



Science & Technology  
Facilities Council

# KURRI FFAG simulation update

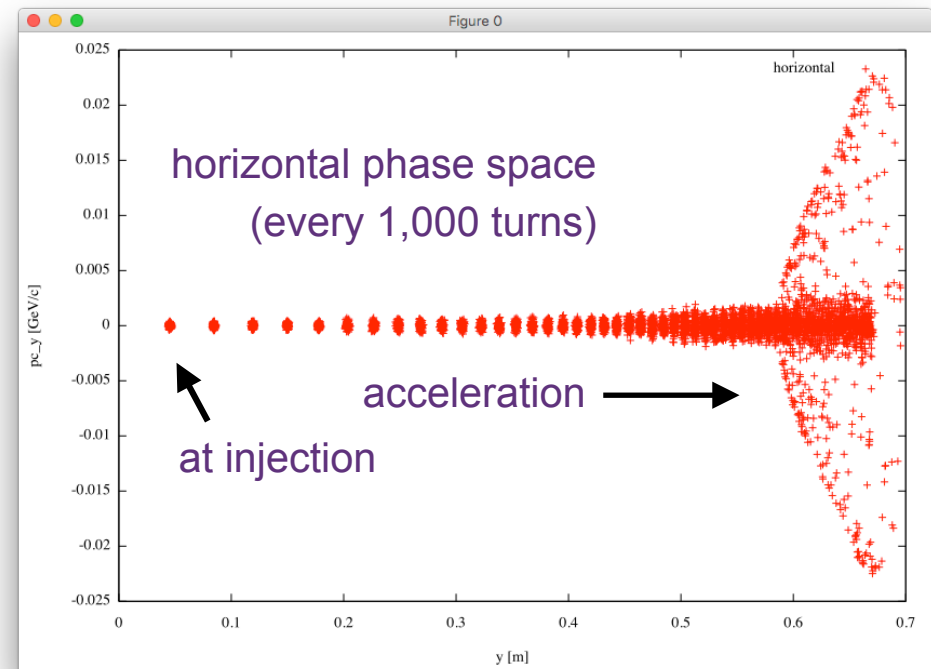
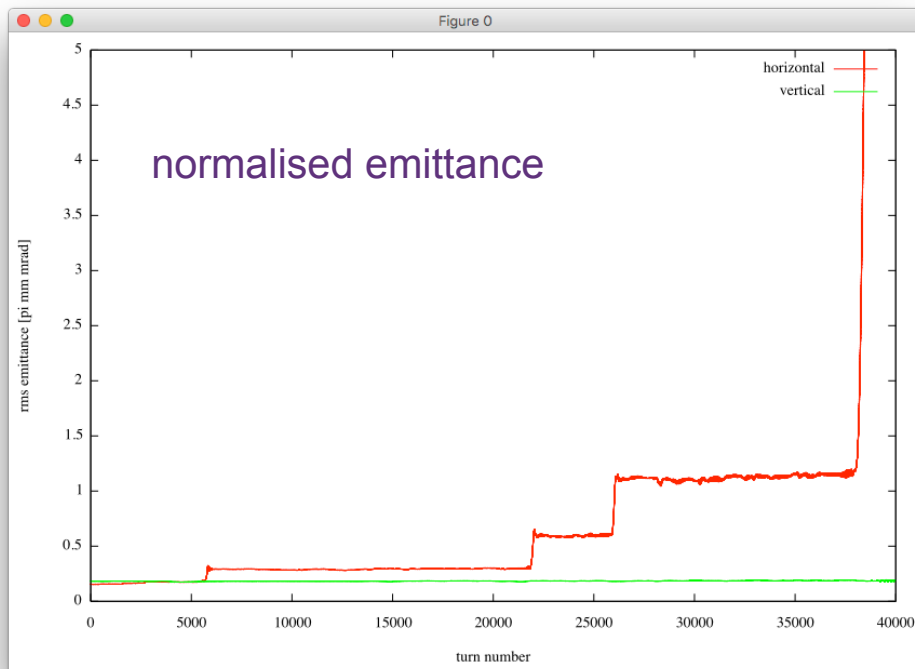
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23 March 2016

# Emittance evolution

Zgoubi and Scode show similar emittance jump at some turns (energy).

No space charge. No error in the lattice.

