

# Measurement of betatron tunes

---

---

Mao Takabatake  
Fukui University

# Outline

---

Motivation

How to measure

Experiments

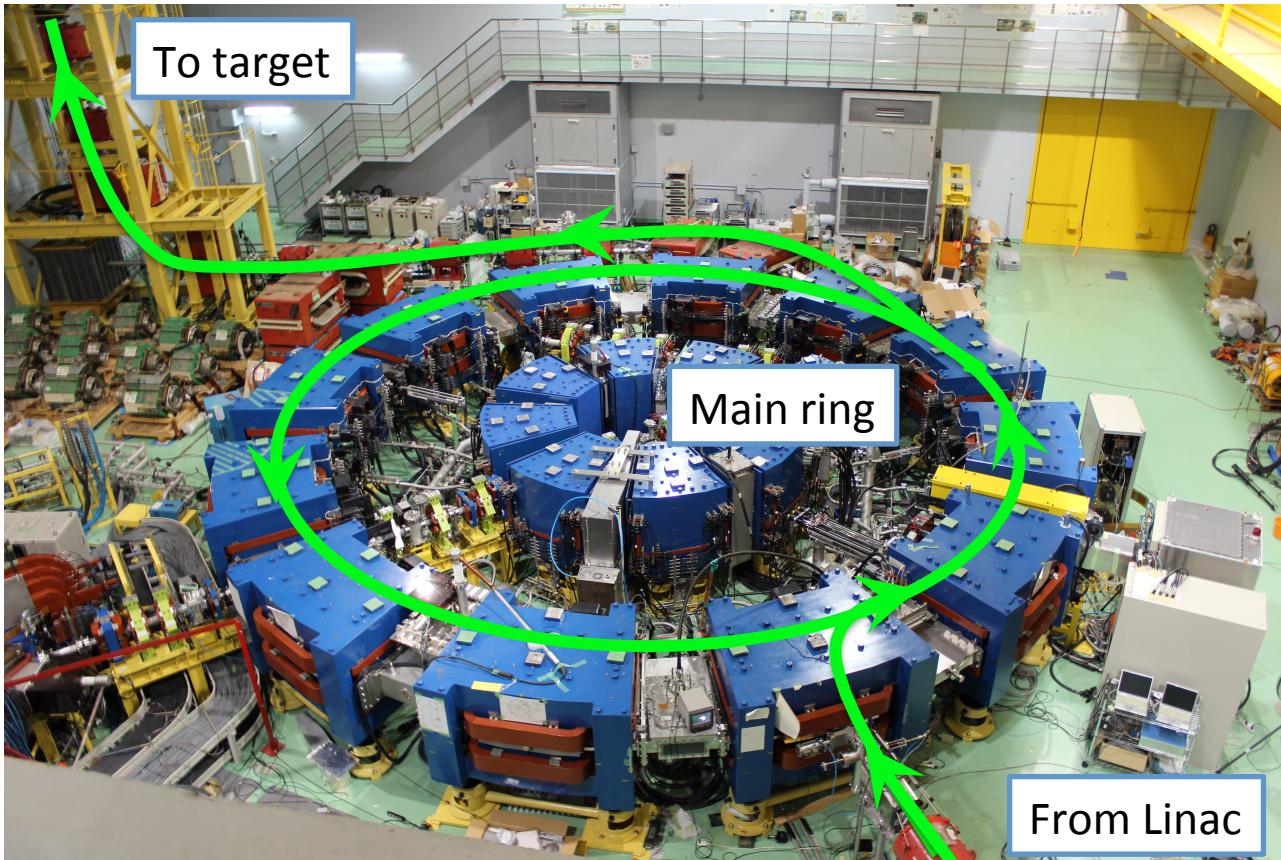
Results

Estimation

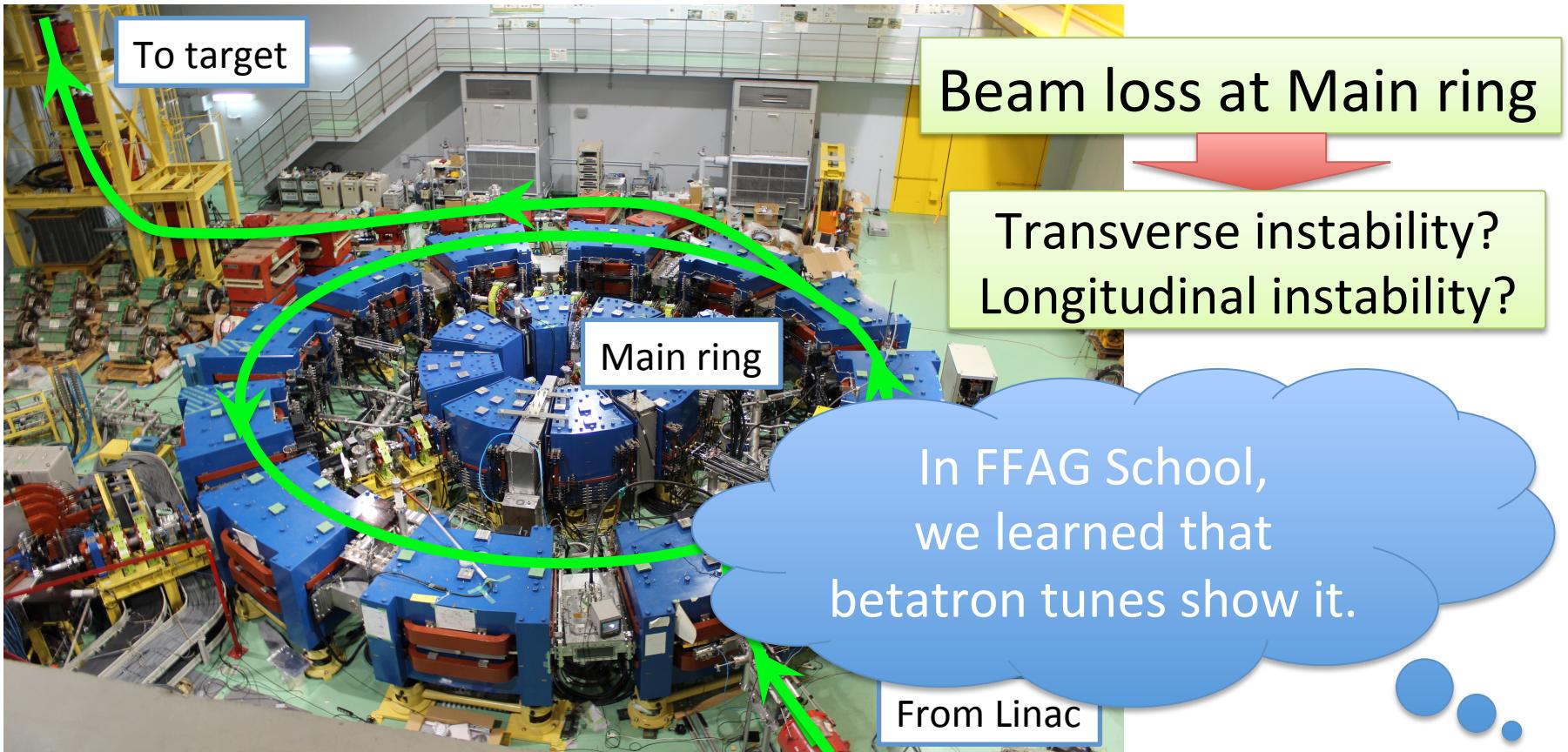
Summary

# Motivation

---

