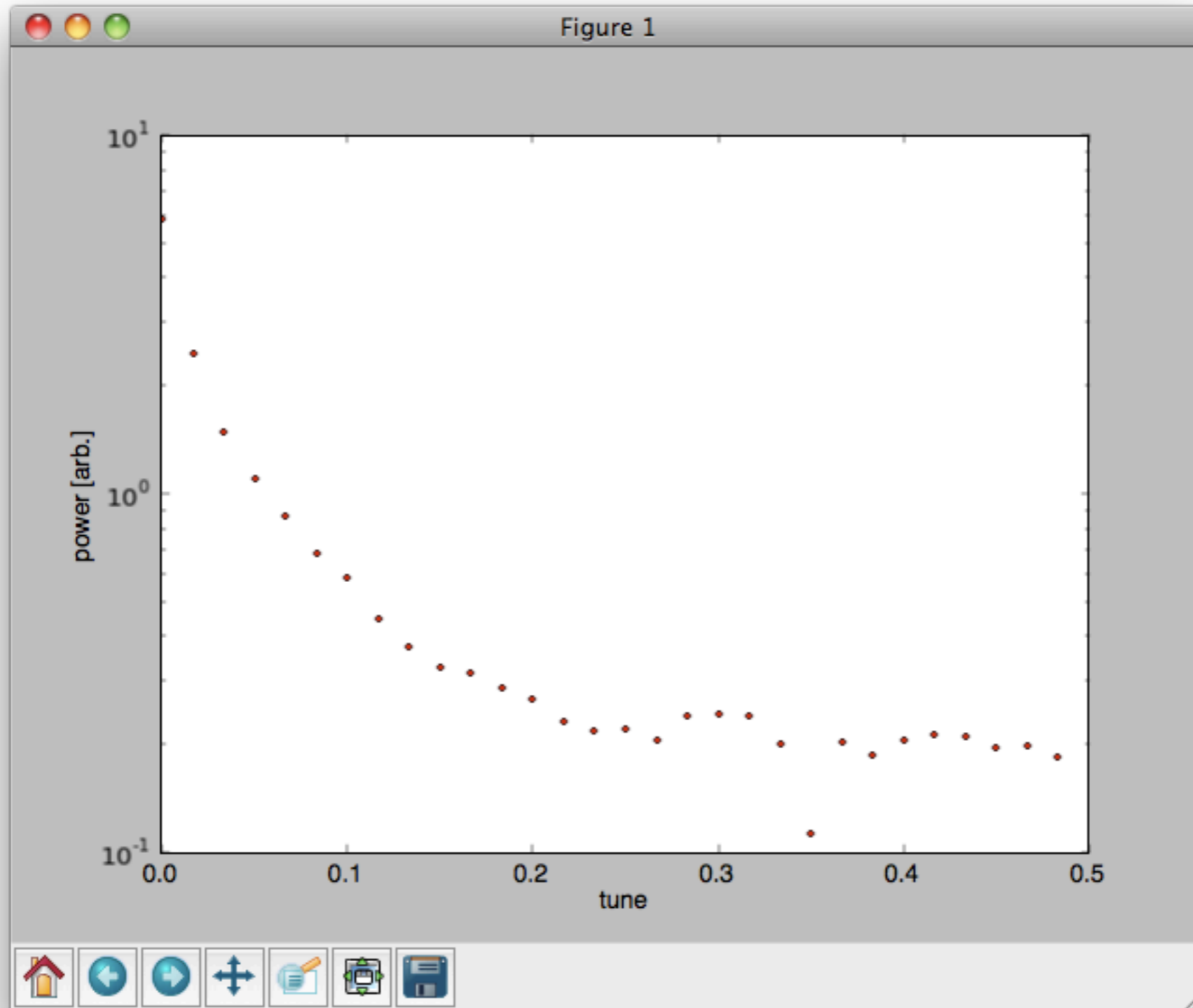


# Tune vs turn (or each moving window when width is 40 turns)



←  $Q_y=0.35$

# FFT of all the peak data as a comparison



# Dependence of window size (1)

- NAFF claims that tune resolution is proportional to  $1/n^4$ .
- In practice, tune estimate depends on window size.
- Wide window (large sampling  $n$ ) does not necessarily give more accurate result.
- Nevertheless, next page shows tune at the early turn is around 0.35 - 0.36 in any case.



# Dependence of window size (2)