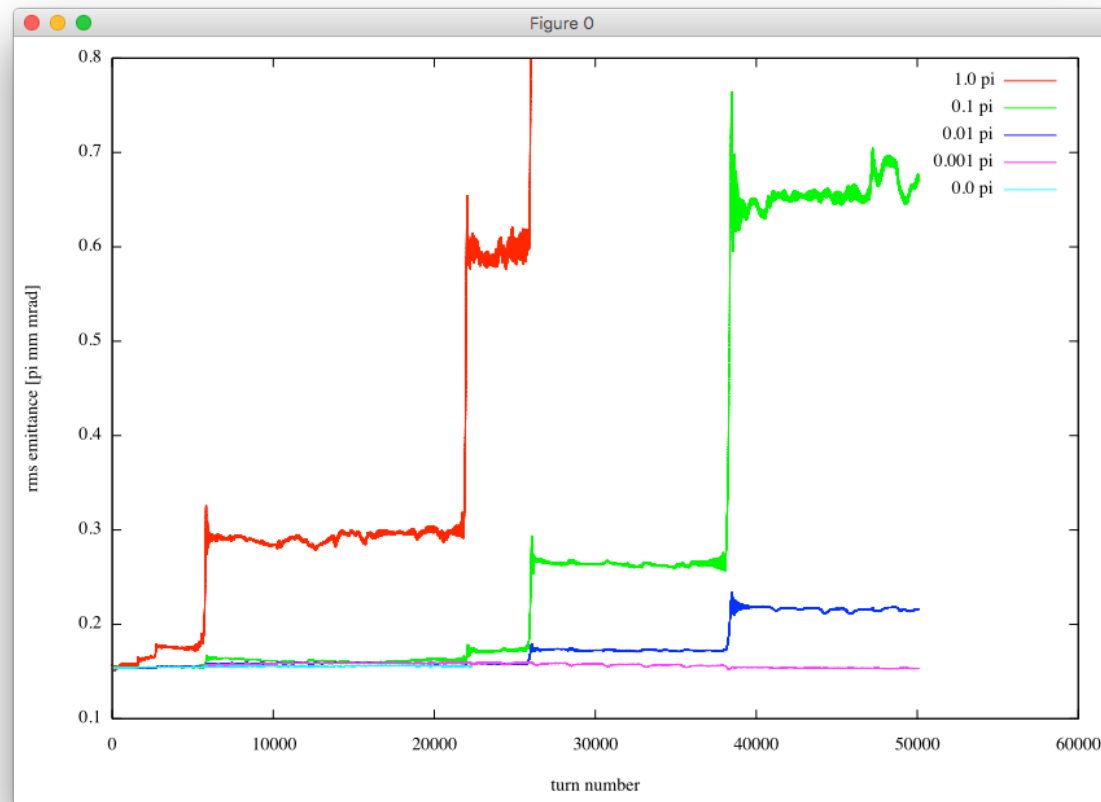
No jump in vertical plane.



$$\begin{aligned} \text{Kinetic energy [MeV]} \\ = 11.0 + 0.002 \times (\text{turn number}) \end{aligned}$$