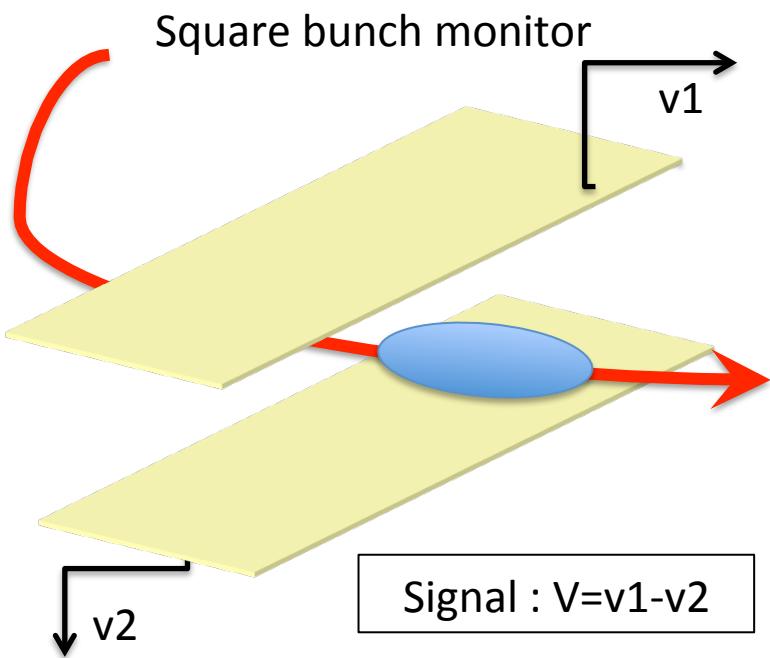


# Motivation

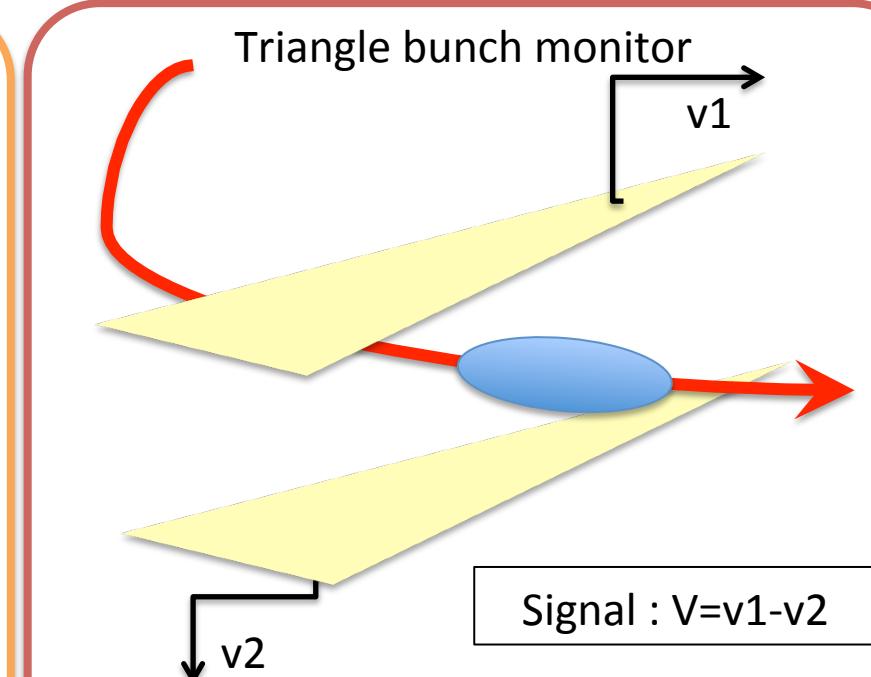


## Measure betatron tunes

# How to measure