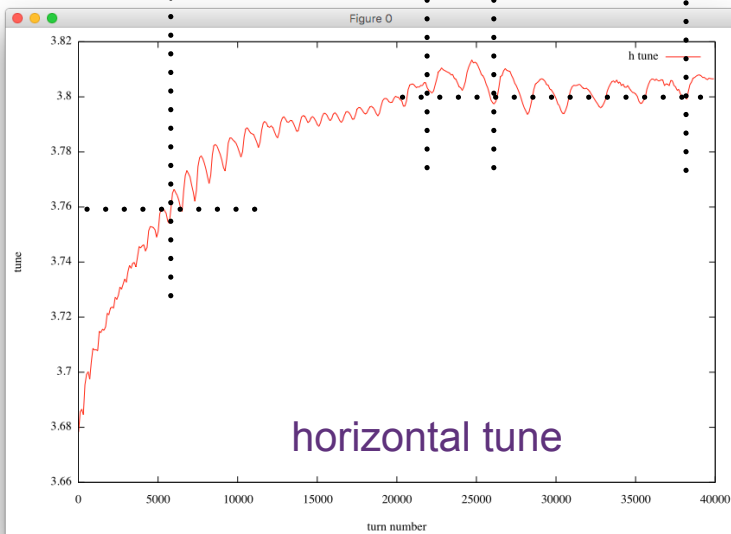
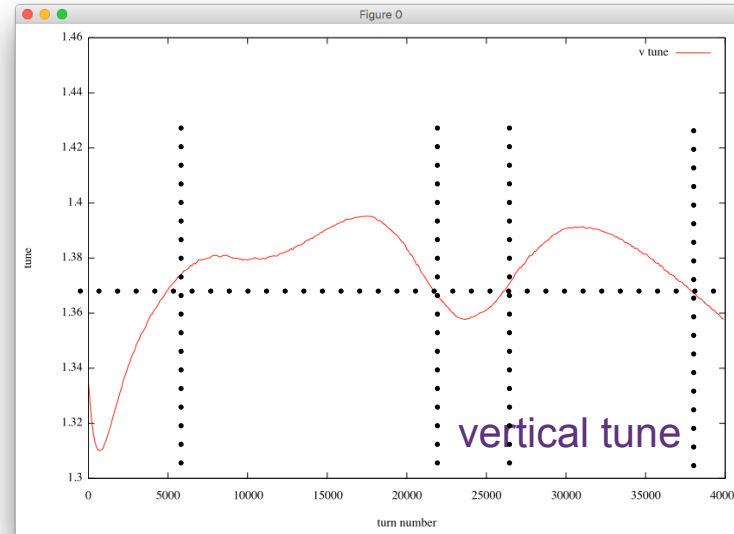
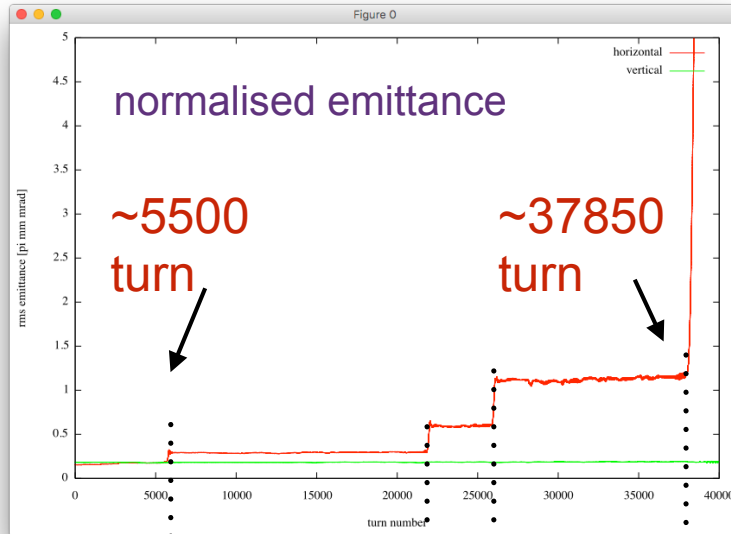
# Parameter dependence *vertical emittance*

When vertical emittance is reduced (1 pi to 0 pi), the jump disappears.



Except the first jump, it happens at around  $Q_h=3.8$

# Tune evolution

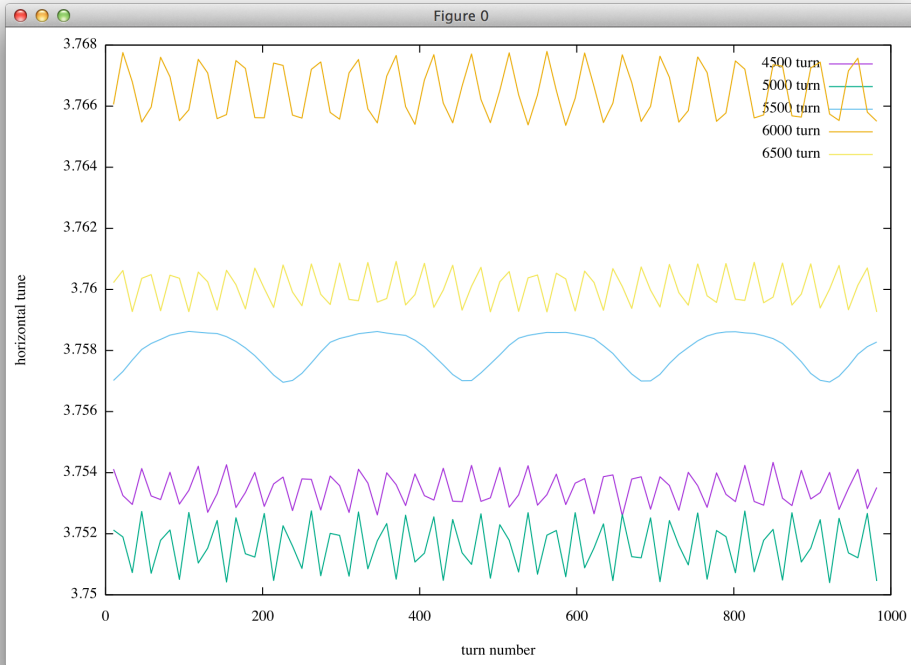


In fact,  $Q_v \sim 1.37$  when jump appears.

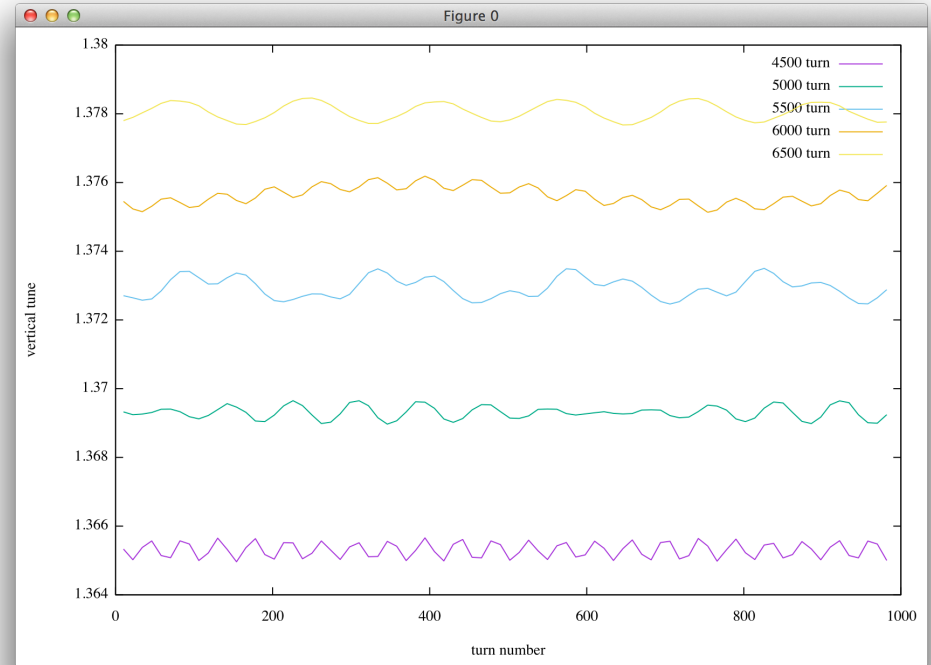
~~$Q_h + 6Q_v = 12$  7th order coupling~~

~~Since the order of vertical is much higher than horizontal, there is no jump in vertical?~~