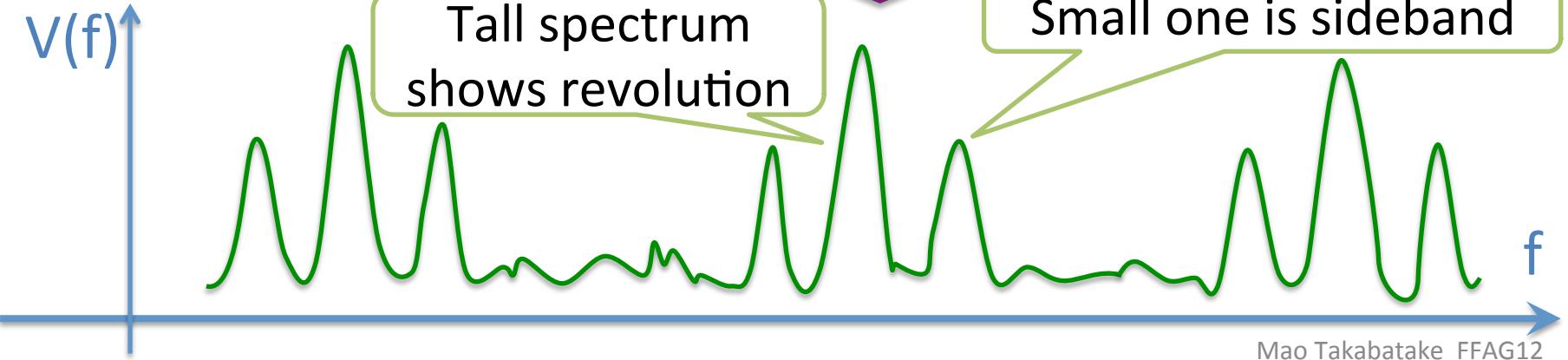
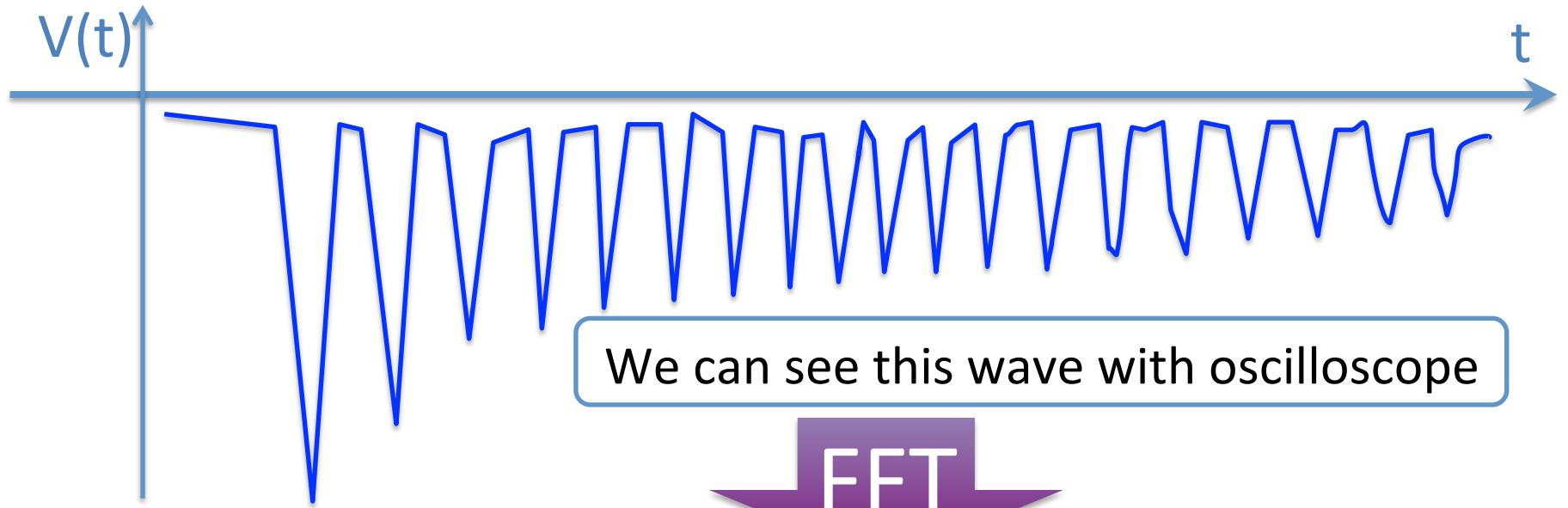
Signal height depends on **vertical** oscillation