# Tune at ~5500 turn



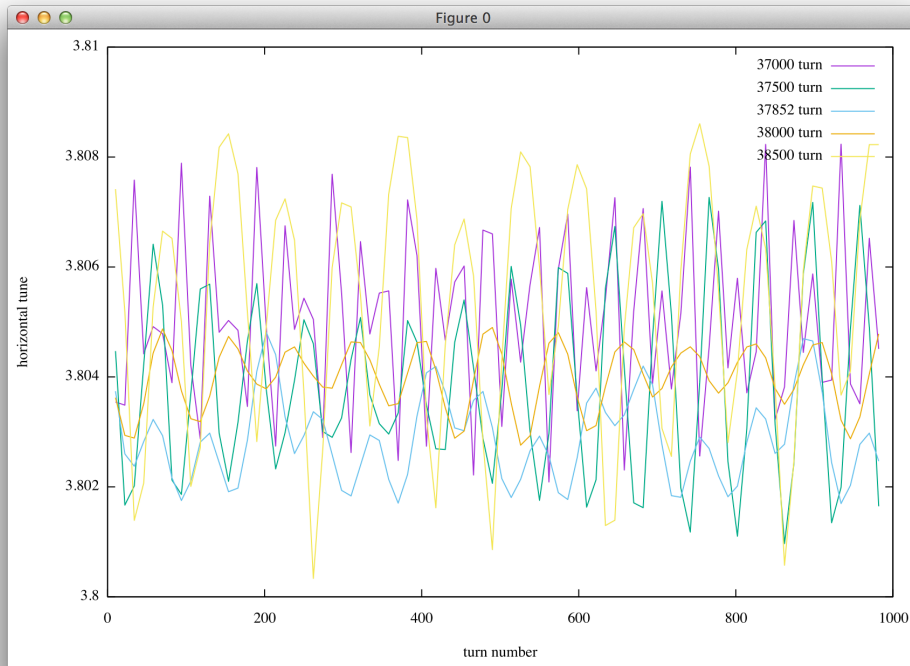
$Q_h = 3.758$



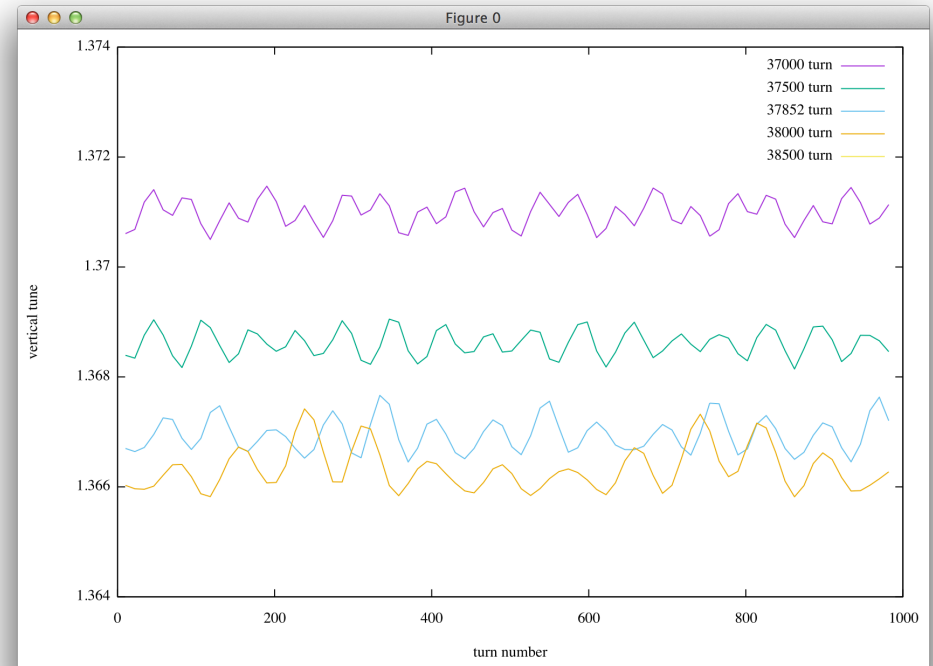
$Q_v = 1.373$

$$6Q_h + Q_v = 23.921$$

# Tune at ~37850 turn



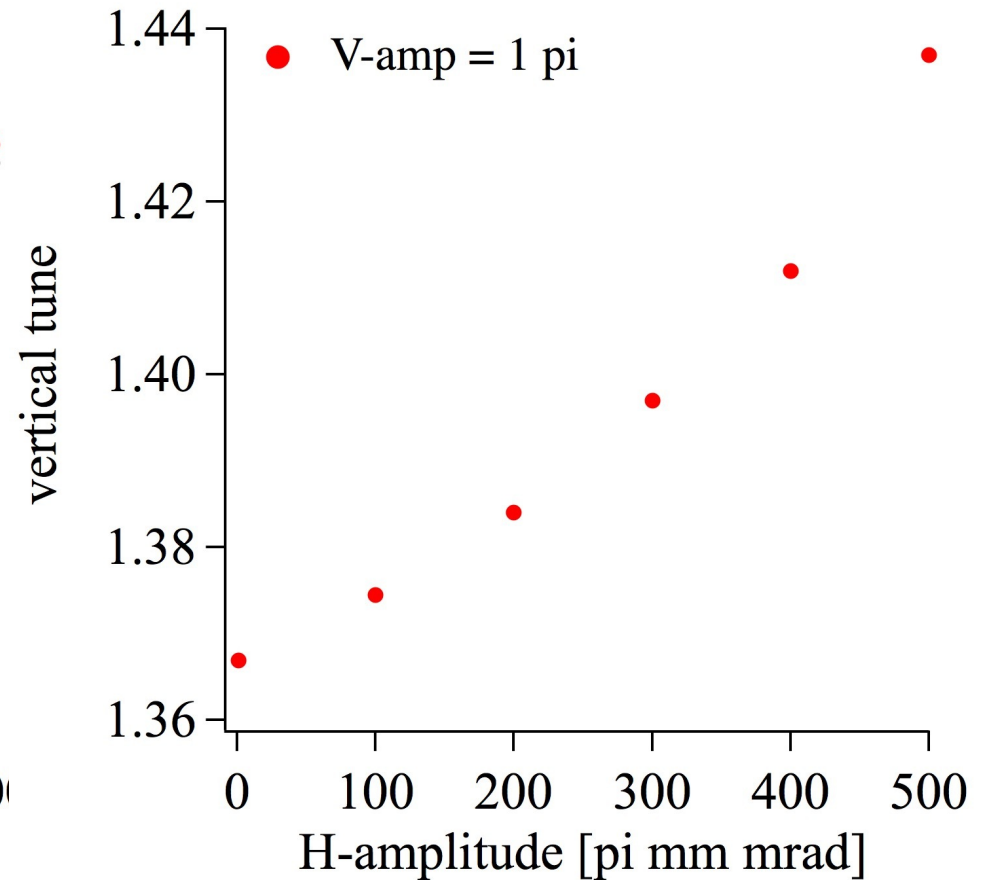
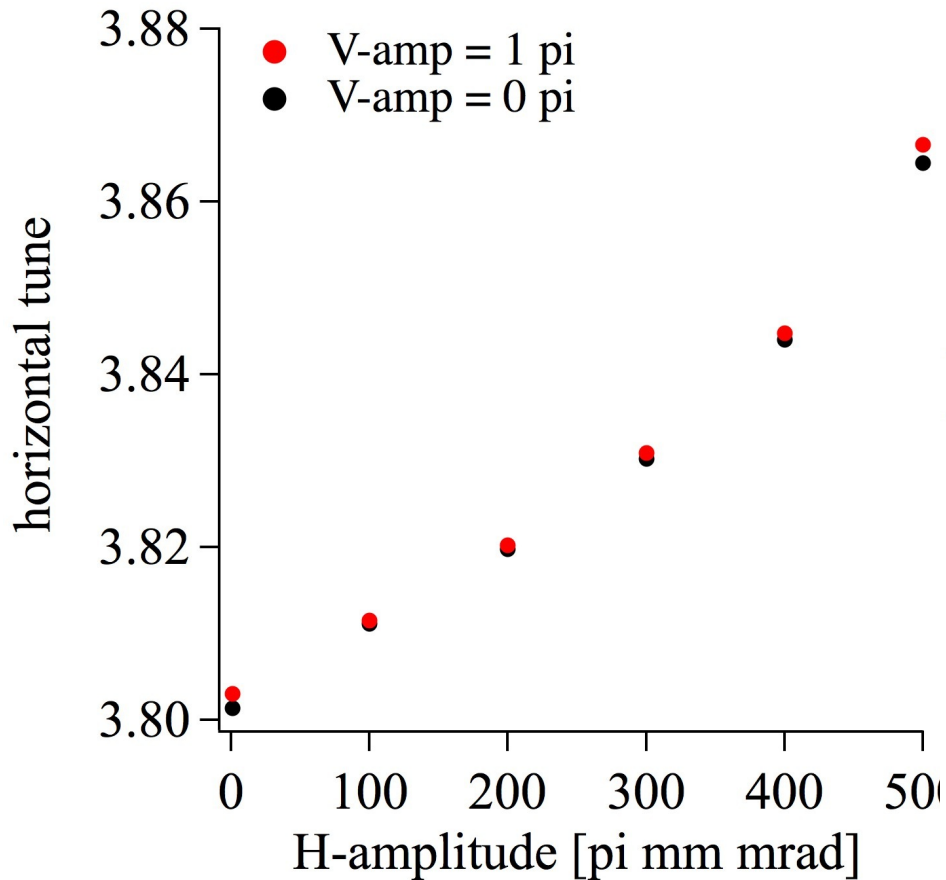
$Q_h = 3.803$