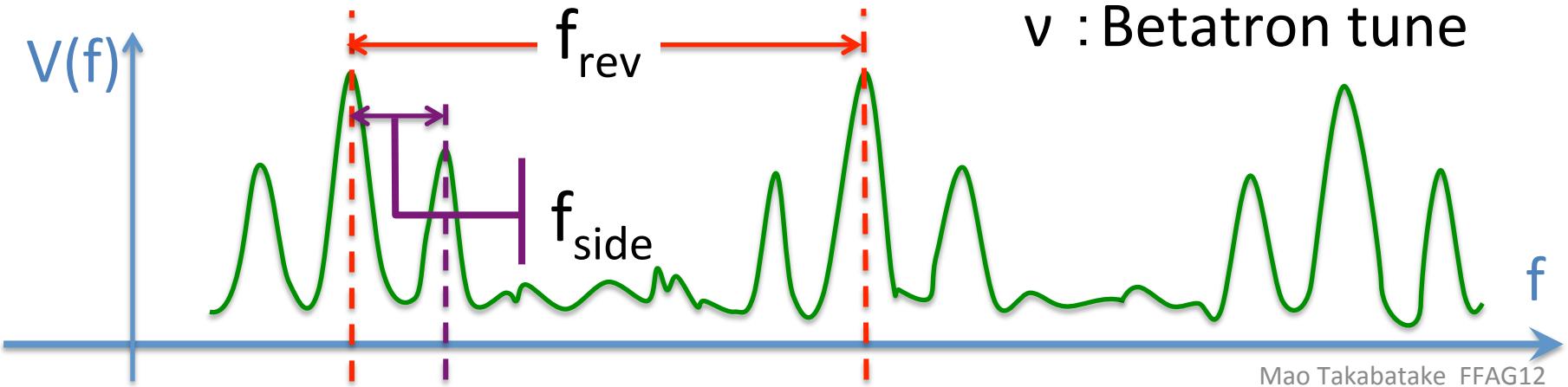
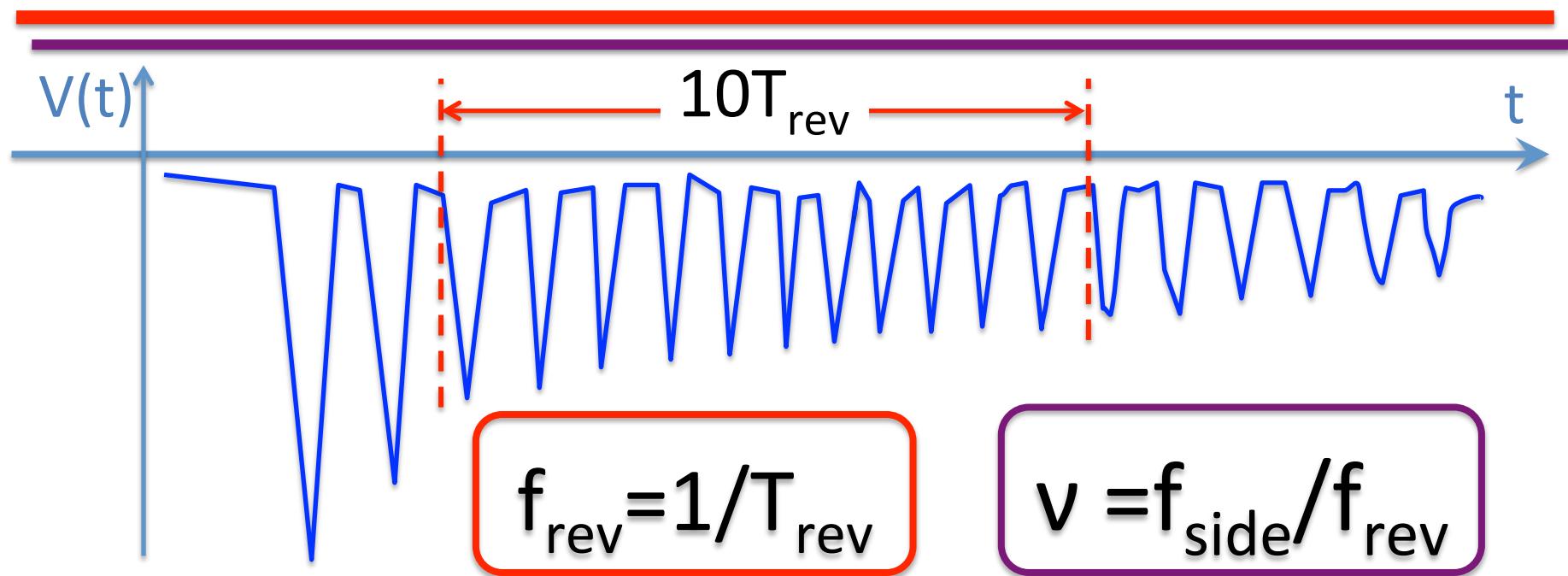
Signal height depend on **both** oscillations