$Q_v = 1.367$

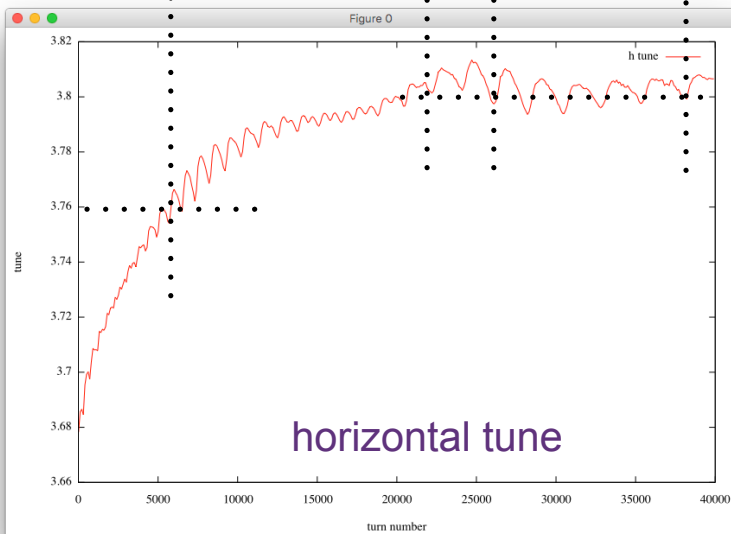
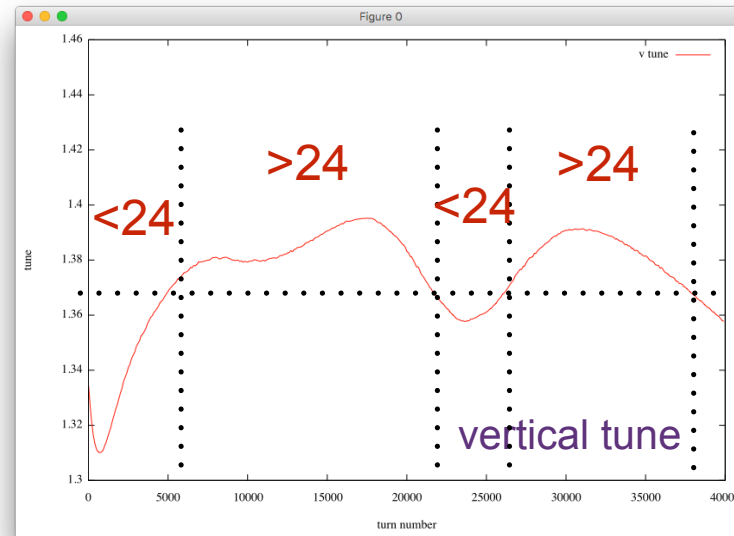
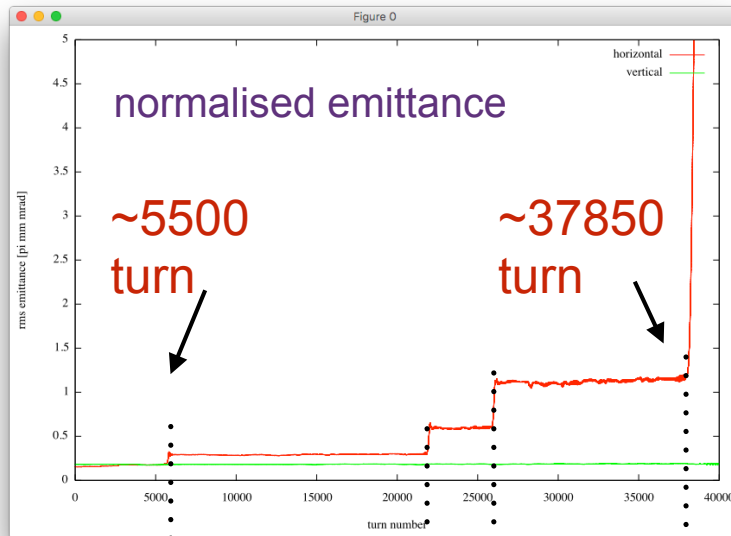
$$6Q_h + Q_v = 24.185$$

# Amplitude dependent tune



Amplitude dependent tune shift is negligible.

# Tune evolution



$$6Q_h + Q_v = 2 \times 12 \quad \text{7th order coupling}$$

Much higher order in horizontal plane is consistent with much higher increase of horizontal emittance.



# Remark

- Still it is mystery that no indication of emittance growth in vertical direction.
  - Does it depend on the crossing angle?
- Trapping at the end of a cycle can be understood by amplitude dependent tune shift.
  - Fixed point moves out to maintain the resonance condition.
- Another explanation is syncho-beta resonance which occurs only in horizontal direction.