Their difference shows **horizontal** oscillation

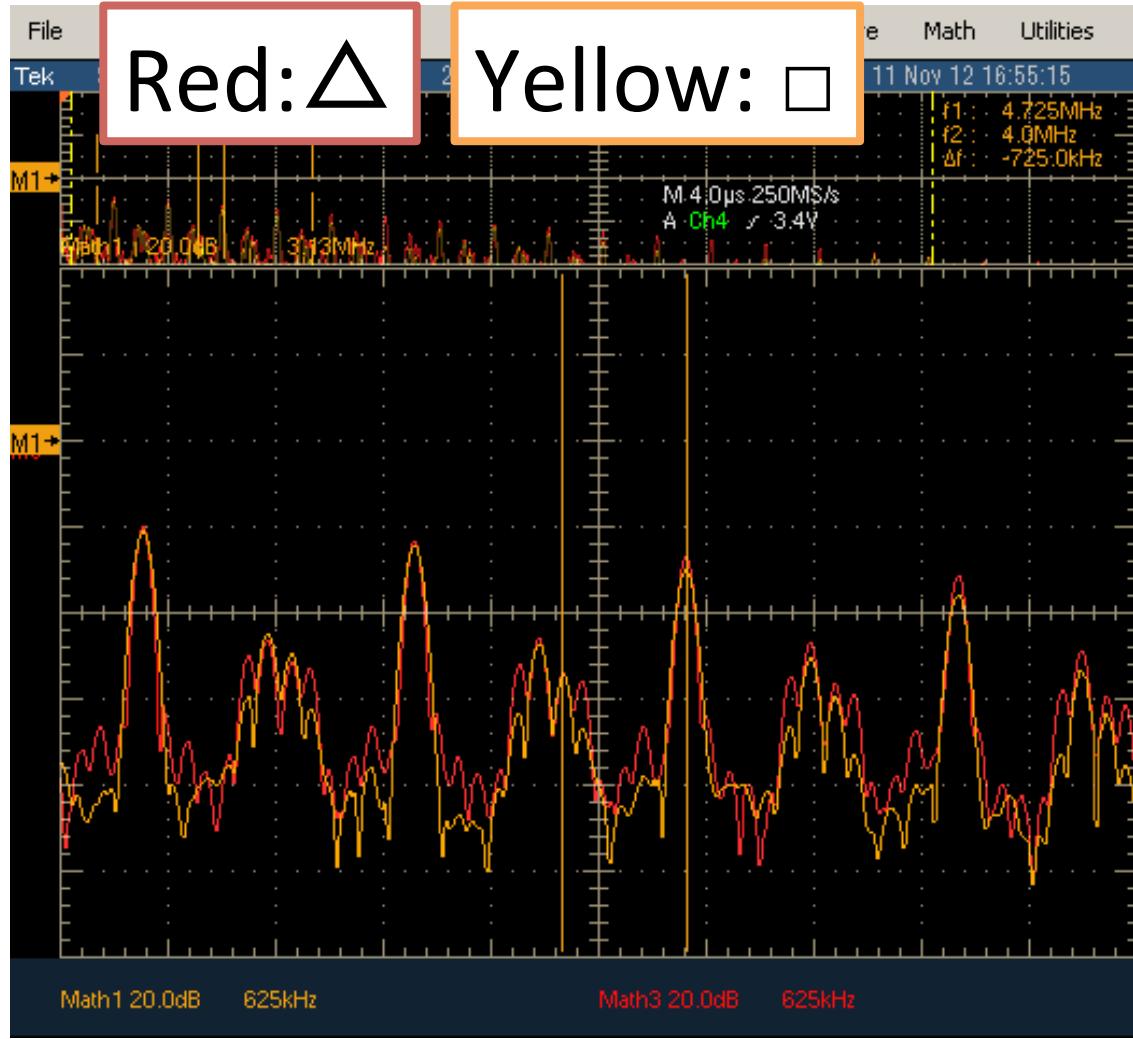
# How to measure



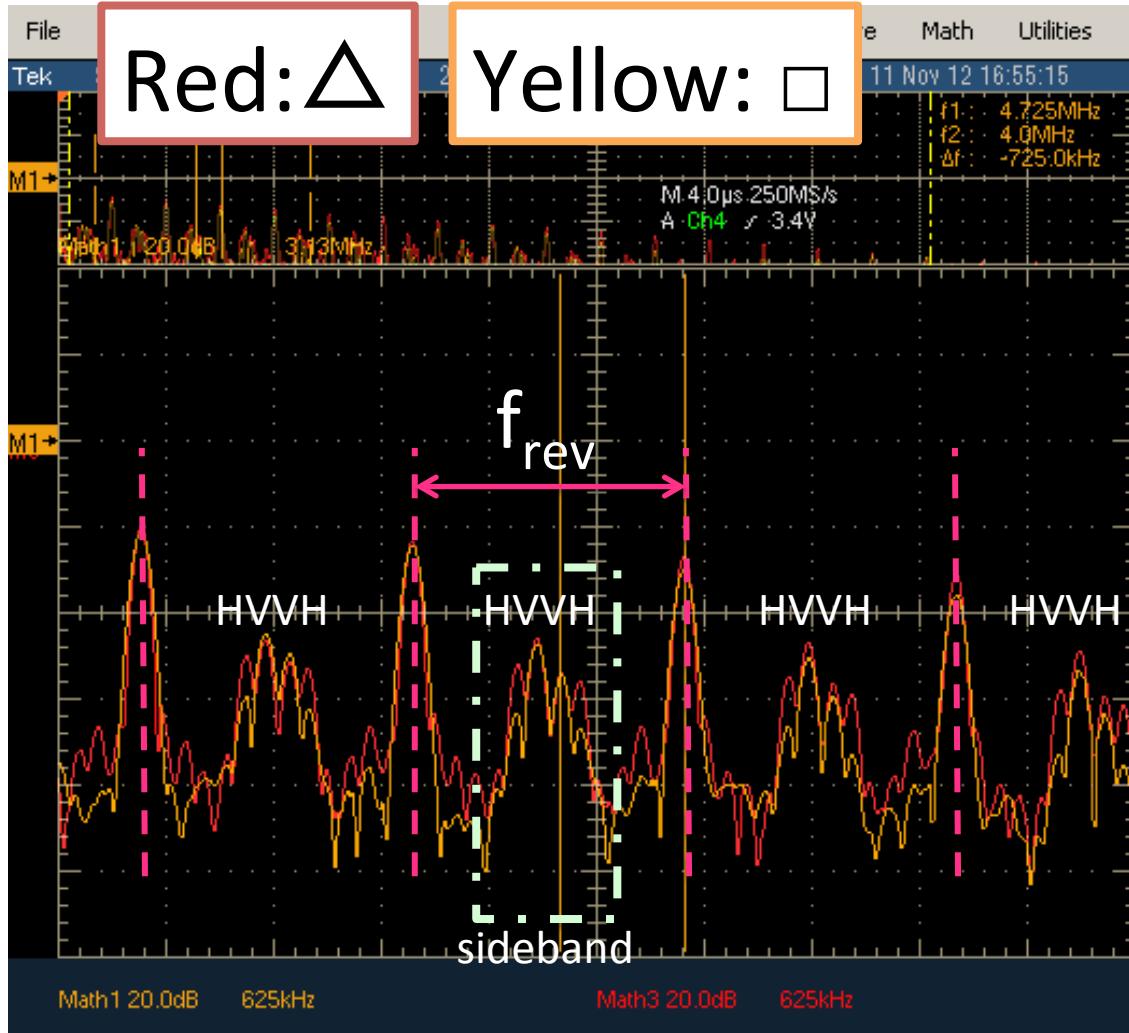
# How to measure



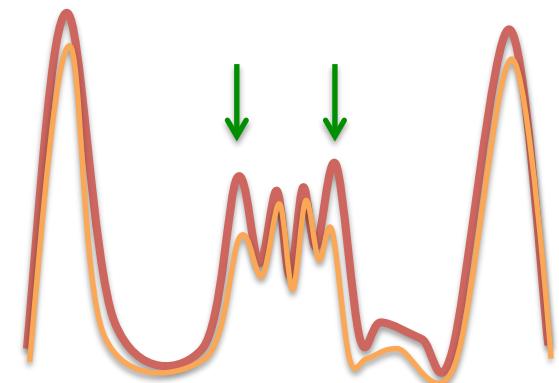
# Experiments



# Experiments



H: horizontal  
V: vertical



These difference show horizontal position

We want to make it more surely...

# Experiments

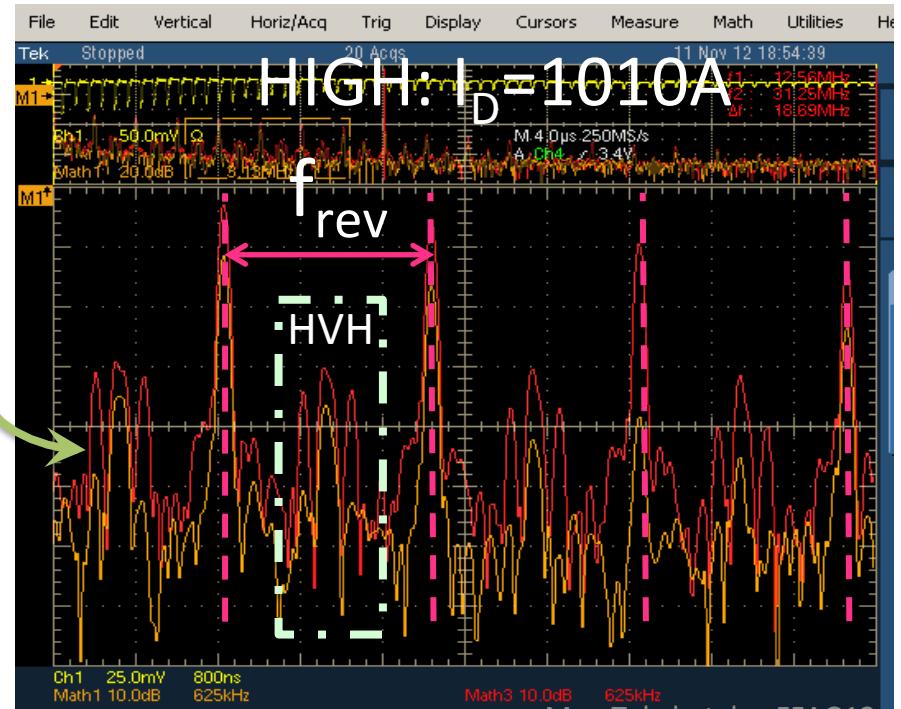


Red:  $\Delta$

$$\nu_x^2 \approx 1 + k$$
$$\nu_y^2 \approx -k + F^2(1 + 2 \tan^2 \varepsilon)$$

Yellow:  $\square$

$$F^2 = \frac{\langle (B - B_{ave})^2 \rangle}{B_{ave}^2}$$

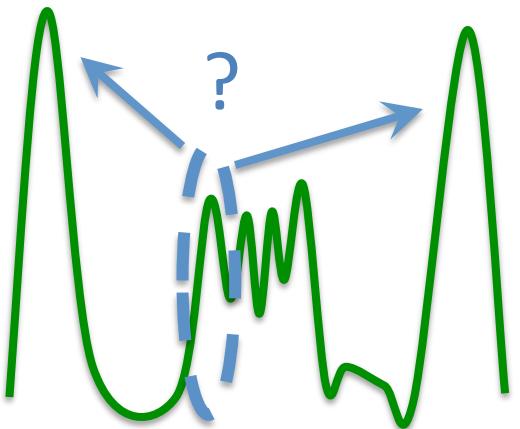


They differ in the current  
of defocus magnet

The spectrum of V unites!

# Result

$I_D[A] (F/D)$	970 (814/970)	1010 (814/1010)
$f_{rev}[\text{MHz}]$	1.575	1.575
$f_{side}[\text{MHz}] : \text{horizontal}$	0.6125	0.6094
$f_{side}[\text{MHz}] : \text{vertical}$	0.725	0.740
$v : \text{horizontal}$	0.388 OR 0.612	0.386 OR 0.614
$v : \text{vertical}$	0.460 OR 0.540	0.470 OR 0.530

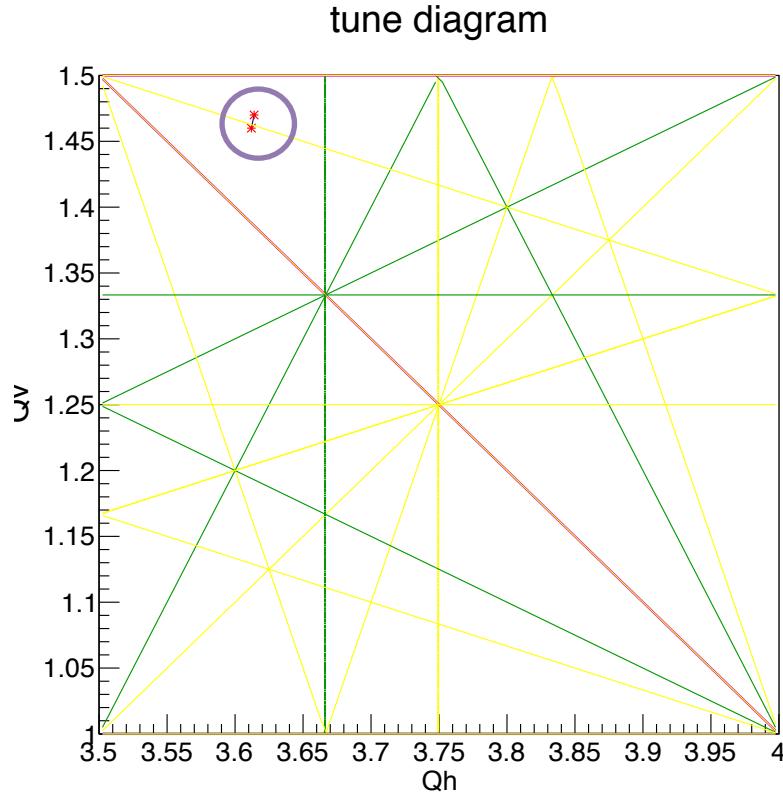


We **cannot** judge only  
by experimental result  
which harmonic of the  
spectrum is master.

# Estimation

- How to judge which is master?

→ We must check design of this ring



$I_D[A]$ (F/D)	970 (814/970)	1010 (814/1010)
$v$ : horizontal	0.612	0.614
$v$ : vertical	0.460	0.470



# Summary

---

- We measured betatron tunes for 2 different F/D ratios.
- We estimate betatron tunes.
- Betatron tunes is ...

$I_D [A]$ (F/D)	970 (814/970)	1010 (814/1010)
<b>v : horizontal</b>	0.612	0.614
<b>v : vertical</b>	0.460	0.470